Gas-Liquid Flow Regimes in Horizontal Annulus

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ABSTRACT

Gas-liquid flows in annulus channels are frequently encountered in the underbalanced drilling operation when the gasified drilling fluid is used. Accurate characterization of two-phase flow regimes in such conduits is critically important in order to gain a better understanding of the flow behaviours in the channels, thus to ensure a successful drilling operation achieved. In this paper experimental studies regarding gas-liquid flows in a concentric and fully eccentric horizontal annulus were reported. The test section setups of the flow loop have a length of 10.8 m, with outer and inner pipe diameters of 0.0768 m and 0.060 m respectively. Air and water at atmospheric pressure constituted the gas and liquid phases and the range of gas and liquid superficial velocities investigated during this study was 0.14 – 24 m/s and 0.15 – 2.78 m/s respectively. Flow regimes observed in both annulus setups by high speed camera imaging were dispersed bubble, elongated bubble, slug, wavy slug, churn, wavy annular and annular. A detailed description of the flow regimes with different features are presented together with high quality images. The local liquid holdup time series together with its probability density function (PDF) are used to gain more insights about the characteristics of the observed flow regimes. Effects of the annulus eccentricity on the observed flow regimes are also investigated. It is found that the annulus eccentricity affects the shape and structure of the elongated bubble, wavy annular and annular flow regimes. It is also observed that the annulus eccentricity causes the transition from elongated bubble to dispersed bubble to take place at higher liquid superficial velocities. It is also found that in the fully eccentric annulus causes transitions between different flow regimes to occur at higher liquid and lower gas superficial velocities when compared with that of concentric ones. An improved flow regime map is proposed based on gas and liquid Froude numbers by integrating the test results from this study with over 1000 data points found in literature.

Keywords: Concentric, Fully eccentric, Two-phase flow, Annulus, Horizontal, Experimental

1 Introduction

Multiphase flow modelling relies on determination of the topology or distribution of the phases and the interface geometry which are not usually known beforehand. The accurate determination of the flow regimes in conduits is one of the major challenges facing two-phase flow modelling. Design parameters including pressure drop and heat transfer etc. depend on the flow phase distribution in conduits and without a knowledge of the flow regimes, these parameters would not be computed accurately (Yadigaroglu, et al., 2018).

Industrial operations abound in the chemical, nuclear and petroleum industries where the two-phase flow of gas and liquid is observed in annuli. Operations such as off-normal boiling of subcooled liquid coolants in the nuclear industry, double pipe heat exchangers for evaporation and condensation in the chemical industry as well as underbalanced drilling, well clean up and production in the petroleum industry are typical examples. For exploiting offshore marginal fields underbalanced drilling techniques are particularly important. During the underbalanced drilling operations, gas-liquid flow in vertical, inclined and horizontal annuli can be encountered. The annulus eccentricity could also be changing during these operations. Due to the importance of the two phase flow in annuli, many studies have been carried out for a few of decades in order to gain the knowledge regarding the flow behaviours in such channels. It was noted that as early as in 1980’s, experimental studies on effect of flow obstruction geometry on pressure drop in horizontal air-water flow was undertaken by Salcudean et al. (1983). A pipe of 0.0254 m diameter having obstructions located centrally and peripherally. The influence of the degree of flow blockage and shape of flow obstructions on pressure drop was examined. No flow regimes were specified during their study.

Later Osmansali & Chang (1988) studied air-water two-phase flow regime transitions in horizontal annuli formed by placing central rods having different diameters concentrically in an acrylic tube of 0.0508 m. The inner to outer diameter ratios (Di/Do) studied in the work were 0.375, 0.5 and 0.675 (with hydraulic diameters Dh = 0.0318, 0.0254 and 0.0191 m, respectively) where Dh is hydraulic diameter. Flow regimes identified included stratified-smooth, stratified wavy, slug and annular.

Lage et al.,(2000) undertook small scale experimental and theoretical studies of two-phase flow in horizontal and slightly deviated fully eccentric annuli. The annulus setup was 50 m long, having outer (Do) and inner (Di) diameters of 0.1016 and 0.0508 m respectively. Test fluids utilized were air-water and diesel-nitrogen mixtures. Flow regimes identified include dispersed bubble, stratified, intermittent and annular flows. However, their data points were too few and could not produce a complete view of flow regime maps.

For their part, Ekberg et al.,(1999) studied flow regimes in narrow horizontal annuli. Experiments were conducted in two different annuli with Do and Di of 0.00863 & 0.0066 m for the first annulus and 0.0352 & 0.03315 m for annulus two. Flow regimes observed were classified by the researchers as slug, slug, dispersed bubble, churn as well as other hybrid regimes. The annulus setups were small and not likely to be encountered in the oil and gas industry.

Zhou et al., (2004) performed extensive air-water experiments in a large scale annulus with Do of 0.2124 m and Di of 0.089 m. Observed flow regimes included stratified smooth, stratified wavy, slug, stratified to slug, slug to dispersed bubble and slug to annular. They also developed theoretical basis for flow regime transitions.

Omrulu, Metin and co-workers (Omrulu et al., 2006; Metin & Ozbayoglu, 2007) studied extensively two-phase flow through fully eccentric horizontal annulus. Their experimental setups consisted of different (Do) 0.0932, 0.1143 m and (Di) 0.0488 and 0.05715 m. Flow regime identification was by visual means and limitations in their setup meant that mainly the intermittent flow regime was observed during their study. They proposed a mechanistic model based on representative diameter for flow regime determination in fully eccentric annulus.

Mendes et al., (2011) studied flow regimes in inclined gas-liquid flow in annular ducts. The annulus geometry made from borosilicate glass had a length of 10.5 m and Do 0.111 m and Di 0.075 m. Air-water flow regimes observed stratified smooth, stratified wavy, slug, slug, churn, bubble and dispersed bubble.

Later on, Osgouei and others (Osgouei & Ozbayoglu, 2010; Osgouei et al., 2012; 2013) presented studies on two-phase flow in a horizontal annulus having an eccentricity of 0.623. They presented flow regime determination techniques based on diagugradicant discriminant analysis and suggested in a separate paper flow regime identification based on Artificial Neural Networks.

Gschwindner, (2013) undertook experimental studies in a concentric annulus with Do of 0.0515 m and Di of 0.0333. Air and water were the test fluids and flow regime identification was...
achieved using video camera recordings. Observed flow regimes were limited to intermittent and bubble flow due to the small range of liquid and gas superficial velocities investigated.

Recently, Nossen et al. (2017) conducted an experimental study of two-phase flow in horizontal and inclined annuli. The annulus test section was concentric, having outer and inner diameters of 0.1016 and 0.0508 m respectively. Test fluids used were SF6 gas – water and SF6 gas – Exxsol D60 oil. Flow regimes observed during their studies were Slugs, large waves, very low frequency slugs and transitional as a very limited range of gas and liquid superficial velocities were investigated.

In summary, a review of related literature points to the fact that the flow structure in the annulus setup is different from those observed in circular pipes due to flow obstruction by the central pipe. As a result, the characteristics of the flow regimes are different. There is a lack of detailed information on the flow regimes encountered in horizontal annuli, as most studies undertaken to characterize flow regimes were based on visual observation, which proved challenging due to the obstruction and deformation in vision caused by the unique geometries of the flow channel. Also, in spite of the fact that in some applications e.g. underbalanced drilling operations, annulus eccentricity is an issue for horizontal two-phase flow regimes and their transitions. However, based on available literature, not much attention has been paid to this although most issues relating to vertical annuli have mainly been resolved.

To address these issues, this study presents detailed systematic experimental studies which have been conducted in fairly large (a) horizontal concentric and (b) fully eccentric annuli to characterize flow regimes and their transitions. High speed camera images and ring-type conductance probes designed for this study have been utilized to examine the flow regime features in horizontal annuli.

2. Experiments

2.1 Experimental Setup

The experimental study have been carried out in the Process Systems Engineering laboratory of the Cranfield University. A simplified schematic diagram of the flow loop is as shown in Fig. 1(a). Air and water were the testing fluids with the air supplied to the flow loop using a screw compressor by AtlasCopco® model GA55 with a maximum discharge pressure of 7.5 barg and free air maximum delivery capacity of 638 m³/hr. Two automated valves (namely VC301 & VC302) are used in regulating the air flow rate while measurement is undertaken by one of two Rosemount Mass Probar flow meters (FT302 and FT305) with accuracy of ±1.4%. Air flow rates ranging between 0 – 150 Sm³/hr are measured by FT302 while flow rates above 150Sm³/hr are measured by FT305. Water flow to the flow loop is provided from a water tank with a capacity of 2 m³ using a progressive cavity pump with maximum discharge pressure of 6 barg. The water flow is measured using an Endress & Hauser Promag 50 electromagnetic flow meter ranging between 0 – 18 m³/hr, having an accuracy of ±0.5%. A 2 m long stainless steel section preceding the annulus test section is allowed for mixing of both phases before it enters the annulus test section where a development length of 1 m is allowed before the first instrument is placed, and then flows through the entire annulus section. The fluid mixture exit the annulus test section into a section of circular pipe before emptying into the water tank which is open to the atmosphere, where gas-liquid separation takes place.

The annulus test section is formed using two Polyvinyl Chloride (PVC) pipes with outer pipe diameter (Do) is 0.0768 m and inner pipe diameter (Di) is 0.060 m creating a hydraulic diameter of 0.0168 m. it is 10.8 m in length and the flow observation and measurement sections are placed 6.01 m away from the point where the fluid mixture enters the annulus which gives a length of 357 pipe diameters. Two GE Druck static pressure transducers model PMP 1400, and a WIKA model A-10 static pressure transducer ranging between 0-6 barg and accuracy of ±0.25% of full scale are used to obtain the static pressure in the test section. The fluid mixture temperature is measured by a J-type thermocouple with accuracy of ±2.5°C. The eccentricity of the annulus is adjusted using 4 mm stainless steel pins fed through an eccentricity adjuster fabricated from PVC rods by moving the pins in or out depending on the eccentricity desired as depicted in Fig. 1(b). The pins are small enough to ensure that they don’t interfere with the two-phase flow that goes through them. Liquid holdup measurement is done using two pairs of conductance probes designed for this study and this 430 mm long section made from perspex glass also serves as the imaging window.

The two pairs of ring-type conductance probes used for measuring the area-averaged liquid holdup were designed based on the recommendation of Fossa (1998) and flush mounted on the outer pipe of the annulus test section. The probes are designed such that the ratio of the electrode spacing De to the pipe diameter D is 0.34 resulting in electrode spacing of 26 mm. Two pairs of electrode were used each having a width of 6 mm and distance of 270 mm between each electrode pair. A desktop computer using a LabView® based system consisting of National Instruments (NI) connector board interface and connected to the instrumentation using coaxial cables is used for data acquisition. Flow regime images are captured using an OLYMPUS model i-SPEED 3 high speed camera at 1000 frames per second and adequate lighting is provided using Arrilite 800-W lights.
2.2 Experimental Procedure

2.2.1 Conductance Probes

The conductance probes employed for this study operate based on the principle that the two-phases employed as testing fluids have different electrical conductivities. Therefore the electrical impedance between two electrodes immersed in a multiphase fluid mixture is determined by the conductance and permittivity of these individual phases, the fraction of the phases, the flow regime observed and the configuration of the sensor. Calibration of the ring-type conductance probes was carried out offline based on the recommendations of Fan & Yan (2014) for stratified flow in concentric and fully eccentric annulus setups. Known volumes of liquid (water) were introduced into each annulus setup and the corresponding voltages were recorded. A high-level voltage output of 5 V was obtained when the annulus section was completely filled with water and a low-level voltage output of 0 V was observed when the annulus was empty (filled with air). The voltage output from each pair of conductance probe was normalized using maximum voltage value when the annulus was filled with water for each annulus setup, this produced a dimensionless value. A non-linear relationship was obtained between the liquid holdup and the voltages for each annulus setup and during experimental runs, the obtained voltages are plugged into the developed calibration curves and the liquid holdup was determined as such. The uncertainty of the conductance probe measurements are found to be within ±2% of indirect measurements.

2.2.2 Experimental Scheme

The annulus section eccentricity is adjusted as appropriate using the 4 mm stainless steel pins earlier described. During this study, two eccentric positions were investigated: (i) concentric and (ii) fully eccentric annulus setups. Figure 2 shows the visualization of the flow regimes observed in concentric and fully eccentric annulus setups with subtle differences. Similar flow regimes were identified in both annulus setups with subtle differences in some cases. The flow regimes identified include dispersed bubble, elongated bubble, slug, wavy slug (classified for this study), churn, wavy annular and annular flow regimes. Limitations in the experimental setup means the stratified flow regime was not encountered.

For the presentation of flow regimes in forthcoming figures, the superficial gas velocities in the annulus were computed based on the measured pressure and temperature of the test section, the centre of which the flow regimes were also photographed as follows:

\[ V_{SB} \left( \frac{m}{s} \right) = \frac{P_G Q_G T_M}{P_M T_C A} \tag{1} \]

Where \( P_G \) and \( T_C \) are the initial pressure and temperature of the gas phase (101325 Pa and 15°C) respectively, \( Q_G \) is the volumetric flowrate in (Sm\(^3\)/s), \( T_M \) and \( P_M \) are the temperature and pressure of the two-phase mixture measured at the test section and \( A \) is the cross-sectional area of the annulus.

Typical photographic representations of the flow regimes obtained are presented in Figure 3 and a brief description of each regime is presented below:

3.1.1 Dispersed Bubble Flow: The dispersed bubble flow regime is observed at high liquid and low gas superficial velocities. Tiny gas bubbles are dispersed in a continuous liquid phase concentrated initial close to the top of the annulus cross section. The mechanism for the formation of this flow regime is the breakdown of gas plugs during the elongated bubble or slug flow regimes. Increasing the liquid superficial velocity results in a more even distribution of gas bubbles in the annulus section.

3.1.2 Elongated Bubble Flow: Also known as the limiting case of slug flow. It is encountered at very low gas and liquid superficial velocities. Characterized by alternating liquid body which fills the entire annulus cross section and gas plugs trapped at the top of the annulus. The shape of the gas plug observed...
depends on the annulus eccentricity under study. No gas bubbles are entrained in the liquid body.

3.1.3 Slug Flow: This flow regime is similar to elongated bubble but occurs at higher gas superficial velocities. Initially preceded by a stratified smooth or wavy interface depending on the superficial gas velocity. The stratified system is followed by faster and shorter moving liquid body with higher energy intensity than those observed in elongated bubble flow. The liquid body wraps itself around the inner pipe of the annulus and contains some entrained gas bubbles flowing close to the top or centre of the annulus, due to a decrease in flow liquid holdup and increased turbulence.

3.1.4 Wavy Slug Flow: This flow regime was classified as such for this study and is similar to what was observed by Nossen et al. (Nossen et al., 2017) and classified as large wave flow. It is characterized by a long liquid film region during wave development, followed by a small liquid body which briefly bridges the top of the annulus, after which it seems to lose energy and is pushed away by a following wave. Some gas bubbles are entrained in the small liquid body at higher liquid superficial velocities. It has some of the features of slug flow but possesses its own unique feature to be classified as a flow regime.

3.1.5 Churn Flow: The churn flow regime is similar to the slug flow regime but is characterized by a chaotic liquid phase containing a large amount of entrained bubbles travelling with an oscillatory motion. No clear boundaries can be observed for both phases. The mechanism of this regime is an increase in the gas void fraction resulting in the breakdown of the continuous nature of the liquid body that follows each successive Taylor bubble. This causes a collapse of the slug which falls back and is mingled with the one following. It has been confirmed in the past from experimental studies that the churn flow regime could not exist in horizontal or shallow inclined two-phase flow. In vertical upwards flows people use “churn flow” to describe an intermediate region between slug and annular flows in the flow regime map (Hewitt and Jayanti, 1993). Similar to this, churn flow observed in the annulus also sits between the slug and annular flow regimes.

3.1.6 Wavy Annular Flow: Occurring at low liquid and high gas superficial velocities, this flow regime is characterized by a continuous gas core with some entrained liquid in the annulus centre, a thin liquid film at the top of the annulus and a thicker film at the bottom with a wavy interface. The annulus eccentricity affects the observed film level and interface.

3.1.7 Annular Flow: At higher gas superficial velocities than for wavy annular flow the annular flow regime is encountered. A smooth liquid film is observed at the top and bottom of the annulus. The film at the bottom is thinner when compared with those of the wavy annular flow.
Further characterization of the flow regimes in horizontal concentric annuli is undertaken using a combination of time series and Probability Density Function (PDF) plots of liquid holdup obtained from conductance probes. Conductance probe techniques have been employed in the past by researchers including Barnea et al. (1980), Kelessidis & Dukler (1989) and Das et al. (1999) for flow regime classification. The raw voltage values obtained from conductance probes are converted to instantaneous liquid holdup by using obtained calibration curves for each annulus setup studied and plotted on a time series plot. Further statistical analysis of the liquid holdup plots were conducted to clearly identify each flow regime observed during gas-liquid flow in horizontal annuli and compared with visually observed flow regimes. Representative time varying liquid holdup and PDF plots are presented in Fig. 4 for horizontal concentric annulus.
For the dispersed bubble flow regime, a steady uniform oscillation of the time varying liquid holdup around a value of 1 gives an indication of the presence of spherical bubbles dispersed in a continuous liquid phase. The PDF plot is unimodal having its peak value at holdup value 0.97.

During the elongated bubble flow regime, the time varying liquid holdup plot is observed to fluctuate intermittently from a crest value of 0.7 to a crest value of 1. The higher crest value corresponds to full liquid filling the annulus section between the ring electrodes while the lower crest value indicates the passage of the elongated gas bubble through parts of the probe. The PDF feature of this flow regime indicates two peaks close to each other at high liquid holdup values.

Pulsating probe traces are observed for the slug flow regime, which indicates how the slug liquid body and Taylor bubbles alternate in the annulus section between the ring electrodes. A bimodal PDF trend is observed with two very distinct peaks. One peak exists within liquid holdup range between 0.30 – 0.50, while the second peak exists between ranges of 0.7 – 1.0.

The nature of the wavy slug is seen by the width and amplitude of the time varying liquid holdup plot at low holdup values. Small waves are represented by the zig zag spikes at low holdup values, while a peak value at higher holdup values signifies a small liquid body that just touches the annulus top. The PDF trend for this regime is unimodal in nature with its peak at low liquid holdup values, with the second peak observed in slug flow at higher liquid holdup values disappearing.

Churn flow is characterized by its rowdy nature and this is evident in the time varying liquid holdup plots, where random peaks and troughs are observed. The observed PDF trend is unimodal with peak at low holdup values similar to what was observed in wavy slug flow. However, the area under the curve is large cutting across a wide liquid holdup range. Also low but non-zero PDF values are observed at liquid holdup values up to 0.8.

Wavy annular flow shows a probe trend which reflects the effect of unstable aerated waves passing through it, with most of the liquid flowing at the bottom of the annulus as a film. A unimodal PDF plot located at low holdup values with peak value averagely around 0.25. It is distinguishable from the annular flow regime by its larger area under the curve and low PDF value.

Finally, small spikes are observed consistently about low holdup values during the annular flow regime when time varying instantaneous liquid holdup values are plotted. These spikes indicate a wavy interface and the film thickness is proportional to the mean liquid holdup value. A single PDF peak is obtained at low holdup values near 0. It has a smaller area under the curve when compared with the wavy annular flow regime but a higher PDF value.

These classifications are used in conjunction with high speed camera images to classify flow regimes accurately in horizontal annuli.

### 3.3 Effect of Annulus Eccentricity on Flow Regimes

As stated earlier, two different annulus setups were used for the experimental investigations presented in this study: (a) the concentric annulus and (b) the fully eccentric annulus. The fully eccentric annulus has the inner pipe in its configuration lying at the bottom of the outer pipe forming a geometry shaped like a half moon which is different from the concentric annulus geometry. A scenario where the annulus eccentricity may be changing can be encountered during underbalanced drilling with drill pipe (inner pipe) rotation as the well is being drilled. The annulus inner structure affects the distribution of phases and as such may influence some of the flow regimes observed.

At the low gas and lowest liquid superficial velocities (0.21 m/s and 0.15 m/s respectively) investigated during this study, the elongated bubble flow is observed in the concentric annulus while the slug flow regime is observed in the fully eccentric annulus. A larger flow area is available at the top of the annulus for the gas phase to occupy in the fully eccentric annulus when compared with a small annulus gap in the concentric annulus. Therefore at this low gas flow rate, the gas phase in the eccentric annulus has sufficient contact area and energy to sweep the liquid phase to bridge the annulus wall intermittently forming slug flow while the gas phase is trapped as an elongated gas bubble in the small concentric annulus gas at the top of the annulus because of...
small gas flow area and low energy. Fig 5(a) and (b) show the high speed image and PDF trends for this flow condition in horizontal concentric annulus respectively while (c) and (d) show those for the fully eccentric annulus.

Figure 5: Effect of annulus eccentricity on flow regimes (Vsl= 0.15 m/s; Vsg = 0.21 m/s) (a) Elongated bubble flow in concentric annulus (b) Elongated bubble flow PDF trend in concentric annulus (c) Slug flow in fully eccentric annulus (d) PDF trend for Slug flow in fully eccentric annulus.

The bubble shape observed in the elongated flow regime is also affected by the annulus eccentricity. Fig. 6(a) shows the bubble shape observed in the concentric annulus. It is shaped as a flatworm and is shorter in length when compared with the bubble shape in Fig 6(c) which is the bubble shape in fully eccentric annulus. The PDF trends for both annulus are shown in Fig. 6(b) and (d) for concentric and fully eccentric annulus respectively. The effect of the bubble shape is captured in this trend where for the concentric annulus, the tiny bubble shape and length is reflected in the observed peaks at high liquid holdup values. On the other hand, the PDF trend for the elongated bubble flow regime in fully eccentric annulus captures the large bubble length and size which is reflected in the observed peaks high and lower liquid holdup values. Also, the highest peak in the concentric annulus has a higher PDF value when compared with that of the fully eccentric annulus. Generally, the slug flow region is largely unaffected by the annulus eccentricity and is the dominant flow regime in both annulus setups.

Figure 6: Typical elongated bubble flow (Vsl =0.83 m/s; Vsg = 0.21 m/s) (a) concentric annulus (b) PDF trend for concentric annulus (c) fully eccentric annulus (d) PDF trend for fully eccentric annulus.

The liquid film height observed in the wavy annular and annular flow regimes are also affected by annulus eccentricity. In Fig 7, typical annular flow regime images are presented for both the concentric annulus and the fully eccentric annulus. Fig 7(a) shows representative liquid film height in the concentric annulus during annular flow while Fig. 7(c) shows that for a fully eccentric annulus. A higher liquid film height is observed in the fully eccentric annulus when compared with the concentric annulus. This is because of the impact of the flow geometry in the fully eccentric annulus. The inner pipe restricts the flow of the liquid phase at the bottom of the annulus resulting in a higher liquid film. This is captured by the PDF trends presented in Fig 7(b) and (d) for concentric and fully eccentric annulus respectively. A similar scenario is observed for the wavy annular flow regime. It is envisaged that the variation of the flow channel geometry due to eccentricity would affect phase separation of the flow, i.e. the larger the eccentricity, the easier the gas/liquid
separation. This in the end would influence the flow regimes formed.

Figure 7: Typical annular flow regime (Vsl = 0.15 m/s; Vsg = 16.29 m/s) in (a) concentric annulus, (b) PDF trend for concentric annulus (c) fully eccentric annulus (d) PDF trend for fully eccentric annulus

3.4 Flow Regime Maps

3.4.1 Experimental Flow Regime Maps

Flow regime maps were developed from experimentally observed flow regimes for both annulus setup investigated for this study. The coordinates were the superficial liquid and gas velocities as ordinate and abscissa respectively. The effect of annulus eccentricity on observed flow regime transitions was also studied. As depicted in Fig. 8(a), at the lowest liquid and gas superficial velocities investigated in the concentric annulus, the elongated bubble flow is first encountered, Fig. 8(b) on the other hand shows at in the fully eccentric annulus at the same conditions, the slug flow regime is encountered. The slug flow regime is the predominant flow regime in both annulus setup. Similarly, the effect of annulus eccentricity on experimental flow regime transition are presented in Fig.9. The flow regime transitions were drawn arbitrarily and comparisons were made by superimposing both flow regime transitions on one map. It can be observed in Fig. 9 that the transition to elongated bubble and dispersed bubble flows in the fully eccentric annulus, take place at Vsl of 0.22 m/s and 1.56 m/s respectively, which is higher than that at which the transition takes place in the concentric annulus (Vsl = 0.10 m/s and 0.99 m/s respectively). This is due to the geometry effect and the distribution of the phases in both annulus setups. More area for gas phase to occupy in the fully eccentric annulus means that the elongated bubble flow regime will occur at higher liquid superficial velocities. For this same reason, higher liquid flow rates are required to breakdown to large gas plugs in this setup when compared with the concentric one. Generally speaking, the transitions from elongated bubble to slug, slug to wavy slug and wavy slug to annular flow regimes occur at lower gas superficial velocities in the fully eccentric annulus when compared with the concentric one. This shift appears to be consistent with the observed effect of eccentricity on phase separation.

Figure 8: Experimental flow regime map for (a) concentric annulus; (b) fully eccentric annulus
and troughs in the holdup time series plots. On the other hand, the PDFs show a more dominant second peak at higher holdup values at higher Vsl values with the peak at lower holdup values gradually diminishing in value.

During two-phase flow at Vsg of 16.29 m/s, increasing Vsl from 0.27 to 1.94 m/s showed the effect of increasing liquid flowrates in the annular flow region. The short spikes noticed at the lowest Vsl gradually become more frequent and occur at higher holdup values as observed on the holdup time series plot. This gives an indication of the increased wavy interface of the liquid film at the bottom of the annulus. With regards to the PDF trend, the area under the PDF curve increases with increase in Vsl and shift the single observed peak from near enough zero to higher holdup value up to 0.28. At Vsl of 1.94 m/s, the flow transitions to wavy annular flow is due to reduced energy of the gas phase.

Due to constraints in space, all the observable flow regime transitions are not presented in this article but it is worth mentioning that at other gas and liquid superficial velocities investigated during this study, transition to wavy slug and churn flow regimes were also encountered and the effect of flowrate increases affected the observed holdup time series and PDF trends for these regimes.

### 3.4.3 Comparison of Flow Regime Maps

The experimentally developed flow regime map in horizontal concentric annulus is compared with the flow regime map proposed by Osgouei et al.,(2010) for flow through horizontal concentric annulus as presented in Fig. 11. It can be observed the flow regime transitions from literature developed by Osgouei et al.,(2010) is unable to predict the slug, churn and annular flow regimes accurately. The wavy annular flow regime is the only regime predicted fairly accurately by the map.
Figure 10: Effect of gas and liquid superficial velocities on Time series and PDF trends in horizontal concentric annulus
3.5 Development of Flow Transition Parameters

The differences observed in the compared flow regime maps, as well as lack of studies which accurately characterize flow regimes and their transitions in horizontal annulus, shows the need to develop flow regime transition parameters. Exactly 1174 experimental data points integrated from literature and experiments are harnessed to develop this model. Data was obtained from studies by Sunthankar et al.,(2000), Zhou et al.,(2004), Omurlu et al.,(2006), Ozbayoglu & Omurlu (2007), Osgouei et al.,(2010), Mendes et al.,(2011), Gschaidner (2013), Nossen et al.,(2017) and integrated with experimental data from the fully eccentric annulus setup. The developed flow regime transitions in this study is based on different annulus eccentricities, hydraulic diameters, fluid properties as well as gas and liquid superficial velocity ranges. Most of the data is assumed to have been collected under ambient temperature and pressure as operating conditions were not reported in the studies.

A flow regime map is proposed based on modified gas and liquid Froude numbers

\[ Fr_L \geq -0.078 \ln Fr_G + 0.129; \quad Fr_G \leq 0.025 \]  

\[ Fr_L \geq -0.0247 \ln Fr_G - 0.2; \quad Fr_G < 0.04 \]  

\[ Fr_L \geq 4.115e^{19.4Fr_G} and \quad Fr_G < 0.04 \]  

\[ Fr_L \geq -122.9Fr_G^2 - 12.28Fr_G + 10.7 and \quad Fr_G > 0.04 \]

The flow chart shown in Fig. 13, illustrated in the flow chart shown in Fig. 13.

Presented in Fig. 12 is the flow regime map developed from this study, which can be employed for both horizontal and eccentric annulus geometries. Flow regimes can be determined step by step based on the liquid and gas Froude numbers as illustrated in the chart shown in Fig. 13.

The developed parameters were tested against 109 data points from the concentric annulus of this study, predicting the flow regimes with an accuracy of 90%, 81% and 85% respectively for the Bubble, Intermittent and Annular flow regimes respectively.

The breakdown of the performance of transition parameters on
Figure 13: Flow chart for flow regime identification in horizontal annuli.

Flow Regime: Bubble flow

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<th>FrL ≤ -0.247lnFrG - 0.2</th>
<th>FrG &lt; 0.15</th>
<th>0.15 ≤ FrG &lt; 2.78</th>
<th>FrG ≥ 2.78</th>
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Table 1: Performance of transition parameters on test data set.

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4 Conclusion

The developed flow regime transition parameters are applicable to any two-phase flow system in horizontal annuli. The parameters were successfully predicted by the neural network model built for the conductance measurement in horizontal pipe.


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