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**Algorithm 1:** 2D ingot evaporation model - Ingot definition

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%% Request user input parameters;
Request  $t_p$  = time required for e-beam to draw a pattern & time step used in time discretization;
Request;
for  $i \in Oxidelist$  do
|  $X_i$  = mass fraction for oxide i (in wt%)
end
Request  $N$  = number of points used to discretize the target height;
Request  $M$  = number of points used to discretize the target width-wise;
Request  $t_{dep}$  = deposition time;
%% Initialize target matrices and physical parameters for constituent oxides;
Given  $n$  = number of oxides in oxide list;
Given  $N_A$  = the Avogadro Number;
Given  $k_B$  = the Boltzmann constant;
Given  $D_t$  = Target diameter;
Given  $H_t$  = Target height;
Given  $T(y)$  = Temperature distribution on ingot surface;
/* Define dimensions of finite elements */
 $\delta_X = H_t/N$  ;
 $\delta_Y = D_t/M$  ;
for  $i \in Oxidelist$  do
| /* Define physical properties of the oxides */
|  $\rho_i$  = oxide density of oxide i;
|  $Mmol_i$  = molar mass of oxide i;
|  $V_{P_i}(T)$  = Vapour pressure as a function of temperature ;
| /* Calculate volume fraction of the oxide */
|  $V_i = \frac{X_i}{\rho_i} \frac{1}{\sum_{i=1}^n \frac{X_i}{\rho_i}}$ ;
| /* Calculate number of molecules per finite element */
|  $N_{M_i} = N_A \rho_i \delta_X \delta_Y^2 X_i / Mmol_i$ ;
| /* Initialize target matrix for each oxide */
|  $TM_i = N_{M_i} * J[N, M]$ , where  $J[N, M]$  is an all-ones matrix of dimensions N, M;
end
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**Algorithm 2:** 2D ingot evaporation model - Evaporation loop

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%% Calculate the evaporation rate distribution on the surface for each oxide;
for  $i \in Oxidelist$  do
    for  $y \in M$  do
         $\delta_{m_i}[y] = \sqrt{\frac{Mmol_i}{2\pi k_B T(y)}} V_{P_i}(T(y))$ ; where  $\delta_{m_i}$  is a vector of dimension M representing the
        molecules evaporated for oxide i from the ingot surface;
    end
end
end
%% Calculate the evaporation in the specified time;
while  $t \leq t_{dep}$  do
    for  $i \in Oxidelist$  do
        while  $y \leq M$  do
            while  $x \leq N$  do
                if  $TM_i[x, y] > 0$  then
                     $TM_i[x, y] = TM_i[x, y] - \delta_{m_i}[y]$ ;
                    if  $TM_i[x, y] \geq 0$  then
                         $y = y + 1$ ;
                    else if  $TM_i[x, y] < 0$  then
                         $TM_i[x + 1, y] = TM_i[x + 1, y] - TM_i[x, y]$ ;
                         $y = y + 1$ ;
                    end
                else if  $TM_i[x, y] \leq 0$  then
                     $x = x + 1$ ;
                end
            end
            Break;
        end
        Break
    end
end
 $x = 0$ ;
 $y = 0$ ;
 $t = t + t_p$ ;
end
```

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