Design Issues of an IPM Motor for EPS

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Abstract: In electric power steering (EPS), permanent magnet (PM) brushless ac (BLAC) motors offer distinct advantages over other electric motor types in terms of torque smoothness, reliability and efficiency. The design procedure of an interior permanent magnet (IPM) motor used in EPS is presented in this paper. The requirements of the steering system are first introduced, and the machine’s specifications are then derived. Critical issues which have considerable impacts on the machine’s performance, such as operation mode, rotor structure and slot/pole combination, are analyzed. Subsequently, a 12-slot/10-pole sinusoidally excited IPM machine with concentrated windings is proposed and optimized based on finite element analysis (FEA) modelling. The losses and efficiency are then computed. Performance predictions from the FEA results confirm all the requirements are met or exceeded. A prototype motor has been built for validation.

Keywords: Electric power steering, interior permanent magnet, motor design, finite element analysis.

1. Introduction

Global warming is becoming a very important global issue. It was even one of the three main topics in the recent 2009 G8 Summit. Carbon dioxide (CO\textsubscript{2}) emission is the main contributor of green house gas which leads to global warming. Transportation accounts for more than 20\% of man-made CO\textsubscript{2} [1]. It is therefore highly desirable to reduce green house gas emission by improving vehicles’ fuel efficiency. On the other hand, the number of electric machines installed in modern vehicles has been increasing at a rapid pace. The more luxury the vehicle, the more electric machines will be equipped. Well optimised electric machines with high efficiency will therefore play a pivotal role in improving the vehicles’ overall efficiency, and thus in reducing the CO\textsubscript{2} emission to mitigate global warming.

An apparent trend that electrical power steering (EPS) is becoming an alternative to the hydraulic power steering (HPS) can be seen in recent developments in automotive industry. In the HPS system, a pump driven by the engine is constantly running to keep the hydraulic pressure, no matter assistance is required or not. While in the EPS system, the electric motor is driven only when the steering wheel is turned. EPS thus offers much better fuel economy, which can account for 3\% improvements in fuel efficiency [2]. Electric machines, the key actuators in the EPS system, are crucial in influencing the vehicle’s steering performance. A brushed DC motor was equipped in the world’s first EPS system in 1993 by Honda, on Acura NSX [3]. Presence of brushes limits its performance especially at higher speeds, and the sparks may cause safety and electromagnetic interference (EMI) problem. A much more competitive solution based on permanent magnet (PM) brushless machines has drawn considerable interests from both industrial and academic research communities. The high torque/volume ratio, high dynamics, high speed due to field-weakening capability and absence of brushes, simple machine structure and high efficiency are some of the advantages of PM machines. For the disadvantages, the magnets will subject to the risk of irreversible demagnetization in overloading or high temperature conditions. Various PM machine topologies have been developed for EPS applications. Research have been focusing on some particular aspects, such as cogging torque reduction and torque ripple minimization [4]-[8], saturation effect [9]-[11], losses [12] [13], and fault tolerance [3] [14] [15]. Whereas most studies principally focus on the electromagnetic design level on the size and shape of the magnets of the machine, it appears that few studies emphasize on machine topology selection level prior to detailed machine electromagnetic design. For a complete EPS system design procedure, it is strongly felt that essential issues for machine
characteristics, including machine topology, operation mode, and slot/pole combination, should be firstly decided.

This paper concerns the design of a PM machine for EPS applications. The requirements of the EPS application are introduced and the specifications of the desired machine are then derived. Before detailed design, some critical issues which essentially affect the final performance, viz., operation mode of either brushless alternating current (BLAC) or brushless direct current (BLDC), rotor structure of either surface-mounted permanent magnet (SPM) or IPM, as well as slot/pole combination, are analyzed in details. Subsequently, a 12-slot/10-pole sinusoidally excited IPM machine with concentrated windings is optimally designed and verified with finite element analysis (FEA). A prototype has been built for validation.

2. Application requirements and design specifications

A. Application overall requirements

EPS is an important subsystem on vehicles, which works extremely frequently during driving. In such a safety critical application, high reliability must be fully considered during the whole design process. Besides, in terms of limited available space and the demanding working environments, the desired electric machine is to have following features: compact size, low weight, low cost, variable speed over wide torque-speed areas, low acoustic and electromagnetic noise, high efficiency, as well as smooth torque output for the precision steering and driving comfort.

B. Design specifications

For small and middle sized vehicles, the electric machine is mounted on the pinion steering gear or on the steering column. Assistant torque is applied to the steering column via a worm-gear. Therefore, the electric machine can run at relatively higher speed. About 6–8 kN column force is required in this EPS system, which corresponds to 7 Nm torque demand for electric machine [16] [17]. The specifications for the desired electric machine under study, which is to be used in a column-type EPS, are summarized in Table I. The required torque-speed curve is shown in Figure 1.

Table I: Specifications of desired electric machine for EPS application.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Specification</th>
</tr>
</thead>
<tbody>
<tr>
<td>DC-bus voltage</td>
<td>42 V</td>
</tr>
<tr>
<td>Stall torque</td>
<td>7 Nm</td>
</tr>
<tr>
<td>Base speed</td>
<td>600 rpm</td>
</tr>
<tr>
<td>Maximum speed</td>
<td>2000 rpm</td>
</tr>
<tr>
<td>Torque ripple</td>
<td>&lt; 3%</td>
</tr>
</tbody>
</table>

Figure 1: Torque-speed curve of desired electric machine for EPS application.

3. Discussion on critical design issues

Great attention should be paid to certain critical issues which primarily impact the machine’s output characteristics. These critical issues mainly include operation mode, rotor structure and slot/pole combination.

A. Operation mode

PM Brushless machines could be driven in both BLDC and BLAC modes. The definitions of BLDC and BLAC mode are related to the waveforms of the back electromotive force (back-EMF) and the driving current [18], viz.,
- BLDC: Trapezoidal back-EMF with rectangular current;
- BLAC: Sinusoidal back-EMF with sinusoidal current.

The typical torque-speed performances [19] of brushless motor driven with BLDC and BLAC modes are shown in Figure 2.

![Figure 2: Typical torque-speed curves with different operation modes.](image-url)

For EPS applications, the electric machine usually runs at low or medium speeds. Then
the BLAC mode is preferred as it can achieve a higher torque output at lower speed. Additionally, the BLAC mode usually results in much smaller torque ripple than the BLDC mode [7], which is highly desirable in EPS applications. Hence, the BLAC mode should be employed, whilst the sinusoidal back-EMF has to be guaranteed.

B. Rotor structure

PM machines provide many possibilities to place magnets on rotors, which can be broadly divided into the SPM or IPM categories according to the fixtures of the PM onto the rotor core. The main SPM types are shown in Figure 3 (a), (b); whereas the main IPM types are shown in Figure 3 (c), (d).

Based on dq-coordinates, the electromagnetic torque can be calculated as,

$$T_e = \frac{3}{2} p \left( \lambda_m \cdot i_q + (L_d - L_q) i_d \cdot i_q \right)$$

where \(p\) is the number of pole pairs, \(\lambda_m\) is the PM-excited flux linkage, \(i_d\), \(i_q\), \(L_d\) and \(L_q\) are \(d\), \(q\)-axes currents and inductances, respectively. For SPMs of type shown in Figure 3(a), where \(L_d = L_q\), the last item in equation (1) is zero. On the contrary, \(L_d < L_q\) for SPMs of type shown in Figure 3(b) and also for the IPMs. Thus, an extra torque boost can be obtained by applying appropriate \(i_d\) and \(i_q\), which is so called reluctance torque [20].

Though SPMs can offer slightly better dynamics due to smaller inductances as a result of low (air-like) permanence of the magnets, IPMs can easily achieve the ideal sinusoidal back-EMF which is tremendously required in BLAC mode. Furthermore, IPMs own many other advantages over SPMs, as will be discussed in the next section.

C. Slot/pole combination

The concentrated windings allow many combinations of slots and poles to PM machines. Different slot/pole combinations have extensive influence on machine characteristics, such as back-EMF, cogging torque, losses and efficiency [2] [18].

Common slot/pole number combinations for 3-phase, non-overlapping winding electric machines are,

$$\frac{N_s}{N_p} = k \left( \frac{3}{2} \right), k = 1,2,3,\ldots$$

where \(N_s\) and \(N_p\) are numbers of slots and poles, respectively. These machines, 3s/2p, 6s/4p, 9s/6p and 12s/9p, inevitably suffer low usage of windings with a winding factor of 0.866.

In order to maximize the winding flux-linkage and power density, coil-pitch should be equal to pole-pitch, which means slot number is equal to pole number. These combinations present maximum flux-linkage and power density, but also large cogging torque, and are therefore only suitable for single phase motors. Thus, the realistic combination of slots and poles should aim at ‘coil-pitch \(\approx\) pole-pitch’ rather than ‘coil-pitch = pole-pitch’. Therefore, \(N_s\) and \(N_p\) differing by 1 and 2 are the two closest cases.

- **Case 1**: \(N_s\) and \(N_p\) differed by 1, viz.,

$$\left| \frac{N_s}{N_p} \right| = 1$$

Electric machines with these slot/pole combinations such as 3s/2p, 3s/4p, 9s/8p, 9s/10p, show a number of merits, including high flux linkage per coil, high torque density and negligible cogging torque. However, there will be a potential weakness in terms of unbalanced magnetic force, which results in vibration and acoustic noise, as well as decreased lifecycle.

- **Case 2**: \(N_s\) and \(N_p\) differed by 2, viz.,

$$\left| \frac{N_s}{N_p} \right| = 2$$

Machines with these slot/pole combinations, for instance, 6s/4p, 6s/8p, 12s/10p, 12s/14p, indicate similarly remarkable attributes, such as high torque density and small cogging torque. Moreover, there is no risk of unbalanced magnetic force.

The analysis shows that Case 2 to be the better option, and the 12s/10p combination has therefore been chosen for this application. The potential merits are confirmed by the comparison of back-EMF waveforms with different slot/pole combinations, as shown in Figure 4. It is clearly shown that the 12s/10p offers more sinusoidal back-EMF than others.
4. Proposed machine

The foregoing discussion has led to an initial model selection of a 12s/10p IPM machine, which is to be driven in BLAC mode. The design of the PM’s shape and other machine parameters can now be effectively completed. The key parameters are listed in Table II, including the winding configuration and rotor shape modification. The proposed machine optimized by FEA is shown in Figure 5.

Table II: Machine parameters.

<table>
<thead>
<tr>
<th>Symbol</th>
<th>Machine Parameter</th>
<th>Value</th>
<th>Unit</th>
</tr>
</thead>
<tbody>
<tr>
<td>$N_s$</td>
<td>Number of slots</td>
<td>12</td>
<td></td>
</tr>
<tr>
<td>$N_p$</td>
<td>Number of poles</td>
<td>10</td>
<td></td>
</tr>
<tr>
<td>$m$</td>
<td>Number of Phases</td>
<td>3</td>
<td></td>
</tr>
<tr>
<td>$N_{coil}$</td>
<td>Number of turns</td>
<td>30</td>
<td>per coil</td>
</tr>
<tr>
<td></td>
<td>PM material</td>
<td>NdFeB35</td>
<td></td>
</tr>
<tr>
<td></td>
<td>Magnetization</td>
<td>Parallel</td>
<td>orientation</td>
</tr>
<tr>
<td></td>
<td>Stator and rotor</td>
<td>35W470</td>
<td>lamination material</td>
</tr>
<tr>
<td>$K_p$</td>
<td>Slot fill factor</td>
<td>54%</td>
<td></td>
</tr>
<tr>
<td>$R_{so}$</td>
<td>Stator outer radius</td>
<td>75.0</td>
<td>mm</td>
</tr>
<tr>
<td>$R_{si}$</td>
<td>Stator inner radius</td>
<td>41.0</td>
<td>mm</td>
</tr>
<tr>
<td>$R_o$</td>
<td>Rotor outer radius</td>
<td>40.0</td>
<td>mm</td>
</tr>
<tr>
<td>$g$</td>
<td>Air gap</td>
<td>0.5-0.95</td>
<td>mm</td>
</tr>
<tr>
<td>$w_{pm}$</td>
<td>PM width</td>
<td>10.0</td>
<td>mm</td>
</tr>
<tr>
<td>$t_{pm}$</td>
<td>PM thickness</td>
<td>2.0</td>
<td>mm</td>
</tr>
<tr>
<td>$w_{st}$</td>
<td>Stator tooth width</td>
<td>5.0</td>
<td>mm</td>
</tr>
<tr>
<td>$l_a$</td>
<td>Active axial length</td>
<td>70</td>
<td>mm</td>
</tr>
<tr>
<td>$I_{peak}$</td>
<td>Rated peak current density</td>
<td>1.7e7</td>
<td>A/m²</td>
</tr>
<tr>
<td>$U_{dc}$</td>
<td>DC-link voltage</td>
<td>42</td>
<td>V</td>
</tr>
<tr>
<td>$P_{em}$</td>
<td>Rated power output</td>
<td>435</td>
<td>W</td>
</tr>
<tr>
<td>$I_{peak}$</td>
<td>Rated peak phase current</td>
<td>14</td>
<td>A</td>
</tr>
<tr>
<td>$R_{ph}$</td>
<td>Phase resistance</td>
<td>0.27</td>
<td>Ω (100 °C)</td>
</tr>
</tbody>
</table>

A. Winding configuration

Non-overlapping concentrated windings are adopted, which exhibit outstanding features of high winding factor (0.933) and short end winding. Only phase A is illustrated in Figure 6.

B. Rotor shape modification

As mentioned previously, sinusoidal back-EMF is required for the BLAC driving mode, while the essential condition is to attain the sinusoidal air gap flux density distribution. A practical technique of rotor shape modification is employed. One of IPM’s important advantages over SPM can be clearly illustrated in Figure 7, where it can be seen that it is much simpler to precisely manufacture the rotor lamination’s outer shape in IPMs, than the magnet’s outer shape in SPMs. This also leads to some other desirable characteristics:

- IPMs use simple rectangular-shape magnets with parallel magnetization -- reducing magnet price and manufacturing cost;
- the magnets are mechanically protected -- suitable for high speed operation without protective rings or retaining sleeves on the rotor;
presence of flux bridge makes the magnets better protected against demagnetization -- offering high overloading capability.

Figure 7: Rotor outer shape modifications for sinusoidal air gap flux density, (a) IPM and (b) SPM.

Besides, it is noteworthy that cogging torque minimization comes along with the gain of sinusoidal air gap flux density distribution.

5. Performance evaluation

A commercial FE software MagneForce is used to evaluate the machine performance by two-dimensional (2-D) FEA.

A. Air gap flux density

As analyzed before, a non-uniform air gap is introduced to obtain sinusoidal flux density distribution, hence sinusoidal back-EMF and negligible cogging torque. The air gap flux density distributions at conditions of no load and full load are given in Figure 8. And the corresponding harmonic components are shown in Figure 9. Since the third harmonic will be eradicated across the line windings, the effective higher harmonic contents are seen relatively small compared with the fundamental, and a good sinusoidal back-EMF is expected.

B. Back-EMF

The three phase back-EMF at the rated speed of 600 rpm is shown in Figure 10, which are visually seen very symmetrical. Fourier analysis is then undertaken to evaluate the harmonic content of the spectrum. The total harmonic distortion (THD) is found to be 0.67%, which means that the back-EMF is essentially sinusoidal.

C. Inductance

Taking the saturation effects into account, the load will affect the permeance, which will result in inductance variation. Based on FEA, \( L_d \) and \( L_q \) are calculated with different load conditions, i.e. variation of phase current with different amplitudes and advanced commutation angles. The results are shown in Figure 11 and 12 respectively. The ratio \( L_q / L_d \) represents for the saliency level of a PM machine, which is determined by the physical structure and load condition, and is related to the reluctance torque. Figure 13 shows the variation of \( L_q / L_d \).
During operations at higher load, $L_q$ varies in the range of almost 40%, while $L_d$ varies in the range of 5% only. This can be explained by the cross-coupling effects between $d$- and $q$- axes, as a result of high magnetic saturation. It is generally known that operations with high magnetic saturation are inherent design features for electric machines with high power density [17].

**D. Torque**

The electromagnetic torque is calculated according to equation (1) under different load conditions, as shown in Figure 14. The maximum torque occurs when the advanced commutation angle is about $25^\circ$. And the separated reluctance torque component is also computed according to equation (5) by utilizing the FEA data obtained in calculating the electromagnetic torque, in order to save simulation time, as demonstrated in Figure 15.

$$T_r = \frac{3}{2} p (L_d - L_q) i_d i_q$$  

Torque ripple should be completely minimized to ensure accurate steering and comfortable driving experience. In general, torque ripple consists of two components, viz., the load dependent component and the load independent component. The former can be extensively ameliorated by employing BLAC mode, and the latter is essentially the cogging torque of the machine, which has already been reduced by means of a sinusoidal air gap flux density distribution, as indicated in Figure 16. Figure 17 shows the output torque waveform at full load condition, where the smoothness of the torque is evident. From the zoomed-in view of the torque ripple in Figure 18, it is further confirmed that the peak to peak torque ripple is 0.17 Nm, or 2.2% of the average output torque, which well exceeds the requirement of less than 3%.
**E. Losses and efficiency**

For EPS applications, the machine runs at low and moderate speed, where electromagnetic losses dominate the total losses. Thus, only the electromagnetic losses are evaluated here. Electromagnetic losses mainly include copper losses in the stator windings $P_{Cu}$, iron losses in the stator and rotor laminations $P_{Fe}$, and eddy current losses in the magnets $P_{PM}$. The power flow can be expressed by,

$$P_{in} = P_{Cu} + P_{Fe} + P_{PM} + P_{out}$$

(6)

Apparently, copper losses are the main part considering that the iron losses and eddy current losses are often small or negligible at low speed. Based on these assumptions, the efficiency map of the proposed motor as a function of phase current and advanced commutation angle is computed and is given in Figure 19.

**6. Conclusions**

A full design procedure of an brushless PM motor drive system used for EPS applications
is proposed. The requirements of the EPS application are firstly introduced and the specifications of the desired machine are then deduced. For correct selection of the right machine topology before detailed electromagnetic machine design, critical issues including operation mode, rotor structure and slot/pole combination are first analyzed. Consequently, the IPM rotor type, BLAC operation mode and 12s/10p combination have been selected for further design. The final design is fully optimized by FEA. Subsequently, the characteristics of the proposed machine such as air gap flux density, back-EMF, inductance, output torque, cogging torque, torque ripple, losses and efficiency, are evaluated. The comprehensive 2-D FEA results verify that the design fully meets the requirements of the steering system. Finally, the mechanical design is shown and a prototype motor has been built for verification in future work.

Acknowledgement
The first two authors gratefully acknowledge the internship supported by the Department of Engineering Systems and Management, Cranfield University, UK, to which this work relates. All authors would like to thank Nanyuan Electric Machinery Co., China for manufacture of the prototype machine, and MagneForce Software Systems Inc., USA for offering evaluation license of MagneForce V4.0.

References

