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Swelling-induced telephone cord blisters in hydrogel films

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Abstract

Polymeric hydrogels can undergo dramatic shape and volumetric change when immersed into an appropriate solvent due to swelling or shrinking. Experimental studies have observed a variety of instability patterns in hydrogels. The telephone cord blister (TCB) with large deformability is one intriguing instability pattern but the assessment of its global morphology parameters, that is, the wavelength and transverse amplitude are still of inadequate appreciation. The present paper considers swelling-induced TCBs in a hydrogel-based film on a rigid substrate. Based on a previously developed theoretical framework for TCBs under small deformation, typically in a hard thin film, the theoretical derivations for the two global morphological parameters are furthermore developed for TCBs under large deformation in a soft thin film. Predictions for the morphology parameters of the developed theory agree very well with extensive experimental results. The critical mechanical conditions associated with the material-specific parameters such as the cross-linking density and swelling ratio are revealed. In addition, by reversing the calculation, the swelling-induced compressive stress in the un-delaminated film and the interfacial adhesion toughness are also accurately determined from measurements of the hydrogel TCBs. The present work provides an insight to design the microfluidics by controlling the morphology parameters with high precision.

Key words: Telephone cord blister, Compressive stress, Adhesion toughness, Hydrogel, Swelling, Buckling

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Nomenclature

Λ	linear swelling ratio of hydrogel
λ	wavelength of blister under small deformation condition
ν	Poisson's ratio of film
σ_0	swelling-induced compressive stress in film
$\tilde{\lambda}$	wavelength of blister under large deformation condition
\tilde{A}_y	transverse amplitude of blister under large deformation condition
A_x	height of blister
A_y	transverse amplitude of blister under small deformation condition
E	Young's modulus of film
G_c	interface adhesion toughness of film/substrate material system
h	thickness of film
R	half-width that is perpendicular to the sinusoidal centreline of blister

1. Introduction

Thin films with thick substrates composites systems are ubiquitous in modern daily life and scientific and engineering applications. The films are in either hard or soft form depending on individual situations, and blisters of various morphologies can be formed in these films either on purpose or occurring as a damage. Therefore, it is of great value to have a better understanding of blisters formation mechanics and a capability for predicting their morphologies. For hard films, the generation and development of blisters are deemed to be undesirable as the function of the structural component will be lost. For instance, if blisters and spallation failure occur in thermal barrier coating material systems, the underneath metallic substrate will be exposed to the high-temperature and corrosion environment, leading to the loss of metals [1, 2]. In contrast, three-dimensional (3D) bioinspired configurations in soft materials are however desirable in the fields of Tissue Engineering [3], Biomedical Engineering [4], *etc.* since the highly deformable morphologies offer opportunities for novel designs, for instance, soft microfluidic control systems and soft biomimetic robotics that are inspired by the water circulation of mimosa leaves [5]. The large morphological deformation in a homogeneous soft film can be created in response to a small change in environmental stimulus, but not limited to temperature, pH value, light, ionic strength, *etc.* [6]. Moreover, by aligning anisotropic additions, composite soft materials exhibiting anisotropic swelling or inhomogeneous stimuli-response are used in the design of soft sensors or actuators [7–10].

21 The deformation of blisters and their morphologies are often related to deformation
22 instability. A variety of deformation instability patterns have been identified in ex-
23 perimental studies [11–16] including wrinkles, creases, folds, ridges, *etc.* for both hard
24 and soft thin films subjected to geometric confinement or mechanical loadings. From
25 a conventional mechanical viewpoint, such structural instability patterns are caused by
26 buckling or post-buckling that is driven by initial compressive stresses in the films before
27 de-bonding at the interface. For hard film systems, the compressive stresses are usually
28 led by mismatch strains between the dissimilar materials; however, for the soft materials
29 such as a cross-linked polymer network film, when immersed in an appropriate solvent
30 swelling occurs due to diffusion of the solvent. This in turn brings about large volumetric
31 growth and compressive stresses in the soft material. For the buckling-driven delami-
32 nation, an initial interface separation of critical size is required for given compressive
33 stresses [17, 18]. Several studies [19–21] have proposed methods to design and fabricate
34 deformable patterns with special considerations given to modifying the film thickness,
35 the chemical composition such as the cross-linking density, the surface bonding geometry,
36 the localised adhesion, the swelling degree, and the environmental sensitivity.

37 Takahashi *et al.* [20] created some distinctive 3D architectures in hydrogel-based thin
38 films immersed in deionised water by processing selective adhesiveness at the interface.
39 It was experimentally observed that a straight-sided blister was formed and developed at
40 first during swelling in deionised water. After 170 s, it transformed to a TCB that prop-
41 agated forward with wavy boundaries between the hydrogel film and the substrate. The
42 TCB reached equilibrium in 600 s with progressive interface delamination and exhibited
43 a large transverse amplitude-to-wavelength ratio which manifests deep post-secondary-
44 buckling with large geometrical nonlinearity. The single-layer hydrogel film was further-
45 more covered with less-swellable bulk gels, creating a stacked hydrogel composite device.
46 The stacked bulk gel acts as not only reinforcement matrix that stabilizes the micro-
47 channel architecture even at high flow rates for a long duration, but also a diffusive
48 matrix that cultures cells [21].

49 Although Takahashi *et al.* [20, 21] performed systematic research to identify the pa-
50 rameters determining the formation and development of 3D architectures, quantitative
51 analysis upon the correlations with the film thickness, cross-linking density, swelling ra-
52 tio, and the geometry of the non-adhesive interface is still required for the design of
53 microfluidic devices via artificially controlling the morphology parameters. Particularly,
54 when the critical condition for conventional buckling is not satisfied, *i.e.*, the magnitude
55 of swelling-induced compressive stress is smaller than the critical value, or alternatively
56 the width of the non-adhesive region at the interface is small, the ‘ Ω -formulae’ for the
57 TCB in equilibrium developed by Yuan *et al.* [22] can be used to quantify the morphology
58 parameters. It is noted that the Ω -formulae are based on a novel mechanical hypothe-
59 sis originally proposed in Refs. [23, 24], that is, the delamination is driven by pockets of
60 energy concentration. For the highly deformable and flexible soft hydrogel film, it is iden-
61 tified that the Ω -formulae for thin TCBs with small transverse amplitude-to-wavelength
62 ratios still give accurate predictions for the two local morphology parameters, that is,
63 the height and width; however, they are unable to give accurate predictions of the two
64 global morphology parameters, that is, the wavelength and transverse amplitude. It is
65 therefore necessary to furthermore develop the analytical Ω -formulae for TCBs with large
66 deformability in soft thin films.

67 Based on the analytical mechanical models for the instability patterns in soft and

wet materials, the morphology-oriented design would be with higher precision by programming the associated physical parameters, and more importantly, it would provide theoretical tools for the determination of the swelling-induced stress and interface adhesion toughness of soft thin films through blister test [25, 26].

The present study aims to apply and develop the mechanical model proposed in Ref. [22] for the morphology assessment of the TCBs created in hydrogel-based thin films. This paper is organised as follows. Section 2 will present the analytical mechanical model for the TCBs under small and large deformation conditions, with a particular focus on the estimations of the wavelength and the larger transverse amplitude. In addition, mechanical models will be developed to determine the swelling-induced compressive stress in the hydrogel film and the adhesion toughness between the film and the substrate. Section 3 will examine the mechanical models by using the independent experimental results presented by Takahashi *et al.* [20, 21], and a discussion on the blistering mechanism in hydrogel-based films will also be provided. The concluding remarks will be given in Section 4.

2. Analytical mechanical model for telephone cord blisters

2.1. The Ω -formulae for TCBs under small deformation

Yuan, *et al.* [22] studied the spontaneous formation and morphology parameters of the TCBs in hard thin films under biaxial compressive residual stresses by assuming the existence of a pocket of energy concentration instead of an interface separation of critical size. By applying the Von Kármán geometrically nonlinear mechanics and the interfacial mixed-mode fracture mechanics, completely-analytical formulae, *i.e.*, the Ω -formulae are derived for the two local morphology parameters of TCBs of any shape, that is, width $2R$ and height A_x , and for the two global morphology parameters of TCBs of sinusoidal shape, that is, the wavelength λ and transverse amplitude A_y , as schematically shown in Figure 1. To help readers understanding the present development of the analytical mechanical model, a brief introduction of the theoretical derivations is thought to be necessary.

As shown in Figure 1, the local half-width R and height A_x for the fully-developed TCBs are respectively given by

$$R = 2h \left[\frac{\pi^2 E \Omega \bar{\Omega}}{12(1-\nu^2)\sigma_0} \right]^{1/2} \quad (1)$$

and

$$A_x = \frac{4h\Omega^{1/2}\bar{\Omega}}{\sqrt{3}}, \quad (2)$$

where Ω and $\bar{\Omega}$ are expressed as

$$\Omega = \frac{h(1-\nu^2)\sigma_0^2}{2EG_c} = \frac{(1-\nu^2)\sigma_0\varphi_0}{2E} \quad \text{and} \quad \bar{\Omega} = 1 + \left(1 - \frac{3}{2\Omega}\right)^{1/2} \quad (3)$$

with h , E , and ν being the thickness, Young's modulus and Poisson's ratio of the thin film, respectively; σ_0 represents the compressive residual stress before the interface delamination occurs, and G_c represents the interface adhesion toughness between the film

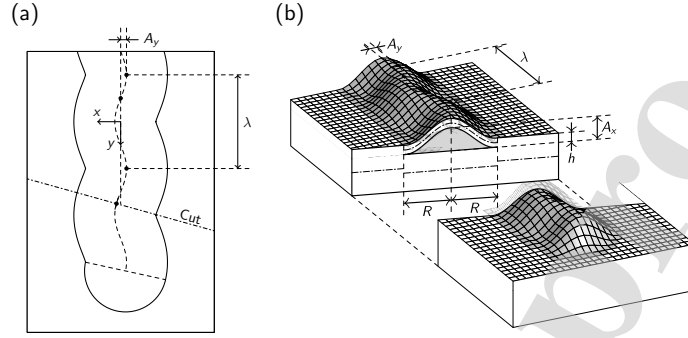


Figure 1: A telephone cord blister of sinusoidal shape. (a): Top view. (b): 3D view of a cut which is perpendicular to the sinusoidal centreline of the TCB.

99 and the substrate, and $\varphi_0 = h\sigma_0/G_c$. It is seen from Eq. (3) that parameter Ω indicates
 100 the ratio between the plane-strain energy density within the thin film before the interface
 101 delaminates and the interface adhesion toughness.

The global wavelength λ and transverse amplitude A_y , as shown in Figure 1 are respectively given by

$$\lambda = 2R \left(\frac{1 - \nu\Omega}{\Omega - 1} \right)^{1/2} \quad (4)$$

and

$$A_y = \frac{\lambda}{\pi} (\bar{A}_y - 1)^{1/2}, \quad (5)$$

with

$$1 + 3\Omega\bar{\Omega}^2 + 2\bar{A}_y^2[\bar{A}_y^2 - 2\Omega\bar{\Omega}(2\bar{A}_y - 1)] = 0. \quad (6)$$

102 It is seen that the analytical Eqs. (1) to (5) derived for the four morphology pa-
 103 rameters are determined by the unique parameter Ω ; therefore, they are together called
 104 ‘ Ω -formulae’ in Ref [22] and current work. Note that the Ω -formulae are only fitting
 105 to the TCBs in hard thin films, under the condition of small deformation, exhibiting
 106 small transverse amplitude-to-wavelength ratios which are usually less than approxi-
 107 mately 1/10. Furthermore, the accuracy of Ω -formulae for predicting the formation,
 108 morphology, compressive residual stresses, and interface adhesion toughness have been
 109 intensively validated by extensive independent experimental data in Ref. [22]. It is con-
 110 vincingly demonstrated a thin film blistering process driven by the pocket of energy
 111 concentration rather than by buckling.

112 2.2. The Ω -formulae for TCBs under large deformation

As soft hydrogel-based material is highly deformable and flexible, TCBs in hydrogel
 thin films exhibit very large transverse amplitude-to-wavelength ratios suggesting deep
 post-secondary-buckling with large geometrical nonlinearity. The Ω -formulae Eqs. (1)
 and (2) still give accurate predictions for the local width and height; however, Eqs. (4)

to (6) are unable to give accurate predictions for the global wavelength and transverse amplitude for the TCBs under large deformation. It has demonstrated that all four morphology parameters of TCBs are dependent on the parameter Ω . Therefore, empirical formulae are developed below by further correcting Eqs.(4) and (5) for the TCBs in the soft hydrogel-based films. By using the wavelength λ from Eq. (4), the corrected wavelength $\tilde{\lambda}$ for TCBs under large deformation is expressed as

$$\tilde{\lambda} = \lambda\Omega\bar{\Omega}^{1/2}. \quad (7)$$

Next, substituting $\tilde{\lambda}$ into Eq. (5) leads to the corresponding \tilde{A}_y , and it is furthermore inserted into following Eq. (8) to obtain the new \tilde{A}_y for the TCBs under large deformation, that is,

$$\tilde{A}_y = A_y\Omega\bar{\Omega}. \quad (8)$$

113 Now all four morphology parameters for the TCBs in hydrogel-based soft films that
114 exhibit large deformability can be determined.

115 2.3. Determination of swelling-induced compressive stress and interface adhesion tough- 116 ness

117 It will be shown in Section 3 the validity of the developed Ω -formulae for TCBs under
118 large deformation can be accurately examined by the independent experimental data of
119 TCBs in the soft hydrogel-based films presented in Ref. [20, 21]. This motivates the
120 current development of mechanical models to determine the swelling-induced compressive
121 stresses in gel-based thin film, and the adhesion toughness between the film and the
122 substrate by reversing the developed Ω -formulae presented in Sections 2.1 and 2.2 and
123 using the experimental measurements of morphology parameters of TCBs. The detailed
124 derivations are shown as follows.

125 2.3.1. Determination of swelling-induced compressive stress in gel-based films

126 Three mechanical models are developed to determine the swelling-induced compressive
127 stress by using the morphology parameters of the fully-developed TCB in soft gel-
128 based thin films.

(1) Use the measurements of TCB local half-width R and height A_x . The parameter Ω is intended to obtain at first, which is derived from Eq. (2), that is,

$$\Omega = 3 \left(\frac{A_x}{8h} + \frac{h}{A_x} \right)^2. \quad (9)$$

Note that Eq. (9) is identical to Eq. (2) in Ref. [27], which indicates its applicability to both TCBs and circular blisters. Next, by using Ω given by Eq. (9) and the measured R , the swelling-induced compressive stress in the gel-based thin film can be given by Eq. (10) which is derived from Eq. (1):

$$\sigma_0 = \frac{E\pi^2\Omega\bar{\Omega}}{3(1-\nu^2)} \left(\frac{h}{R} \right)^2. \quad (10)$$

It is seen that Eq. (10) is insensitive for $\Omega \gg 1.5$. When $\Omega = 1.5$, Eq. (11) is suggested:

$$\sigma_0 = \frac{E\pi^2}{2(1-\nu^2)} \left(\frac{h}{R} \right)^2. \quad (11)$$

(2) Use the measurements of local width $2R$ and global wavelength $\tilde{\lambda}$. Based on Eqs. (4) and (7), the ratio of wavelength to width satisfies Eq. (12) that is again subjected to the parameter Ω if Poisson's ratio ν is constant, that is,

$$\frac{\tilde{\lambda}}{2R} = \Omega \left[\frac{\tilde{\Omega}(1 - \nu\tilde{\Omega})}{\tilde{\Omega} - 1} \right]^{1/2}. \quad (12)$$

129 (3) If the interface adhesion toughness G_c is known, then Eq. (3) can be inserted into
130 Eq. (9) or (10) or (12) to directly obtain the swelling-induced compressive stress without
131 calculating the Ω values.

132 2.3.2. Determination of interface adhesion toughness

133 Four mechanical models are developed to determine the interface adhesion toughness
134 by using the morphology parameters of the fully-developed TCB in soft gel-based thin
135 films.

(1) If the measurement of swelling-induced compressive stress σ_0 before the interface delamination occurs is known, then the measurement of blister height A_x can be used. Insert Eq. (3) into Eq. (9) to obtain the interface adhesion toughness G_c , that is,

$$G_c = \frac{h\sigma_0^2(1 - \nu^2)}{6E} \left(\frac{A_x}{8h} + \frac{h}{A_x} \right)^{-2}. \quad (13)$$

(2) Use the measurement of σ_0 and local half-width R of fully-developed TCBs. Substituting Eq. (3) into Eq. (10) leads to

$$G_c = \frac{\pi^2 h \left[4\sigma_0 (R/h)^2 - \pi^2 E / (1 - \nu^2) \right]}{12 (R/h)^4}. \quad (14)$$

It is also seen that Eq. (14) is insensitive for $\Omega \gg 1.5$. When $\Omega = 1.5$, by using Eq. (3) and Eq. (11), the adhesion toughness is calculated as

$$G_c = \frac{h\sigma_0^2(1 - \nu^2)}{3E} = \frac{h\pi^4 E}{12(1 - \nu^2)} \left(\frac{h}{R} \right)^4. \quad (15)$$

136 (3) Use the measurements of σ_0 , and the TCB global wavelength $\tilde{\lambda}$ and local width
137 $2R$, the interface adhesion toughness G_c can be obtained by combining Eqs. (3) and
138 (12).

139 (4) If the measurement of σ_0 is unknown, Eqs. (9) to (12) presented in Section 2.3.1
140 can be used initially to determine the σ_0 value. Then, substitute the σ_0 value into the
141 above methods to obtain the interface adhesion toughness G_c .

142 In general, G_c value obtained by above-mentioned methods is independent of the
143 mixed-mode fracture partition theories. If, however, the mode I and mode II adhesion
144 toughness are specified individually to determine the overall adhesion toughness, then the
145 TCB morphology parameters do depend on the mixed-mode fracture partition theory,
146 as various fracture partition theories will bring about various values, as illustrated in
147 Ref. [22].

148 3. Experimental validation and discussions

149 3.1. The validation of Ω -formulae for TCBs under large deformation

150 The Ω -formulae under large deformation are now validated by using the independent
 151 experimental measurements of TCB morphology reported by Takahashi *et al.* [20, 21].
 152 Readers are encouraged to read their work for the experimental details to fabricate robust
 153 architectures via selective swelling in hydrogel-based films. Here only key information
 154 with respect to the examinations of Ω -formulae are presented.

155 Takahashi *et al.* [20, 21] prepared silanised glass coverslips and chemically modi-
 156 fied with 3-(trimethoxysilyl)propyl methacrylate (TMSPMA) so that it would cova-
 157 lently bond to the polyacrylamide (PAAm)-based hydrogel film cross-linked by N,N'-
 158 methylenebis[acrylamide] (MBAA). Note the monomer concentration used in Refs. [20,
 159 21] were about 4 M that is much higher than 0.5–2 M for conventional PAAm gels. Also,
 160 as the monomer concentration increases, the cross-link density may also increase due
 161 to entanglement. The overall effect of the high monomer concentration and cross-link
 162 density is to increase the Young's modulus of the hydrogel film as reported in the original
 163 work. For the single-hydrogel-film composite system prepared in Ref. [21], the Young's
 164 modulus is $E = 82.7$ kPa, and the Poisson's ratio is $\nu = 0.5$ indicating incompressible gel,
 165 and the swelling ratio is $\Lambda = 1.39$, respectively. By using the photolithographic and oxy-
 166 gen plasma etching techniques, selective non-adhesive rectangular regions were produced
 167 at the interface. Therefore, when the film/substrate material system was immersed in
 168 the large amount of deionised water, two swelling behaviours were observed: one was
 169 the confined swelling where the bottom surface of the hydrogel film was restricted by
 170 the substrate thanks to the strong adhesion led by covalent bonds generated between the
 171 hydrogel and TMSPMA, and the other one is the side-fixed swelling in the non-adhesive
 172 regions where non-covalent interactions were formed, and the hydrogel can freely swell
 173 in the thickness direction but cannot expand to the adjacent fixed region. As a result,
 174 the swelling pressure and the boundary constraints together lead to biaxial compressive
 175 stresses in the hydrogel film. Furthermore, straight-sided blisters were initially observed
 176 and later transformed to the TCBs with continuous interfacial delamination until reach-
 177 ing equilibrium, which exhibit large transverse amplitude-to-wavelength ratio $\hat{A}_y/\hat{\lambda}$.

Takahashi *et al.* [20, 21] regarded the hydrogel as a Neo-Hookean material, and the swelling-induced compressive stress in the hydrogel is suggested as

$$\sigma_0 = \frac{2E}{3} \left(\frac{1}{\Lambda^2} - \Lambda^4 \right). \quad (16)$$

178 where Λ represents the linear swelling ratio. Note that the deformation of the free
 179 swollen gel compresses in biaxial directions; therefore, the compressed swelling ratio $1/\Lambda$
 180 has been inserted into Eq. (16). It is considered that the validation of the accuracy
 181 and applicability of Eq. (16) would be of significant value. In addition, Takahashi
 182 *et al.* [20, 21] consider that the swelling-induced compression drives buckling occur in
 183 the hydrogel film due to the pre-prepared non-adhesive region at the interface, which
 184 subsequently generates TCBs with the stress relief. There are two stages of blister
 185 growth in the buckling-based approach: first, when the size of the non-adhesive region
 186 at the interface reaches the buckling requirement, or alternatively the swelling-induced
 187 compressive stress is sufficient to trigger buckling, the free-swelling hydrogel starts to

Table 1: Comparison of compressive stress given by Ω -formulae, Neo-Hookean model, and buckling-based approach

Experimental measurements Ref. [21]			Theoretical predictions				
Thickness h (μm)	Width $2R$ (μm)	Height A_x (μm)	Ω	Compressive stress σ_0 (kPa)			
				Ω -formulae Eq. (11)	Neo-Hookean Eq. (16)	Buckling-based (straight blister model)	Buckling-based (pinned-circular blister model)
89.68	319.58	253.26	1.500	171.4	177.3	199.43	163.42

188 bend away from the substrate, forming the blister with energy release rate at the original
 189 fixed sides. Second, at a critical size slightly larger than the buckling requirement the
 190 energy release rate exceeds the adhesion toughness at the interface and the blister grows
 191 till to its equilibrium shape where the energy release rate at the boundaries is smaller than
 192 the interface adhesion toughness, and its growth stops. However, as will be demonstrated
 193 later by the careful calculations, it is found the original swelling-induced compressive
 194 stress before bending out is insufficient to generate the blister. In this circumstance, the
 195 authors of current paper argue that the blister growth is driven by an extra energy source,
 196 called pocket of energy concentration, in addition to the swelling-induced compressive
 197 stress. More specifically, the pocket of energy concentration drives the hydrogel film bend
 198 away from the substrate, and its propagation under the condition that non-adhesive areas
 199 at the interface are too small to trigger buckling. The blister energy which includes the
 200 strain energy and fractured surface energy, is larger than the initial compressive strain
 201 energy in the un-delaminated film and it increases until it reaches a maximum at the end
 202 of the first stage of the blister growth. Subsequently, the blister energy decreases, and the
 203 blister stops growing when the blister energy is balanced with the initial swelling-induced
 204 strain energy in the un-delaminated film. The detailed discussion of energy transitions
 205 between parts of TCBs can be further found in Ref. [22].

206 To identify which of above-mentioned mechanisms is capable to assess the TCB mor-
 207 phology under large deformation with good accuracy, the swelling-induced compressive
 208 stress in the single-hydrogel-film is therefore estimated as the first validation, by using
 209 the average measurement values of local half-width R and height A_x , as shown in Fig-
 210 ure 2 in which ‘Dist’ denotes the measured distance. Based on the Ω -formulae developed
 211 in Section 2, the value $\Omega = 1.5$ is initially calculated using Eq. (9). Accordingly, the pre-
 212 diction of swelling-induced compressive stress σ_0 is obtained by substituting the average
 213 measurement of R into Eq. (11). In addition, predictions of σ_0 based on the buckling
 214 approach for TCBs [13,14], namely, straight and pinned-circular blister models, and that
 215 out of Eq. (16) are also calculated, and the results are together recorded in Table 1.

216 It is seen from Table 1 that the predicted swelling-induced compressive stresses derived
 217 from the Ω -formulae and the Neo-Hookean material model are very close to each other;
 218 however, large difference is observed comparing with the results out of the buckling
 219 approaches. This indicates both Ω -formulae and the Neo-Hookean material model are
 220 suitable to estimate the swelling-induced compression for the TCBs in the hydrogel film
 221 presented in Ref. [20, 21]. For consistency, the swelling-induced compressive stresses
 222 in the hydrogel-based films discussed in this work are evaluated by the Neo-Hookean
 223 material model as given by Eq. (16). It is worth mentioning that the interface adhesion
 224 toughness G_c between the hydrogel film and the chemically modified glass coverslip can
 225 be furthermore obtained by using Eq. (15), that is, 8.52 J/m^2 , and the corresponding

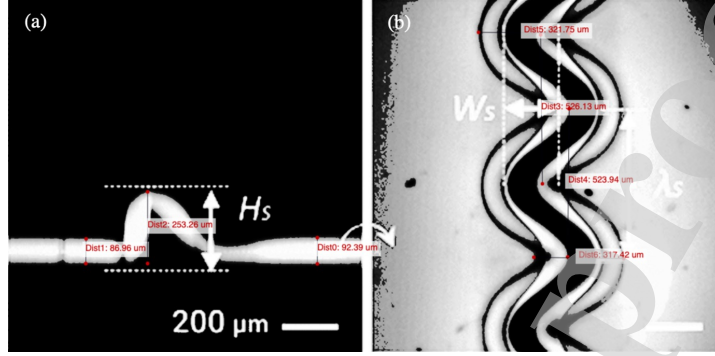


Figure 2: The first TCB under large deformation with morphology measurement. (a): The cross-section view in Grayscale (Dists 0 and 1 are film thickness, Dist 2 is blister height). (b): The top-view in Grayscale (Dists 3 and 4 are wavelength, Dists 5 and 6 are blister width, Coloured version can be found in Figure 2 in Ref. [21]).

Table 2: Comparison of the morphology parameters of the second TCB under large deformation

Experimental measurements Ref. [21]			Theoretical predictions			
Width	Wavelength	Transverse amplitude	Ω	Thickness	Height	Transverse amplitude
$2R$ (μm)	$\tilde{\lambda}$ (μm)	\tilde{A}_y (μm)		h (μm)	A_x (μm)	\tilde{A}_y (μm)
307.24	582.88	133.38	1.722	70.22	289.09	134.92

226 φ_0 is 1.8660. And note that the equations to determine the wavelength $\tilde{\lambda}$ and transverse
 227 amplitude \tilde{A}_y as demonstrated in Section 2 are not applicable because $\Omega = 1.5$; however,
 228 their ratio can be obtained as $\tilde{A}_y/\tilde{\lambda} = 0.1395$.

229 The following examinations are on the prediction accuracy of the TCB morphology
 230 parameters through the developed Ω -formulae. As shown in Figure 3, the second hydrogel
 231 TCB under large deformation is considered. The average measurement values of local
 232 width $2R$ and global wavelength $\tilde{\lambda}$ are substituted into Eq. (12) to obtain the Ω value.
 233 Then, together with the compressive stress $\sigma_0 = 177.3$ kPa given by Eq. (16), the
 234 resultant thickness of the swollen hydrogel film h is calculated. Next, the height A_x and
 235 the transverse amplitude \tilde{A}_y are respectively obtained by using Eq. (2) and Eqs. (5) to
 236 (8). The experimental and prediction results are summarized in Table 2.

237 The prediction of transverse amplitude \tilde{A}_y from the developed Ω -formulae, as shown
 238 in Table 2, reaches an excellent agreement with the measured value. It is therefore
 239 deduced that the corresponding predictions of the resultant thickness for the swollen
 240 hydrogel and the TCB height are reasonably accurate since they are correlated strictly
 241 with the unique parameter Ω . Furthermore, the interface adhesion toughness is estimated
 242 as 5.81 J/m², which is smaller than that illustrated in the first validation. The reason
 243 may be the thickness reduction of the hydrogel film. And the corresponding φ_0 is 2.1416.

244 In the third exercise, the developed Ω -formulae are examined by the TCB with the
 245 measurements of local height and global wavelength, $A_x = 320$ μm and $\tilde{\lambda} = 570$ μm ,

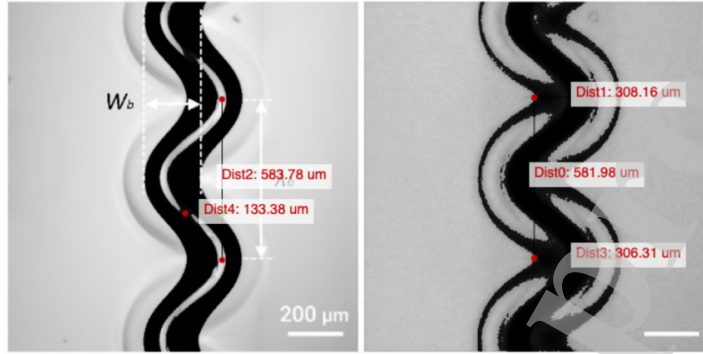


Figure 3: The second TCB under large deformation with morphology measurement. (a): Digital image correlation image (Dist 2 is wavelength, Dist 4 is transverse amplitude). (b) Fluorescent image in Grayscale (Dist 0 is wavelength, Dists 1 and 3 are blister width, Coloured version can be found in Figure S5 in Ref. [21]).

Table 3: Comparison of the morphology parameters of the third TCB under large deformation

Experimental measurements Ref. [21]		Theoretical predictions			
Height	Wavelength	Ω	Thickness	Width	Transverse amplitude
A_x (μm)	$\bar{\lambda}$ (μm)		h (μm)	$2R$ (μm)	\bar{A}_y (μm)
320	570	1.9416	67.33	326.20	164.16

246 respectively. Again, the swelling-induced compressive stress in the hydrogel film is $\sigma_0 =$
 247 177.3 kPa. It is therefore noted that Eqs. (9), (10) and (12) can be combined to solve
 248 the unknown parameters: Ω , h , and R . Then, the prediction of transverse amplitude \bar{A}_y
 249 is obtained by using Eqs. (5) to (8). The results are recorded in Table 3.

250 Since the experimental measurements of the local width and the global transverse
 251 amplitude for the TCB are not available, the accuracy of the predictions from the Ω -
 252 formulae for the third TCB is hard to conclude. Nevertheless, it is noted that the adhesion
 253 toughness between the hydrogel film and the chemically modified glass coverslip is 4.94
 254 J/m^2 and the corresponding φ_0 is 2.4154, which are close to the values for the second
 255 TCB shown in Figure 2. Particularly, the resultant thickness values of the hydrogel films
 256 after swelling are close. Under the condition of same swelling-induced compressive stress,
 257 it is furthermore deduced the TCB geometries outlined in Tables 2 and 3 are analogous
 258 to each other. And the morphology parameters of the two hydrogel-film/glass-substrate
 259 systems must be comparable. Therefore, by cross-validating the experimental results
 260 and theoretical predictions in Tables 2 and 3, it is concluded that estimations from the
 261 developed Ω -formulae for the third TCB are of good accuracy.

262 Now the experimental results presented in Ref. [20] are used to examine the developed
 263 Ω -formulae. Two kinds of fluorescein *o*-acrylate (FL) labelled PAAm-based hydrogels
 264 were chemically fabricated on the TMSPMA modified coverslip substrates. They were

Table 4: Comparison of the morphology parameters of the series of TCBs under large deformation

Experimental measurements Ref. [20]		Theoretical predictions					Width 2R (μm)	Wavelength $\tilde{\lambda}$ (μm)	'Amplitude' 2A _y (μm)
NaCl concentration or Temperature	Height A _x (μm)	'Amplitude' 2A _y (μm)	Ω	φ_0	Adhesion toughness G _c (J/m ²)				
(a) Ionic strength responsiveness – Poly (SA-co-FL-co-AAm)									
0 mM	424.95	376.57	1.8446	1.7539	18.30	384.6	688.07	363.16	
5 mM	383.62	338.18	1.7033	1.6196	19.82	358.2	688.82	311.85	
10 mM	377.44	327.77	1.6847	1.6019	20.04	354.34	692.20	306.04	
20 mM	349.13	307.27	1.6087	1.5297	20.99	336.88	725.75	287.05	
50 mM	344.9	279.61	1.5988	1.5202	21.12	334.32	734.28	285.51	
100 mM	336.44	268.22	1.5801	1.5024	21.37	329.22	755.35	288.77	
(b) Control hydrogel architectures in a – Poly (FL-co-AAm)									
0 mM	340.67	281.24	1.5892	1.5111	21.24	331.76	744.08	284.41	
5 mM	343.60	282.86	1.5958	1.5174	21.16	333.52	737.15	285.13	
10 mM	343.28	275.05	1.5950	1.5167	21.17	333.32	737.87	285.04	
20 mM	348.48	273.10	1.6072	1.5282	21.01	336.48	726.99	286.79	
50 mM	344.25	275.70	1.5973	1.5188	21.14	333.92	735.70	285.32	
100 mM	341.97	274.73	1.5921	1.5139	21.21	332.54	740.92	284.70	
(c) Thermo-responsiveness – Poly (NIPAM-co-FL-co-AAm)									
25 °C	388.87	337.43	1.7196	1.6351	19.63	361.5	686.76	317.20	
30 °C	388.31	327.64	1.7179	1.6334	19.65	361.16	686.95	316.61	
35 °C	357.65	298.30	1.6299	1.5498	20.71	342.08	711.84	291.28	
(d) Control hydrogel architectures in c – Poly (FL-co-AAm)									
25 °C	339.17	269.66	1.5859	1.5080	21.29	330.86	747.90	284.13	
30 °C	335.11	271.76	1.5773	1.4998	21.40	328.42	759.22	283.68	
35 °C	346.45	275.95	1.6024	1.5236	21.07	335.26	731.02	286.03	
40 °C	347.99	280.14	1.6060	1.5271	21.02	336.18	727.93	286.60	
45 °C	343.23	287.13	1.5950	1.5166	21.17	333.3	737.99	285.02	
50 °C	341.27	277.35	1.5906	1.5124	21.23	332.12	742.61	284.54	

functionalised by sodium acrylate (SA) to add ionic strength responsiveness and by N-isopropylacrylamide (NIPAM) to add thermo-responsiveness, respectively. It has been experimentally illustrated that the existence of FL in the PAAm polymer backbone does not affect the swelling ratio, mechanical properties such as the Young's modulus, and the morphology of 3D architectures in the hydrogel-based thin film. Next, the hydrogels were immersed in the deionised water for 24 h, and it was observed that TCBs of large $\tilde{A}_y/\tilde{\lambda}$ ratios were generated spontaneously due to swelling, as shown in Figure 4. For the hydrogel with 0.3 mol % cross-linking density, the Young's modulus and Poisson's ratio of are $E = 121$ kPa and $\nu = 0.5$, respectively. And the hydrogel film thickness after swelling is $h = 94.6$ μm with the swelling ratio $\Lambda = 1.47$ determined from the experiment. Therefore, the biaxial compressive stress induced by swelling is calculated as 339.34 kPa based on Eq. (16).

By using the measurements of TCB height A_x provided from Ref. [20] and Eq. (9), the Ω values for the prepared single-hydrogel-film/glass-coverslip systems are determined. Then the corresponding interface adhesion toughness G_c and φ_0 are obtained based on Eqs. (3) and (14). Furthermore, the TCB local half-width R and 'amplitude', as defined in Ref. [20] $2\tilde{A}_y$ are respectively given by Eqs. (1) and Eqs. (5) to (8). All the theoretical predictions are shown in Table 4.

It is seen from Table 4 that the predicted 'amplitudes' are very close to the experimental measurements, which means the developed Ω -formulae for the two global morphology parameters of TCBs under large deformation again work well. Note that the φ_0 values

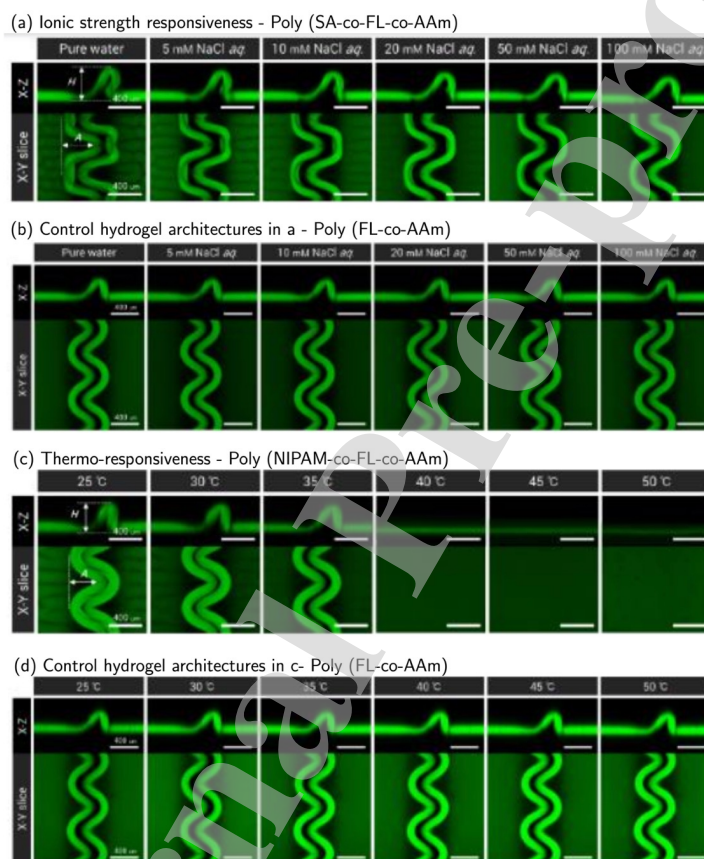


Figure 4: Dynamic control of the series TCBCs under large deformation via stimuli-responsive hydrogel films originally presented in Ref. [20].

286 are extremely small, together with those in the above-mentioned exercises, it is con-
 287 sidered small φ_0 value is one of the conditions for TCBs with large $\tilde{A}_y/\tilde{\lambda}$ to form. In
 288 addition, the determined G_c values for each group are consistent with each other and
 289 reasonable for the non-covalent interactions between the gel film and the glass substrate,
 290 which indicates a robust predictive capability for the developed Ω -formulae.

291 3.2. Discussions on TCB global morphology under small and large deformation

292 The global wavelength λ and transverse amplitude A_y for TCBs under small defor-
 293 mation are given by Eq. (4) and Eqs. (5) to (6), respectively. For the TCBs under
 294 large deformation, the global wavelength $\tilde{\lambda}$ and transverse amplitude \tilde{A}_y are given in the
 295 developed Eq. (7) and Eqs. (5) to (8). In contrast, the two local morphology parameters,
 296 *i.e.*, width $2R$ and height A_x are expressed in identical formulae. To probe into the con-
 297 ditions for large deformation to occur and its consequences the two global morphology
 298 parameters are further studied by comparisons between the small and large deformation
 299 scenarios.

300 The first comparison is made in Figure 5 showing the trends of wavelength-to-width
 301 ratio against the height-to-thickness ratio of TCBs. The morphology parameters are
 302 extracted from the TCBs in the hydrogel-film/glass-substrate systems used by Takahashi
 303 *et al.* [20, 21]; therefore, the Poisson's ratio $\nu = 0.5$ is used in Figure 5. For the same A_x/h
 304 and swelling-induced compressive stress σ_0 , it is obvious that $\tilde{\lambda}$ under large deformation
 305 given by Eq. (12) is larger than λ under small deformation given by Eq. (4). Along with
 306 the reduction of the film thickness, or equivalently the increase of A_x/h or Ω , the $\lambda/(2R)$
 307 ratio initially decreases to its minimum value $\lambda/(2R) = 1.71$ with $A_x/h = 5.46$ ($\Omega =$
 308 2.25), and then it increases to monotonically with respect to increases of A_x/h . However,
 309 the $\lambda/(2R)$ ratio under small deformation decreases monotonically over the range of
 310 A_x/h . This comparison suggests that one possible condition for large deformation to
 311 occur is the width $2R$ is small, that is, the TCB is narrow.

312 In the second comparison, the trends of transverse amplitude-to-wavelength ratio in
 313 terms of the parameter Ω are presented, as shown in Figure 6. Along with the increase
 314 of Ω , a narrow band of A_y/λ for the TCB under small deformation is observed, with
 315 the upper and lower limits as $A_y/\lambda = 0.1053$ ($\Omega \gg 1.5$) and $A_y/\lambda = 0.0930$ ($\Omega = 1.5$),
 316 respectively. However, for the TCB under large deformation, the $\tilde{A}_y/\tilde{\lambda}$ ratio monoton-
 317 ically increases from the starting value $\tilde{A}_y/\tilde{\lambda} = 0.1395$ with $\Omega = 1.5$. Therefore, it is
 318 reasonable to expect that a certain value of the ratio blister branching can occur to form
 319 web blisters which often have large transverse amplitude. Moreover, it is seen that the
 320 experimental data from Ref. [20, 21] fall on the predicted $\tilde{A}_y/\tilde{\lambda}$ line generated by Eqs.
 321 (5) to (8) nicely. Based on Figures 5 and 6, it is again concluded that the developed
 322 Ω -formulae under large deformation are able to provide good predictions of the global
 323 transverse amplitude \tilde{A}_y and wavelength $\tilde{\lambda}$ for the TCBs in soft hydrogel-based films.

324 3.3. Discussions on blistering mechanism for TCBs in soft hydrogel film

325 Takahashi *et al.* [20, 21] reported intriguing experimental observations of the TCBs
 326 created in the hydrogel-based film. Several points are worthy of discussion based on the
 327 developed Ω -formulae:

328 (1) It is experimentally discovered that the blister height increases with increasing
 329 the non-adhesive width. As shown by Eq. (2) the increase of blister height corresponds

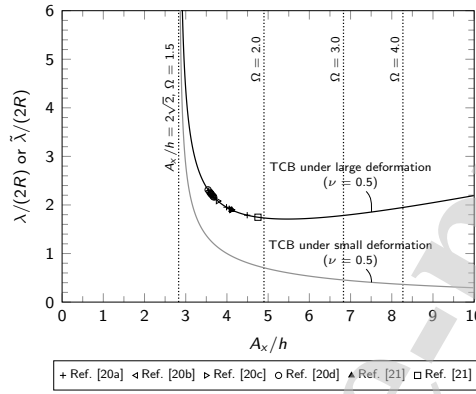


Figure 5: Comparison of wavelength-to-width ratio against height-to-thickness ratio for TCBs under small and large deformation, 'a-c' in the legend denote the four groups of specimens shown in Table 4.

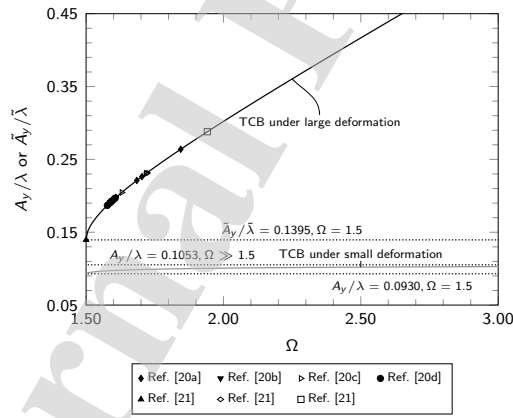


Figure 6: Comparison of transverse amplitude-to-wavelength ratio against the parameter Ω for TCBs under small and large deformation, 'a-c' in the legend denote the four groups of specimens shown in Table 4.

330 to the increase of parameter Ω , which is further inversely proportional to the interface
 331 adhesion toughness G_c . Before the hydrogel film bends away from the substrate, under
 332 the condition that the non-adhesive width is smaller than the critical buckling size, the
 333 subsequent blister growth and propagation are driven by the pocket of energy concentra-
 334 tion. The blister energy which includes the strain energy and G_c , is larger than the
 335 initial compressive strain energy due to swelling in the un-delaminated film. However,
 336 if the non-adhesive width is larger than the critical buckling value before bending out,
 337 buckling will occur and the swelling-induced compressive stress become the driving force,
 338 and G_c is not involved if no further interface delamination occurs [13,14].

(2) The blister height also decreases with increasing the cross-linking density, and
 TCBs were not observed for the cross-linking density values larger than 0.3 mol %.
 Based on the experimental measurements provided by Takahashi *et al.* [20], the decrease
 of cross-linking density leads the Young's modulus to decrease while the swelling ratio
 and the resultant thickness of swollen hydrogel film to increase. Substituting Eq. (16)
 into Eq. (3) results in

$$\Omega = \frac{2hE(1-\nu^2)}{9G_c} \left(\frac{1}{\Lambda^2} - \Lambda^4 \right)^2. \quad (17)$$

339 Then, by inserting the experimental measurements of Young's modulus and swelling
 340 ratio, the average interface adhesion toughness $G_c = 20.75 \text{ J/m}^2$ given from Table 4
 341 into Eqs. (2) and (17), the trend of blister height with respect to the cross-linking
 342 density is obtained as shown in Figure 7. It is observed that the blister height increases
 343 initially and decreases throughout the cross-linking density, which is in agreement with
 344 the experimental observations. Note that the points for the cross-linking density values
 345 larger than 0.3 mol % are not included as the corresponding values of Ω is less than 1.5
 346 that is not satisfied by Eq. (3), hence the developed Ω -formulae are not applicable, and
 347 no TCBs are expected to form with very small non-adhesive width. More importantly,
 348 the condition for the formation of TCBs, that is, $\Omega \geq 1.5$ can be used to determine the
 349 critical cross-linking density, and the associated critical swelling ratio of the gel-based
 350 material as given by Eq. (17). In contrast, the generation of TCBs with the cross-linking
 351 density larger than 0.3 mol % could be led by the large non-adhesive width up to 1000
 352 μm as reported Takahashi *et al.* [20], where TCBs are not driven by the pocket of energy
 353 concentration but by buckling.

354 (3) It is experimentally observed that the deformability of the hydrogel TCBs is
 355 increased with increasing the architecture height. This phenomenon can be easily inter-
 356 preted by Figure 6, where the deformability is represented by the ratios involved global
 357 morphology parameter that increases with increasing the value of Ω , or alternatively
 358 increasing the blister height as shown by Eq. (2).

359 (4) The eventual 3D architectures in equilibrium are in the similar shape if the ratios
 360 of the non-adhesive width and the initial thickness of hydrogel are similar. This exper-
 361 imental observation indicates the morphology parameters of TCBs in the hydrogel film
 362 are determined by the unique parameter Ω . As shown in Eq. (17), in spite of various
 363 initial thickness of hydrogel film and small non-adhesive width, the similar Ω values can
 364 still be obtained since it is determined by the Young's modulus, Poisson's ratio, thickness
 365 of swollen film, and interface adhesion toughness, which are all further related with the
 366 cross-linking density. The current work quantitatively correlates the swelling-induced
 367 3D morphological architecture with mechanical properties and compositions of hydrogel

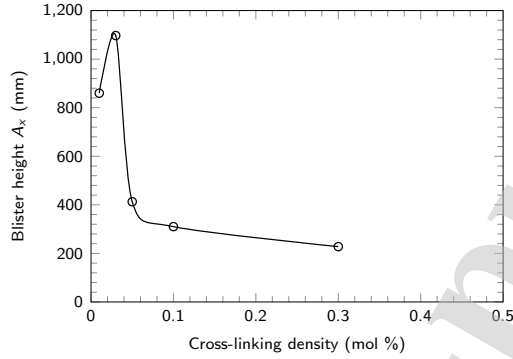


Figure 7: Trend of blister height with respect to cross-linking density using the experimental measurements presented in Ref. [20].

368 films. This will guide the development of alignment strategy of anisotropic soft additions
 369 for soft composites systems that exhibit inhomogeneous swelling. And complex shape-
 370 mode could be shifted and synthesised by basic self-bending, -rolling and -twisting, which
 371 is beneficial to the design of the microfluidic devices and hydrogel machines [28].

372 4. Conclusions

373 Based on a previously developed theoretical framework [18], the ‘ Ω -formulae’ are developed
 374 for the telephone cord blisters exhibiting large deformability created in a soft
 375 hydrogel-based thin film on a rigid substrate. And the theoretical methods as exper-
 376 imental guidance are proposed for the determination of the swelling-induced compressive
 377 stress in the un-delaminated film and the adhesion toughness at the interface. They
 378 give accurate predictions of the local half-width and height, and the global wavelength
 379 and transverse amplitude; and accurate predictions of the swelling-induced compressive
 380 stress that is very close to the value given by the Neo-Hookean model, and consistent
 381 value of interface adhesion toughness for the specific film/substrate materials systems.
 382 It is suggested that the morphology parameters of 3D architectures created in hydrogel-
 383 based films are dependent on the parameter Ω , and most importantly, $\Omega \geq 1.5$ can also
 384 be used as the critical conditions for the formation and development of telephone cord
 385 blisters with large deformability, which can be further correlated to the critical cross-
 386 linking density, swelling ratio, *etc.* For a range of applications in the fields of Tissue
 387 Engineering and Bioengineering, the theoretical understanding of the critical condition
 388 and post-instability surface evolution could facilitate the development of controllable sur-
 389 face patterns in soft materials. Furthermore, the current work opens the possibilities to
 390 design the microfluidic systems by controlling the hollow morphology parameters with
 391 high precision, such as modifying the hydrogel composition, swelling ratio, film thickness,
 392 and interfacial adhesion toughness.

393 **5. Data availability**

394 The authors confirm that the data supporting the findings of this study are available
395 within the article.

396 **6. Declaration of interests**

397 The authors declare that they have no known competing financial interests or personal
398 relationships that could have appeared to influence the work reported in this paper.

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Rachel Thomson: Supervision

Gary Critchlow: Supervision

David Rickerby: Supervision

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Simon Wang: Supervision, Conceptualization, Methodology, Writing - Reviewing and Editing

Declaration of interests

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

The authors declare the following financial interests/personal relationships which may be considered as potential competing interests:

none

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Swelling-induced telephone cord blisters in hydrogel films

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