

Nuclear Arms Control: Optimising Verification Procedures Through Formal Modelling

Paul Beaumont¹, Neil Evans², Michael Huth¹, Tom Plant²

1: Imperial College London, London, UK

2: Atomic Weapons Establishment, Aldermaston, UK

Scenario

- One role of AWE is to advise the UK Government on entering any potential nuclear treaty
- Such advice can be informed by models of potential inspection regimes in order to build trust between treaty parties, and be self-assured that all parties are treaty-compliant
- Mathematical models need to express uncertainty about weapons arsenals and nations' intent, and ability to optimise models to find the 'best' inspection regime.

Inspecting items whilst using IBs

- AWE are interested in a modelling approach because **information barriers** (IBs) and incomplete information in nuclear arms inspections lead to uncertainty in decision making processes.
- Modelling what a nation or organisation inspecting a 'host' nation would believe based on their observations (and their inherent uncertainty) during an inspection is important to decision making.

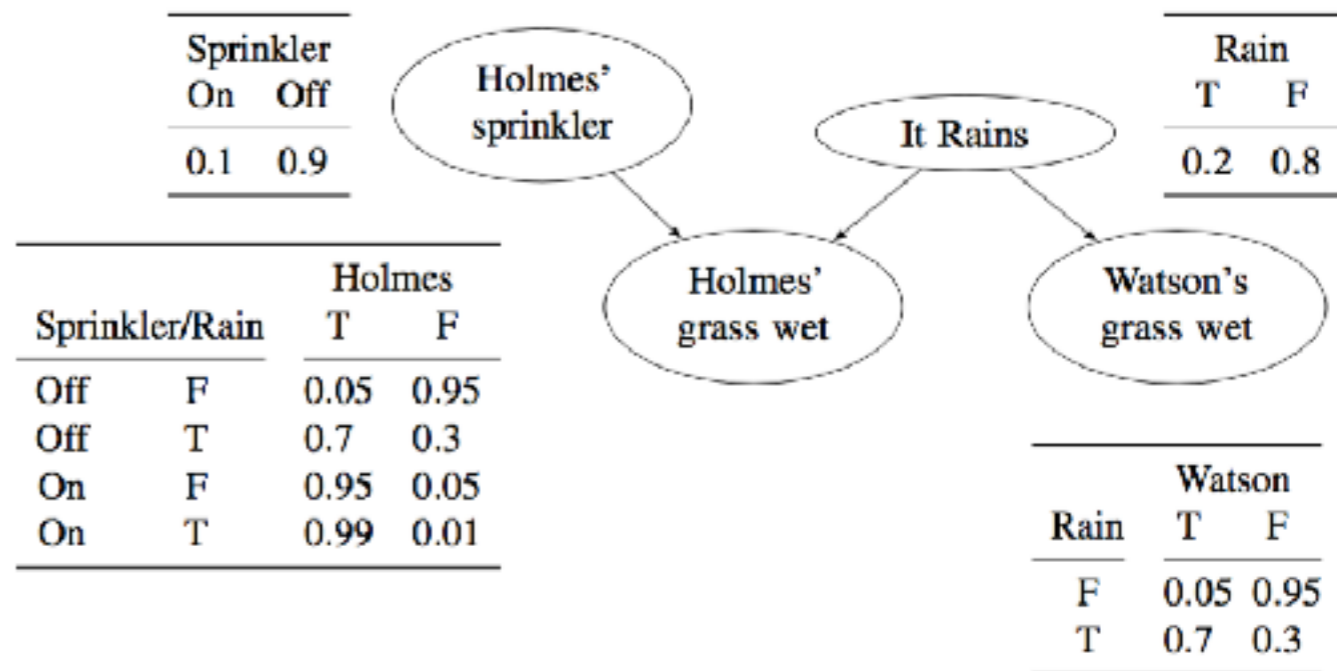


Proposed solution

- We express and analyse such **uncertainty** in models through formal parameters, e.g. x as well as alerting any additional constraints on our model. For example, we could estimate another nation has 'x' weapons where $low < x < high$.
- The constraint solver finds values of x that satisfy all constraints given to it, or reports that this is impossible.
- We can also optimise such satisfiability, e.g. to identify the worst-case weapons arsenal within the constraints.

Mathematical background

- **Bayesian Belief Networks** (BBNs) are graphs that capture the relationships and dependencies between multiple **events**, and their associated conditional probabilities.
- We proposed a methodology for **analysing these models** when **probabilities are uncertain**. We can compute worst-case scenarios in models faced with such uncertainty.



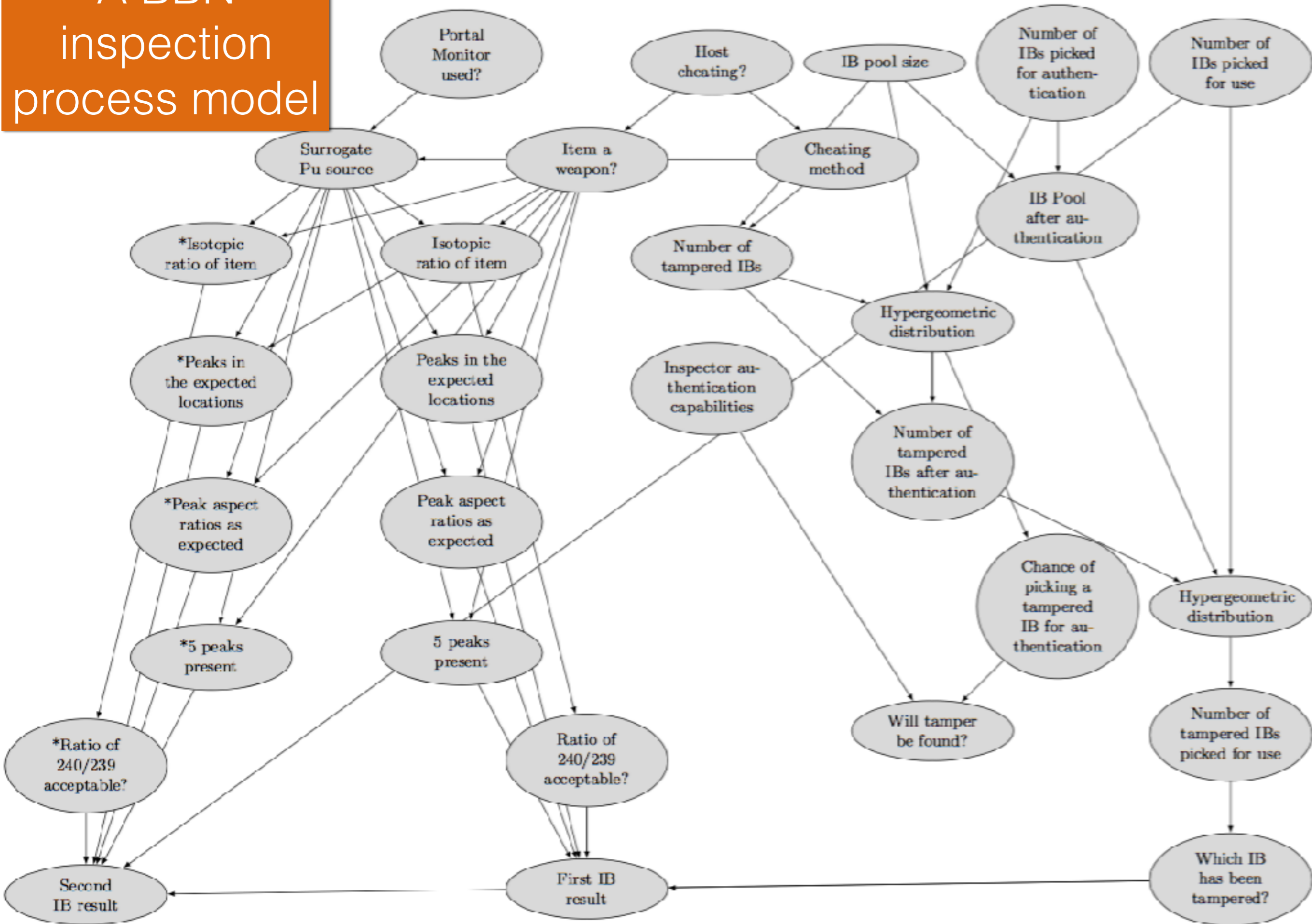
Confidence analysis for nuclear arms control: SMT abstractions of Bayesian Belief Networks

Paul Beaumont¹, Neil Evans², Michael Huth¹, and Tom Plant²

¹ Department of Computing, Imperial College London, London, SW7 2AZ, UK
{m.huth, paul.beaumont09}@imperial.ac.uk

² AWE Aldermaston, Reading, Berkshire, RG7 4PR, UK
{Neil.Evans, Tom.Plant}@awe.co.uk

A BBN inspection process model

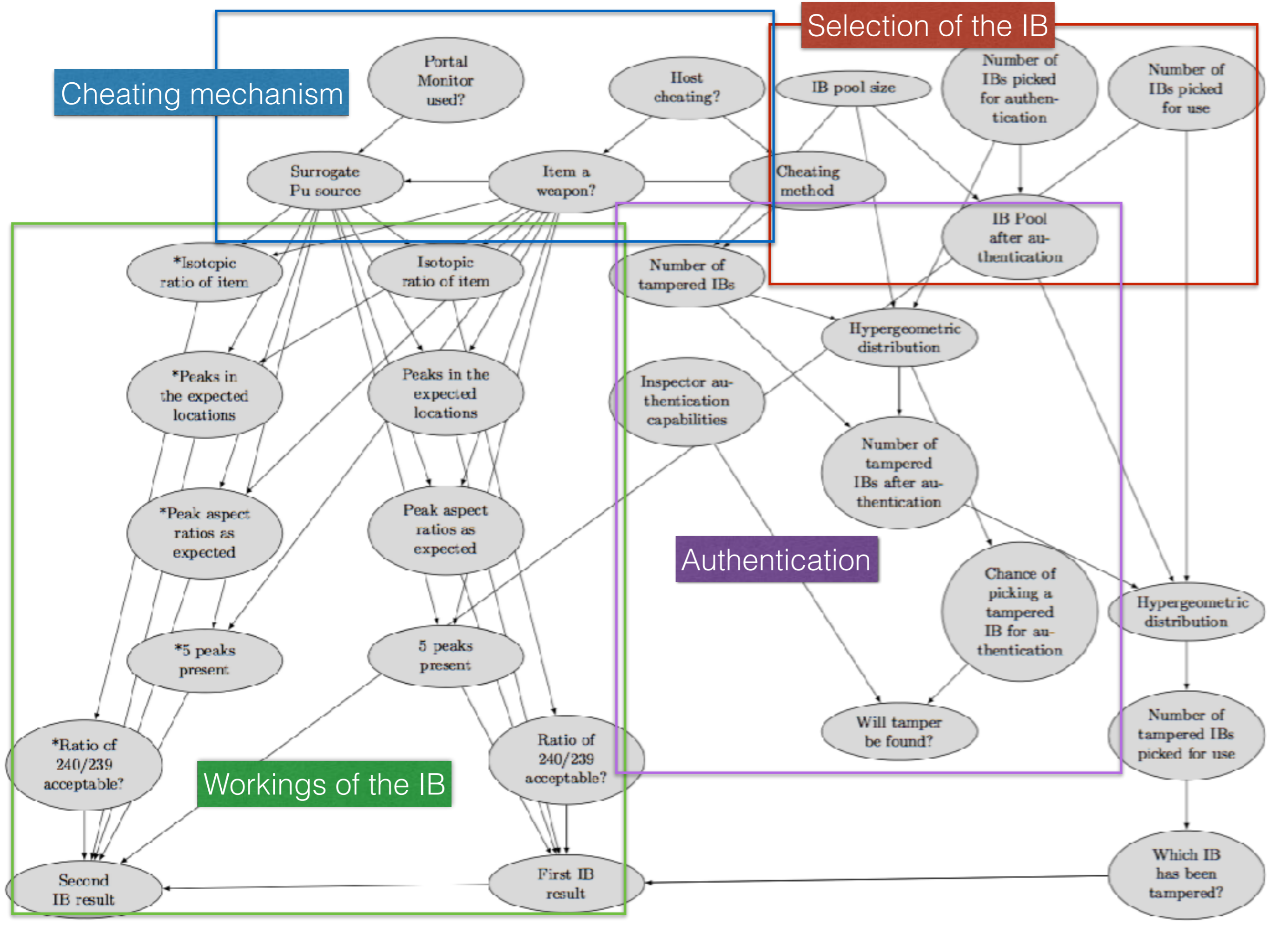


Cheating mechanism

Selection of the IB

Workings of the IB

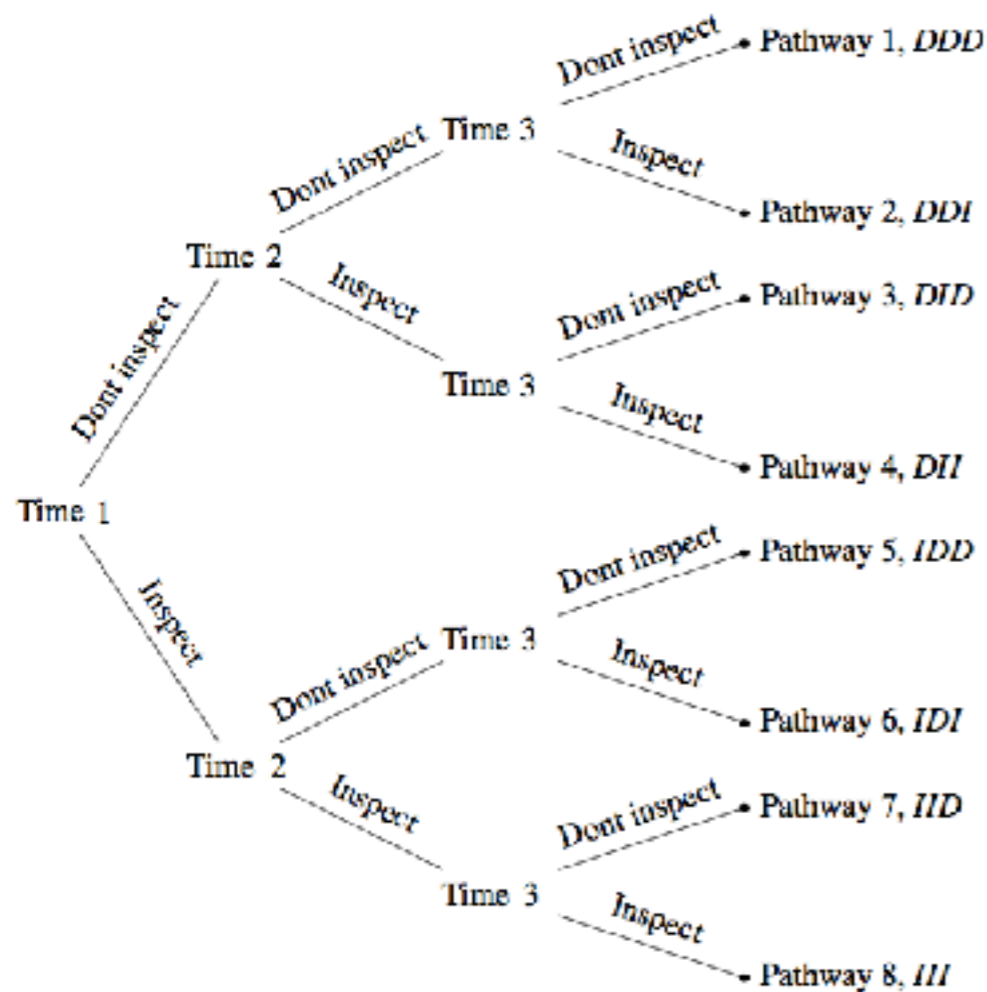
Authentication



Example query

- Given we **definitely observe no tamper abnormalities** on the authenticated IBs, what effect does **uncertainty over whether the portal monitor (body scanner) functioned correctly**, have on the likelihood of the **IB reporting positively** that it believes nuclear material is present?
- Our approach shows the likelihood at which the IB would return positively **varies in the range 0.5 to 0.7**.
- We are in a position to say that we guarantee, in this model, the results cannot vary outside of this range.

Dynamical systems for inspection routines



Dynamical System Pathways

- Dynamical Systems can be used to model changes **over time**.
- Equations describe our beliefs about how issues interact and influence each other (the number of weapons each has, declares, sees on inspections etc).
- We use these systems to **plan optimal inspection scheduling routines**.

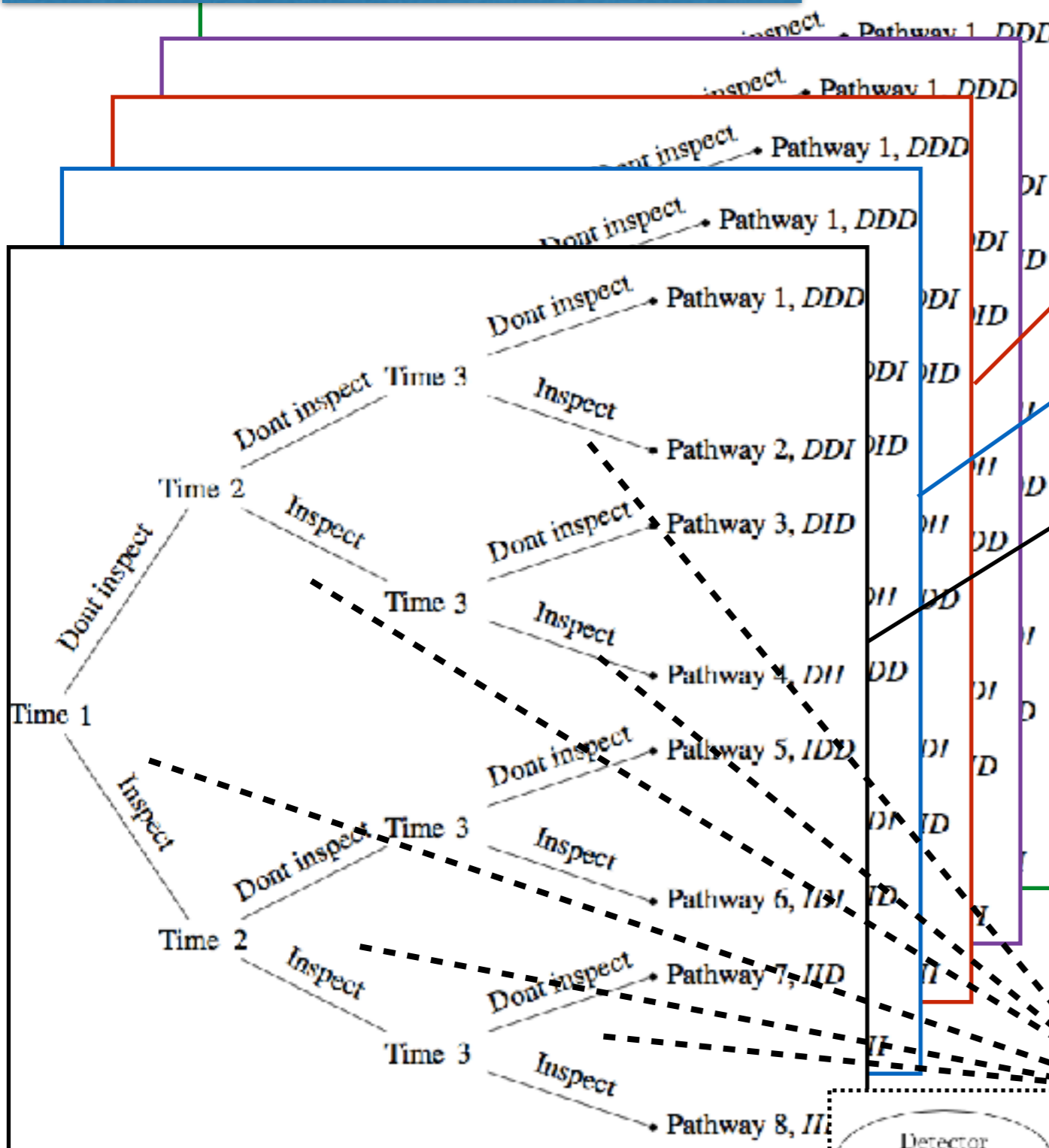
Example query

- For two nations in a treaty, they can each use **at most 3 unscheduled inspections**, none of which can happen at **adjacent time steps**. Scheduled inspections occur every 6 possible inspection time steps and start at time step 1. One nation's initial number of Weapons **is uncertain**, constrained by $low < W_0^{n1} < high$. What is the **minimum** number of weapons the other nation believes that the first owns by the last time step, and **what inspection schedule realises this**?
- Concrete values for W_0^{n1} , and inspection positions are returned, as well as values for all variables in all pathways for comparison.

A finer-grained model

- Dynamical Systems are good at modelling treaty interactions and events over time. Bayesian Networks offer a higher fidelity model of an inspection at a particular time step.
- There are some parameters that can't be varied within the Dynamical Systems model, but multiple instances of the model can be run to overcome this.
- Games can be used to help choose between different strategies - where these strategies could be the varying parameters of the Dynamical Systems model.
- We can use these models together successfully to model finer-grained detail of any potential treaty

Dynamical Systems model over time



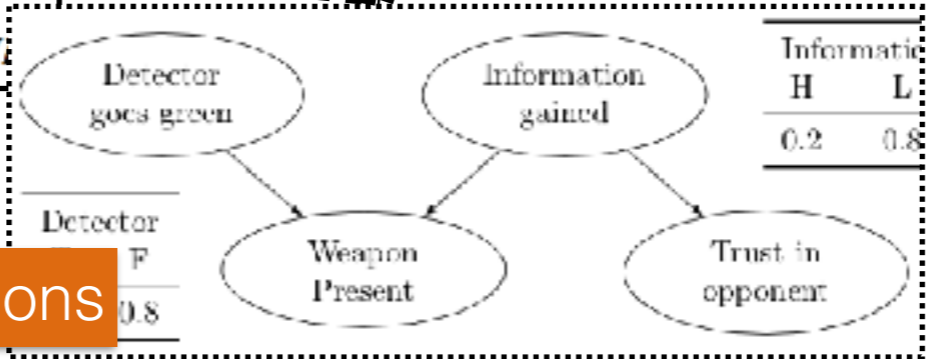
Game Theory solves for different parameters

$$\begin{matrix}
 (3 + x) & (5 + x) & (-1 + 4x) & (5 + 3x) \\
 (5 + 2x) & (3 - x) & (4 - 7x) & (x)
 \end{matrix}$$

Nash Equilibria

1. DS model treaty. Parameters that dictate setup of the DS are varied
2. Each inspection leads to a BBN call
3. DS are optimised for metric of interest
4. Optimal case informs GT payoff
5. Nash Equilibria denotes overall optimum strategy

BBNs model inspections



Analysis & conclusions

- Our approach allows a decision maker planning arms inspections to ask **pertinent questions** about mathematical models in which some of the data are **uncertain**, and to compute how answers may depend on variabilities in such uncertainty.
- Our models of arms control regimes can be run with different parameters, and different optimisations to find best, worst and most probable case scenarios, thus aiding decision support.
- The constraint solver provides answers to such analyses that are intelligible to the problem owner.
- Our approach scales well and could be used to evaluate treaty designs on the whole or the effects of rules within a treaty.
Applications in areas with decision-support needs without data.