

## Experimental and Computational Investigation of an “Open” Transonic Cavity Flow

K Atvars<sup>\*†</sup>, K Knowles<sup>\*‡</sup>, S A Ritchie<sup>\*§</sup>

Aeromechanical Systems Group, Cranfield University, Shrivenham, SN6 8LA, UK

N J Lawson<sup>\*\*</sup>

National Flying Laboratory Centre, Cranfield University, Bedfordshire, MK43 0AL, UK

**Abstract:** This paper presents an investigation of a transonic flow ( $M_\infty = 0.85$ ) over a rectangular cavity having a length-to-depth ratio of 5. Velocities were measured inside the cavity on the central plane and two off-centre planes using a two-component particle image velocimetry system. These measurements were supported by surface flow visualisation, and mean and time-varying surface pressure measurements. The flow was also simulated using an unsteady Reynolds-averaged Navier Stokes code, with a realizable  $\kappa-\varepsilon$  turbulence model. It is shown that this CFD model does not capture all the characteristics of the flow field correctly. However, by using this integrated experimental and computational approach we have been able to identify three-dimensional flow field structures within the cavity. The influence of the thickness of the approaching boundary layer is discussed.

**Keywords:** transonic cavity, flow-visualisation, PIV, URANS CFD

### 1 INTRODUCTION

The phenomenon of flow within a rectangular cavity immersed in transonic flow has become the focus of much research interest recently due to the importance of stealth (and aerodynamic efficiency) in future manned aircraft, such as the F-35 Lightning II, and various unmanned combat air vehicle (UCAV) projects. These aircraft are designed such that the internal carriage of weapons is vital in maintaining a low radar cross-section, which in turn increases the vehicle's survivability. However, when the weapons bay doors are opened for weapons release, flow over the exposed cavity can cause a number of undesirable effects. These include self-sustaining acoustic oscillations and high intensity tones that can lead to structural fatigue [1] (occurring, primarily, in cavities with a low ratio of streamwise length,  $L$ , to cavity depth,  $H$ ) and adverse longitudinal pressure distributions leading to nose-in pitching moments on stores released from the cavity (primarily for high  $L/H$ ) [2].

As suggested above, rectangular cavity flows can be defined as one of two main types, primarily dependent on the length-to-depth ratio ( $L/H$ ) of the cavity [3] (see Fig 1). “Open” cavity flows (Fig 1a) occur in cavities with  $L/H < 7-9$  (typically) and are characterised by strong pressure oscillations which lead to noise radiation (often in excess of 170dB), structural vibration and high levels of heat transfer at the trailing edge. “Closed” cavity flows (Fig 1b) occur in cavities with  $L/H > 10-14$  (typically) and are regarded as quasi-steady

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\* Authors are listed alphabetically.

† Research Fellow

‡ Professor of Aeromechanical Systems. Email: K.Knowles@cranfield.ac.uk

§ Research Officer

\*\* Reader and Pilot

flows. The pressure distribution along the floor of a “closed” cavity shows a large longitudinal pressure gradient (**Fig 1c**) that causes a large increase in pressure drag and can lead to stall separation difficulties. Cavity geometries in the approximate range  $8 < L/H < 11$  are described as “transitional” and here the cavity flows exhibit a combination of “open” and “closed” flow features (**Fig 1c**). Note that Plentovich et al. [3] found that the precise boundaries between open, transitional and closed flows (defined by the centre-line pressure distribution) depend on freestream Mach number and cavity width-to-depth ratio (W/H). Nevertheless, open flow always occurred for  $L/H < 7$ .

For “open” cavity flows, the pressure oscillations which are observed were initially investigated by Rossiter [4]. Rossiter proposed a feedback loop, whereby acoustic waves would form at the downstream wall from vortices shed initially from the upstream cavity wall, with synchronisation occurring between points in the loop. This resulted in the semi-empirical “Rossiter Equation”, which can be used to predict the frequency for a given mode of oscillation in a given cavity geometry:

$$f = \frac{U_\infty}{L} \frac{(m - \alpha)}{\left(M_\infty + \frac{1}{K}\right)} \quad (1)$$

This was subsequently modified [5] to account for the higher speed of sound within the cavity, which is approximately equal to the freestream stagnation speed of sound. This “modified Rossiter Equation” is used here to predict the frequencies of the various oscillation modes in an open cavity flow:

$$f = \frac{U_\infty}{L} \frac{(m - \alpha)}{M_\infty \left[1 + \frac{(\gamma - 1)}{2} M_\infty^2\right]^{-1/2} + \frac{1}{K}} \quad (2)$$

$\alpha$  is an empirical constant, related to the phase lag between instabilities in the shear layer and upstream-travelling pressure wave, which is dependent on cavity length-to-depth ratio and is

$$\text{given by } \alpha = 0.062 \left(\frac{L}{H}\right)$$

The constant  $K$  is the empirical ratio of shear layer and freestream velocities;  $K = 0.57$  is appropriate for thin initial boundary layers but decreases with increasing boundary layer thickness.

Many previous studies of cavity flows have concentrated on the time-averaged and unsteady measurement of the flow using static pressure taps on the surfaces and qualitative visualisation techniques such as schlieren imagery and oil flow visualisation [6-8]. The results of these studies have typically been compared to numerical models with mixed success [9, 10]. There is currently very little data available on the off-surface flowfield within different cavity geometries under transonic conditions. Despite recent improvements in optical measurement techniques such as particle image velocimetry (PIV) [11, 12] and laser Doppler anemometry (LDA) [13], there appears to be little, if any, quantitative flow measurement of the structure of a transonic cavity flow that is not confined to the centre-line of the cavity [14]. In this investigation we present results of applying PIV measurement techniques to a transonic cavity flow and incorporate results from surface pressure

measurements, surface flow visualisation and numerical simulation to produce an overall image of the flow structure in a transonic cavity flow.

## 2 EXPERIMENTATION

All tests were conducted using the Shrivenham transonic wind tunnel (TWT), which has a working section of 206mm (high) by 229mm (wide). This is a closed-circuit, ejector-driven tunnel supplied with air from two Howden screw-type compressors. The compressors supply air at up to 7 bar(g), which is dried and stored in a 34m<sup>3</sup> reservoir. The stored air is sufficient to run the tunnel at Mach 0.85 (the test condition for the present measurements) for about 15 seconds.

The geometry of the cavity is indicated in **Figure 2**, together with the co-ordinate system used here and its origin. To enable optical access for PIV measurements, an all-glass cavity was mounted from the underside of a flat plate which had a sharp leading edge and was raised some 16mm away from the tunnel side wall (**Figure 3**). Data could not be acquired for the first 2mm of the cavity depth due to the presence of the splitter plate. Similarly, the wind tunnel design does not allow the freestream flow to be measured using PIV, because of a lack of optical access but glass panels were fitted in the flat plate upstream and downstream of the cavity to enable LDA measurements in the freestream. For cavity floor pressure measurements and oil flow visualisation an aluminium cavity was used. In each case, the cavity had dimensions of  $L = 160\text{mm}$ ,  $W = 80\text{mm}$  ( $L/W = 2$ ). For the results presented here the cavity had a depth of  $H = 32\text{mm}$ , to give  $L/H = 5$  (other  $L/H$  values were also tested but are not discussed here). This resulted in a blockage ratio of 5%, which is well within acceptable limits for high-speed tunnel testing [15].

At  $M_\infty = 0.85$  a freestream turbulence intensity of 5 - 6% was measured between 20mm and 150mm above the plane of the cavity ( $y/H = 0.63 - 4.7$ ). A pitot-static probe, located 30mm upstream of the cavity leading edge ( $x/H = -0.94$ ), was used to measure the flow approaching the cavity. This revealed a turbulent boundary layer with thickness  $\delta_{0.99} = 18.7\text{mm}$  ( $0.584H$ ), which can be expected to grow a further 0.6mm by the leading-edge of the cavity. This is much thicker than the natural TWT wall boundary layer at this point (6mm) and appears to be the result of a separation at the plate leading edge, followed by a turbulent reattachment.

A custom-built seeding system injected water particles of 5-10 $\mu\text{m}$  diameter into the contraction section to seed the flow (**Figure 3**). This size resulted in a seeding response error of 2.3% of the measured velocity, using the error calculation method described by Dring [16]. The PIV acquisition system consisted of a Dantec FlowMap 500 processor, a Kodak ES1.0 CCD camera and a New Wave Gemini Nd:YAG pulsed laser. The light sheet was projected into the cavity through the clear floor. The seeded light sheet was viewed perpendicularly via a surface-coated mirror angled at 45 $^\circ$  to the cavity right side wall (see **Figure 3**). PIV data were taken for the same three x-y planes across the cavity on which pressure data were acquired (see below).

The Kodak ES1.0 camera frame rate and laser repetition rate allowed data to be recorded at up to 15Hz. This frame rate was too low to capture the unsteady phenomena in the cavity, so time-averaged flow data derived from the instantaneous data are presented from the PIV. (At least a 2kHz system would be needed before time-resolved data could be acquired successfully at this scale.) Time-averaging was performed in correlation-space, which also improved the resolution in regions where fewer particles had been entrained in the flow, such

as in the cavity upstream recirculation region. A set of 700 image pairs were acquired per run at a 15Hz sampling rate and processed into instantaneous vector maps using a window-deformation FFT code; these were then time-averaged. To process the PIV images, DaVis software by La Vision was used. The software employs an iterative image-deformation algorithm, similar to those reviewed by Scarano [17], which more effectively extracts vectors from complex rotating flows with high velocity gradients (as seen in open cavity flows). The window-deformation technique deforms the interrogation region in the second frame according to the velocity gradient present within that region. This leads to identical displacements for all the seeding particles within a region giving an improved signal-to-noise ratio and thus higher accuracy. To process the images, 4 passes were used with two passes at  $32 \times 32$  pixels and two passes at  $16 \times 16$  pixels. All regions were 75% overlapped in  $x$  and  $y$ . To aid clarity, the vector maps presented here were post-processed by sub-sampling by a factor of 3. Based on the seeding response, the geometry error and the processing error, estimated accuracy in this case is better than 3.4% of full-scale measurement. The accuracy of the PIV measurements could have been increased by using seeding particles with sub-micron diameters, however, this would then require greater laser power to scatter an equivalent amount of light, which was not possible for the present tests.

Surface flow visualisations were performed using a paraffin-based solution containing solar yellow fluorescent paint particles. By subjecting the particles to ultraviolet (UV) light, the surface flow patterns were clearly visible and could be photographed using digital still photography. Cavity floor pressures were measured using three rows of 9 pressure tappings each, at  $z/W = 0.5, 0.667$  and  $0.833$  (referred to as the  $CL$ ,  $OC1$  and  $OC2$  planes respectively). These tappings were connected via 46 cm lengths of tubing of a known frequency response, to a Scanivalve ZOC block electronically-scanned pressure transducer containing 32 piezo-resistive pressure sensors. Measurements were taken at a sample rate of 10kHz, and filtered at 5kHz with a resolution of approximately 5Hz; 65 536 samples were taken at each of 4 TWT runs and averaged.

### 3 COMPUTATION

Numerical simulation data were obtained using time-averaged URANS (unsteady, Reynolds-averaged Navier-Stokes) CFD predictions. The URANS approach used here employed the Fluent commercial code and adopted the realizable  $\kappa - \varepsilon$  turbulence model. This turbulence model was chosen as it includes modifications over the standard  $\kappa - \varepsilon$  model which make it more suitable for use in flows containing regions of high shear and swirl [18].

Previous work has shown that open-type cavity flows are largely symmetrical about the centreline plane, when time-averaged [19]. For the present work, this was confirmed by comparing full and half-domain calculations in terms of mean flow structure and mode shapes; although not identical, both agreed equally well with experiments. For most of the results presented here, therefore, only half of the domain was calculated, with symmetry imposed on the centreline plane. This greatly reducing the computational requirements, but at the expense of suppressing any lateral oscillation modes. A mesh refinement study led to the adoption of a mesh containing 952 000 quadrilateral cells (for the half domain, twice this for the full domain), which was found to be sufficient to resolve accurately the Rossiter modes (see Ritchie [20]). This mesh had an increasing number of cells closer to the edges of the cavity (Fig 4). Approximately 20 cells were used to resolve the boundary layer profile upstream of the cavity, with a minimum cell height chosen to give  $y^+$  values of the order of unity. This boundary layer profile was specified to match the experimentally-measured

profile. Calculations were also performed with a much thinner, naturally-growing (but tripped) turbulent boundary layer approaching the cavity [20]. The upstream and downstream domain boundaries (inlet and outlet) were located  $2L$  from the cavity leading edge and trailing edge, respectively. The distance from the surface plane to the upper domain boundary was also  $2L$ , which was found to reproduce free-stream flow conditions at that boundary.

The time step was defined by the sampling rate required to resolve the second Rossiter mode with 50 data points [21]. At this time-step of  $\Delta t = 1.76 \times 10^{-5}$  s the results had also been found to have converged, based on the measurements of the first Rossiter mode. The simulation was initially run to achieve a steady solution, as determined by the static pressure at the mid-height of the downstream wall of the cavity varying by less than 1%. Then the unsteady solution was attained over a further 20 000 time steps, which also ensured transients from start-up had been purged.

## 4 RESULTS & DISCUSSION

### 4.1 Time-averaged Pressure Data

The experimental and numerical time-averaged pressure coefficient data are shown for the three planes within the cavity in **Fig 5**. Although the general levels of  $C_p$  are similar in the two data sets it is clear that the form of the pressure distributions is different; this will be discussed below.

Both the experiments and the CFD show only small differences in pressure distribution between the three planes ( $CL$ ,  $OCI$  and  $OC2$ ). In general for both cases the further from the centreline the lower the pressure, suggesting slightly higher velocities nearer the sidewalls. This small effect is, however, less apparent in the CFD than the experiments.

The CFD results show fairly uniform pressure ( $C_p$  close to zero) for approximately 80% of the cavity length, before a sharp increase near the downstream wall. This form is typical of an open flow, as suggested by Stallings and co-workers [2, 3] and shown in **Fig 1**. By contrast, the experimental  $C_p$  along the first 60% of the cavity floor is slightly negative, reaching a minimum at approximately  $x/L = 0.4$ .  $C_p$  continues rising over the downstream 40% of the cavity length, reaching a maximum recorded value at  $x/L = 0.9$ . These experimental pressure distributions within the cavity are typical of flow on the boundary between open-type and transitional-open-type flows (see **Fig 1**). It is suggested here that this is probably due to the thick boundary layer in the present experiments. Although this effect could not be reproduced fully by the CFD it was seen in all our experimental studies on other cavity geometries: in each case the pressure distribution was typical of a higher length-to-depth ratio than that being tested. Despite this difference (between CFD and experiments), the internal structure of the cavity flow is largely unaffected by this apparent transition [22].

### 4.2 Unsteady Pressure Data

**Fig 6** shows the unsteady pressure spectra from the pressure tapping at  $x/L=0.9$  on the  $CL$  plane for the experimental and numerical cases. Both spectra show the presence of high intensity peaks within the signal, the frequencies of which are compared with the theoretical Rossiter frequencies calculated using Eqn 2. The agreement between the theoretical and experimental results is excellent for the 1<sup>st</sup> and 3<sup>rd</sup> Rossiter modes, with the experimental data showing less than 0.5% variation from the theoretical data in both cases. There is similarly-close agreement for both of the off-centre planes (there is only a slight change of

experimental frequency for the second and third modes). The second mode shows a broader peak in the experimental data but this is also at a similar frequency to the prediction of the modified Rossiter equation (Eqn 2).

The numerical simulation shows slightly higher frequencies than the experiments for the first and third modes, but both are within about 10% of the theoretical values (which do not vary with spanwise position). There is no change in first mode frequency and only a small change (4Hz) in the 3<sup>rd</sup> computed mode between the three planes. There are no 2<sup>nd</sup> mode peaks visible in the numerical simulation spectra above the background noise level for any of the three planes. The cavity is shown to be oscillating with a 1<sup>st</sup> mode dominance in both the experimental and numerical cases, which suggests that the simulation has successfully predicted the oscillation feedback mechanism within the cavity. The numerical 1<sup>st</sup> mode peak *SPL* of 155dB compares with 161dB seen experimentally. The highest-frequency oscillation mode in both the experimental and numerical data is the 3<sup>rd</sup> mode, after which the background noise level swamps any frequency peaks.

The issue of simulating the flow with a plane of symmetry can also be addressed indirectly by looking at unsteady pressure spectra. It is known that asymmetric flow inside a cavity correlates with a second Rossiter mode dominance in the pressure spectrum [23]. The second mode appears to be much reduced in the experimental case and appears to be completely absent in any discernable form from the CFD results. This absence of second-mode dominance in both CFD and experimental results suggests that the symmetry condition on the CFD domain is not affecting the predicted flow structures [23]. A full-domain 3D simulation (discussed further below) has also qualitatively shown good agreement with the symmetry condition.

### 4.3 Surface Flow Visualisation

The pressure coefficient profiles and unsteady spectra have been used to identify the type of flow and oscillation modes occurring within the cavity; a more detailed description of the flow behaviour and structure, however, is not possible from these data alone. Description of the flow behaviour can be further developed with reference to the surface flow visualisation study.

The experimental and computational surface flow patterns are presented in **Fig 7**. Note that the experimental images of the side and end walls (**Fig 7a**) include some perspective error, so, in each case, the diagonal line along the edge of the image is a corner of the cavity. In both the experimental and numerical cases, the streamlines on the floor of the cavity show that the flow is travelling against the freestream direction over most of the cavity length and width, which is consistent with a large single recirculation region in the cavity rotating clockwise for a freestream flow travelling left to right.

The CFD results in **Fig 7b** show a similar pattern on the cavity floor to the experiments, but the side wall reveals that the main recirculation region is further downstream than in the experiments. These CFD results have been produced with a thin, “natural” boundary layer approaching the cavity: the imposition of the thick, experimental boundary layer produced an even more downstream position for the main recirculation. The full-domain calculations, which were only conducted with the thin boundary layer, give surface flow patterns (**Fig 7c**) which are very similar to those seen in **Fig 7b**.

In both the experiments and the CFD the cavity floor streamlines show two contra-rotating flow structures either side of the centreline plane with flow rotation in towards the centreline of the cavity, much like a focus sink. The structures are described in ESDU Item 02008 [24] as ‘tornado-like’ vortices which spiral up towards the mouth plane (i.e. the open plane) of the cavity. Their subsequent trajectory is not speculated on in ref [24] but will be discussed further in the next section. These structures are formed when the flow travelling upstream along the floor of the cavity reaches the natural flow boundary formed by the upstream wall. The proximity of the cavity sidewall forces the flow to divert in the spanwise direction towards the centreline of the cavity. When the flow reaches the CL plane, it meets the flow from the other side of the centreline and is forced to turn to flow downstream but is prevented from doing so by the flow travelling upstream along the cavity floor. The flow is forced to turn out towards the sidewall of the cavity which forms the vertical ‘tornado-like’ structures seen on the cavity floor. Note that similar structures are still seen in “closed” type cavity flows (for higher length-to-depth ratios than used here) but their sense of rotation is reversed [24]. Our recent CFD calculations suggest that only one “tornado-like” vortex exists for narrow cavities with  $W/H=1$ .

#### 4.4 Flowfield Data

**Fig 8** shows the PIV-derived vector maps for the three planes within the experimental cavity. The peak velocity magnitude in the centreline (*CL*) plane is approximately  $140\text{ms}^{-1}$  (52% of freestream value) which is seen in the deflected shear layer near the downstream wall. The peak vertical velocity in this plane is  $v = 80\text{ms}^{-1}$  and occurs directly adjacent to the downstream wall. The shear layer was seen to have a deep deflection into the cavity at the downstream wall. This causes an acceleration of the flow over the deflected shear layer into the cavity near the downstream wall, which is where the  $140\text{ms}^{-1}$  peak velocity was measured.

The *OCI* mean flowfield is similar to that on the centreline, with virtually identical peak velocity magnitude ( $140\text{ms}^{-1}$ ) and peak vertical velocity ( $80\text{ms}^{-1}$ ). The *OC2* plane shows a quite different flow structure and lower peak velocities: the peak velocity magnitude is approximately  $100\text{ms}^{-1}$  (37% of freestream value) and the peak vertical velocity is approximately  $v = \pm 30\text{ms}^{-1}$ . These lower peak velocities in the *OC2* plane appear to be because the shear layer is no longer deflected into the cavity but instead is elevated above the level of the mouth plane by the proximity to the sidewall.

To improve visualisation of the velocity data, line integral convolution (LIC) images [25] of the derived streamlines are presented in **Fig 9** for the three planes in the experimental data. These show a single large recirculation whose centre moves slightly upstream as the sidewall is approached. On the *OC2* plane, however, there are clearly two recirculation regions and inspection of the vector maps reveals that these are co-rotating. This will be discussed further, below, with the aid of the CFD. The peak vertical velocity in the *OC2* plane occurs in the vertical motion regions of this second recirculation, rather than being associated with the shear layer impinging on the downstream wall as in the *CL* and *OCI* planes.

The numerical data from both the half-domain and full-domain simulations are compared with the experiments in terms of LIC plots for the *OCI* plane in **Fig 10**. In both the computational cases the “thin” upstream boundary layer was used. It can be seen that both CFD results contain a large recirculation region but that this is further downstream than in the experiment; this is consistent with the surface flow visualisation results discussed above. The full-domain CFD also shows some form of vertical flow structure towards the upstream wall;

this is not clear in the experiment because of the poor flow seeding density in this region. Something similar is seen in the half-domain calculation but the most prominent feature in this case is a second recirculation in the upper half of the cavity; this only appears in plane *OC2* for the full-domain calculation. It is worth noting that the full-domain and half-domain CFD calculations give very similar flowfields on the *CL* plane, with agreement as close as is seen in the sidewall flow visualisations (**Fig 7**).

The full, 3D flowfield within the cavity can only be visualised from the CFD data. Care must be taken to refer to experimental evidence wherever possible because of the differences between the CFD and experiments. It should also be borne in mind that we are presenting here time-mean results for an unsteady flowfield. **Fig 11** presents 3D visualisations of the full-domain CFD results. **Fig 11a** shows the two “tornado-like” vortices in the upstream third of the cavity, with the single, large recirculation further downstream. Also visible in this figure are two vortices trailing downstream from the downstream corners of the cavity: this feature is consistent with the surface flow visualisations of Taborda et al. [7] (see also [24]). The side view of the cavity flowfield in **Fig 11b** can be compared with the surface flow visualisations of **Fig 7** and with the experimental LIC visualisations of **Fig 9**. As has been pointed out above, the CFD is showing a main recirculation which is somewhat further downstream than seen in the experiments. Aside from this difference, however, the global features of the mean CFD flowfield agree well with the experimental evidence of **Figs 7 & 9**. In particular, the CFD reveals how the second recirculation region seen in **Fig 9c** relates to the side wall flow patterns of **Fig 7a** and the downstream trailing vortices. This aspect is further clarified by the view shown in **Fig 11c**. This upstream view of the downstream wall of the cavity also reveals a small corner vortex between the floor and end wall, which is consistent with the experimental surface flow visualisation (**Fig 7a**).

A key question which arises over the “tornado-like” vortices regards their trajectory above the floor of the cavity. In ESDU Data Item 02008 [24] it is conjectured that they are more or less vertical; their fate on reaching the mouth plane of the cavity is not discussed. From **Fig 11a** it can be seen that flow from these vortices is swept downstream and enters the main cavity recirculation. This is shown more clearly in **Fig 12**, which is the result of a DES (i.e. a hybrid LES/RANS) calculation on a similar geometry to the experiments (only the width is slightly different) with the thick experimental boundary layer imposed upstream.

## 5 CONCLUSIONS

The current study of an empty  $L/H=5$  rectangular cavity in a transonic freestream has integrated experimental and numerical techniques to gain a detailed insight into the 3D flow behaviour throughout the cavity. As well as surface flow visualisation, the experiments have measured mean and unsteady pressures on the cavity floor, and mean velocities on 3 planes inside the cavity. Numerical flowfield predictions have used an unsteady RANS model.

The mean pressure distribution inside the experimental cavity suggests a flow on the boundary between “open” and “transitional-open”. This is felt to be due to the thickness of the boundary layer (approximately half the cavity depth) in the experiments. This effect could not be completely reproduced by the present URANS modelling, although changing the boundary layer thickness did change the predicted flowfield significantly. The CFD, even with the experimental boundary layer imposed, shows a typical “open” flow pressure distribution.



A strong oscillation feedback mechanism is present within the cavity. Both the experimental and numerical unsteady pressure spectra show up to the third Rossiter mode of oscillation; experimental mode frequencies have excellent agreement with the theoretical values calculated using the “modified-Rossiter” equation (Eqn 2). The cavity flow is seen to oscillate in 1<sup>st</sup> mode dominance with a peak SPL of approximately 160dB. The CFD shows reasonable agreement in terms of frequencies and peak sound pressure levels. There is, however, no clear second Rossiter mode in the half-domain CFD results, possibly because of the assumption of lateral symmetry.

Flow visualisation (both surface oil and PIV-derived) shows a single main recirculation in the body of the cavity, with two vertically-oriented “tornado-like” vortices upstream of this. The CFD shows the same key flow features, albeit with the main recirculation predicted further downstream. Nevertheless, the CFD is sufficiently close to the experimentally-observed flowfield to allow some confidence in its use to elicit other major flowfield features. Thus, it appears that the “tornado-like” vortices bend downstream and are swept into the main recirculation region. Close to the downstream corners of the cavity two vortices leave the main recirculation and trail downstream away from the cavity.

More detailed analysis of the unsteady behaviour of “open” cavity flowfields will require a time-resolved PIV system, with kHz repetition rates, and a hybrid LES/RANS CFD approach.

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## Appendix

### Notation

$CL$	cavity centreline plane: $x$ - $y$ plane at $z/W=0.5$
DES	Detached Eddy Simulation
$f$	cavity oscillation mode frequency (Hz)
$H$	cavity depth (m)
$K$	empirical ratio of shear layer and freestream velocities
$L$	cavity length (m)
LES	Large Eddy Simulation
LIC	Line Integral Convolution
$m$	cavity oscillation mode number
$M_\infty$	freestream Mach number
$OC1$	cavity off-centre plane 1: $x$ - $y$ plane at $z/W=0.667$
$OC2$	cavity off-centre plane 2: $x$ - $y$ plane at $z/W=0.833$
PFF	“pressure far field” boundary condition
RANS	Reynolds-averaged Navier Stokes
$SPL$	sound pressure level (dB)
TWT	transonic wind tunnel
$u$	velocity component in the $x$ direction (m/s)
$U_\infty$	freestream velocity (m/s)
URANS	Unsteady RANS
$v$	velocity component in the $y$ direction (m/s)
$w$	velocity component in the $z$ direction (m/s)
$W$	cavity width (m)
$x$	co-ordinate from the cavity leading edge, parallel to the cavity length and the freestream
$y$	co-ordinate normal to the cavity mouth plane, pointing out of the cavity
$z$	co-ordinate from the cavity left wall, parallel to the cavity width
$\alpha$	empirical constant related to the phase lag of the cavity oscillation process
$\gamma$	ratio of specific heats, = 1.4 for air

$\delta_{0.99}$

boundary layer thickness, measured to 99% of  $U_\infty$

## Figure captions

**Fig 1** Cavity flow types: a) schematic of subsonic, open cavity flow; b) schematic of subsonic, closed cavity flow; c) classification for subsonic flows, based on streamwise pressure gradient, after Stallings et al. [2]

**Fig 2** Cavity geometry and axis systems

**Fig 3** PIV experimental set-up

**Fig 4** CFD domain and grid: a) domain construction and boundary type; b) overview of grid in and around cavity; c) detail of grid around upstream cavity lip.

**Fig 5** Comparison of mean pressure coefficient profiles: experiment vs 3D CFD, half-domain simulation

**Fig 6** Comparison of unsteady pressure spectra on centreline at  $x/L = 0.9$ : experiment vs 3D CFD, half-domain simulation. Experimental spectrum has been adjusted for frequency response of apparatus. The vertical lines indicate the first three Rossiter modes according to Equation 2.

**Fig 7** Surface flow patterns: a) experimental flow visualisation; b) surface streamlines from 3D CFD, half-domain simulation, “thin” boundary layer; c) sidewall streamlines from 3D CFD, full-domain simulation, “thin” boundary layer.

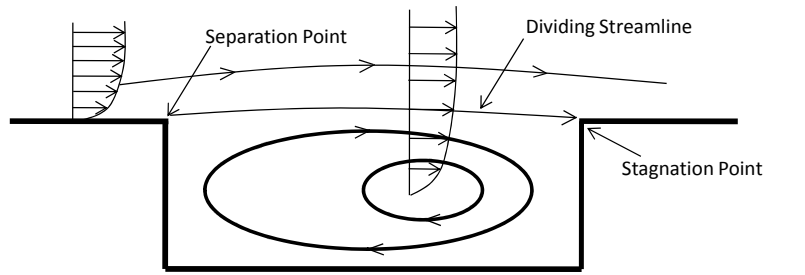
**Fig 8** PIV results: velocity vectors, coloured by magnitude, for planes  $CL$  (top)  $OCI$  (middle) and  $OC2$  (bottom). The icon in the top right indicates that these results are for an empty cavity.

**Fig 9** LIC images of the PIV-derived velocity vector fields: a)  $CL$  plane; b)  $OCI$  plane; c)  $OC2$  plane

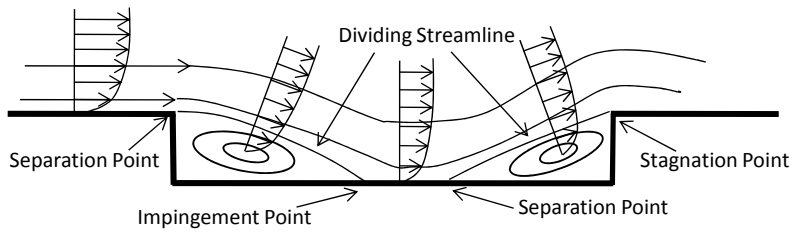
**Fig 10** LIC images of  $OCI$  plane: (a) PIV results, (b) CFD results with a half-domain simulation and (c) CFD results with a full domain simulation. All images are of the full domain inside the cavity; freestream flow is from left to right over the top of the cavity in each case.

**Fig 11** Visualisation of the 3D CFD flowfield; full-domain simulation: a) view from in front of the cavity looking downstream, front and side walls removed for clarity; b) side view of cavity with side wall removed for clarity, freestream flow from left to right; c) view looking upstream from the back wall (removed for clarity, together with the side walls). Streamtraces coloured by velocity magnitude.

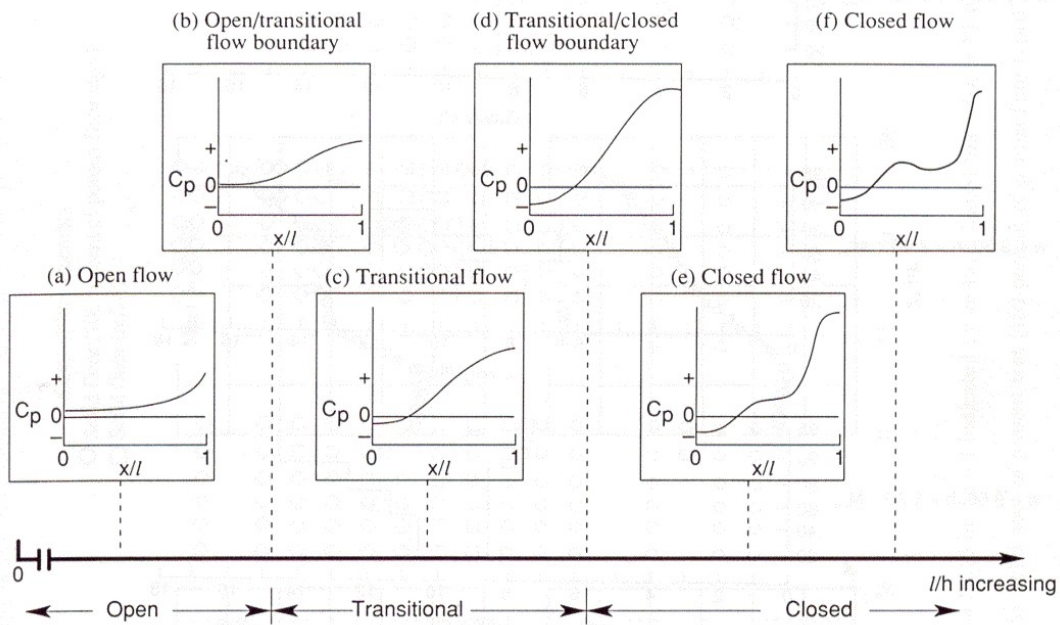
**Fig 12** Visualisation of 3D CFD: DES courtesy of Bidur Khanal (unpublished);  $M_\infty = 0.85$ ,  $L/H=5$ ,  $W/H=2$ , thick experimental boundary layer; view from in front of the cavity looking downstream, front and side walls removed for clarity. Streamtraces coloured by velocity magnitude.



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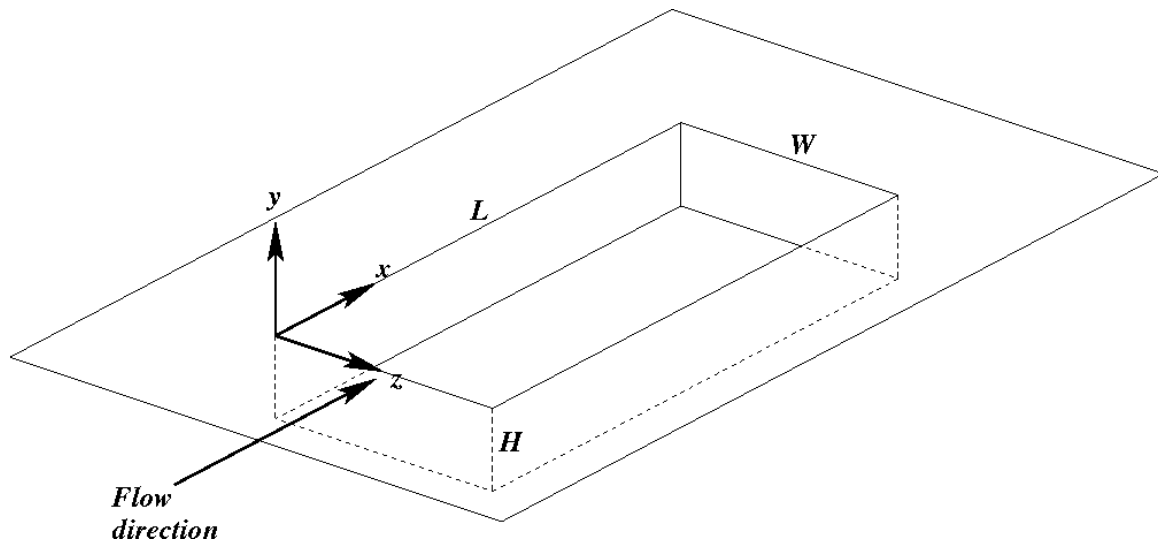


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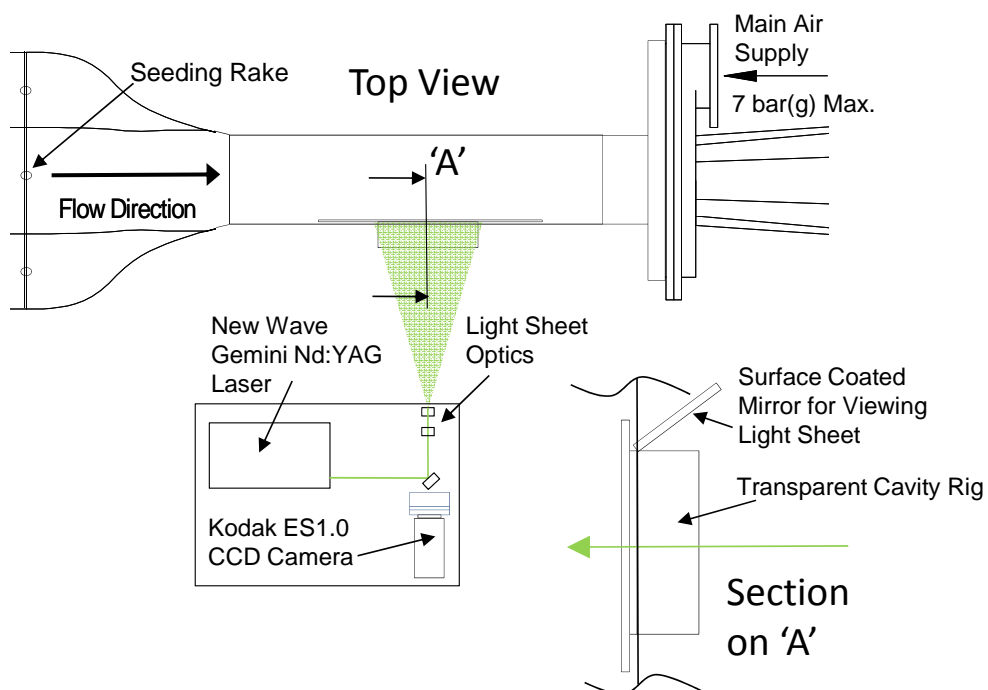


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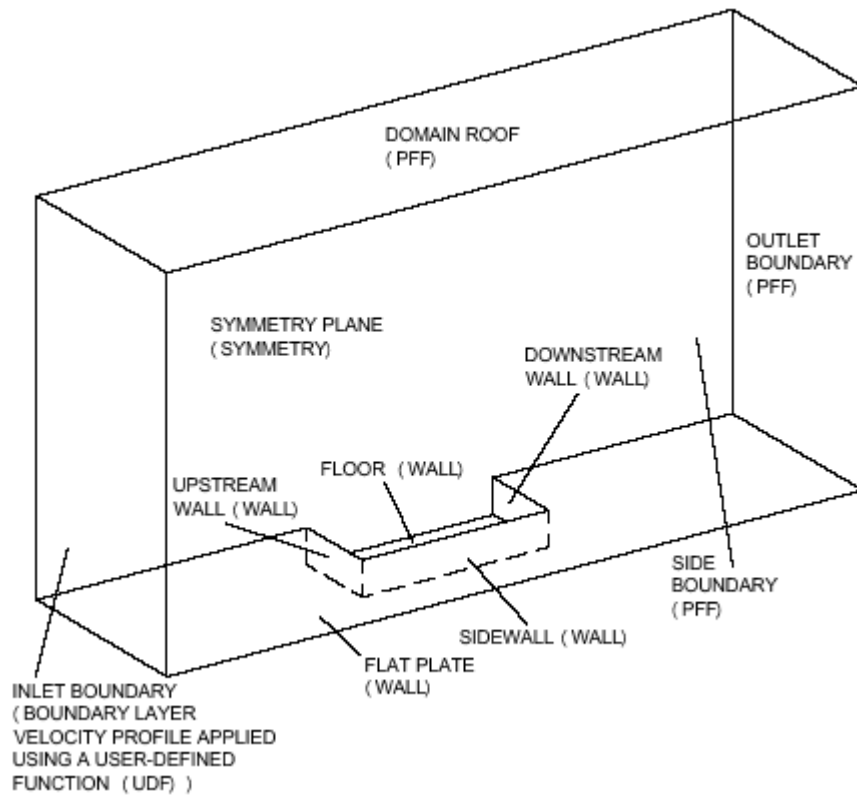
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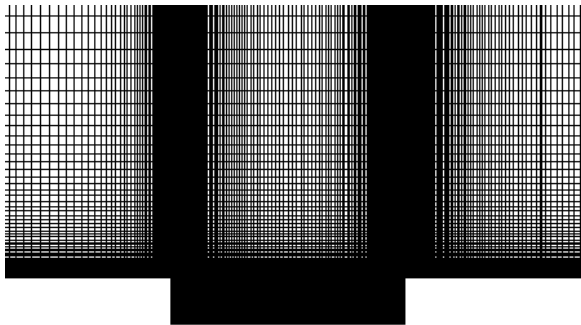
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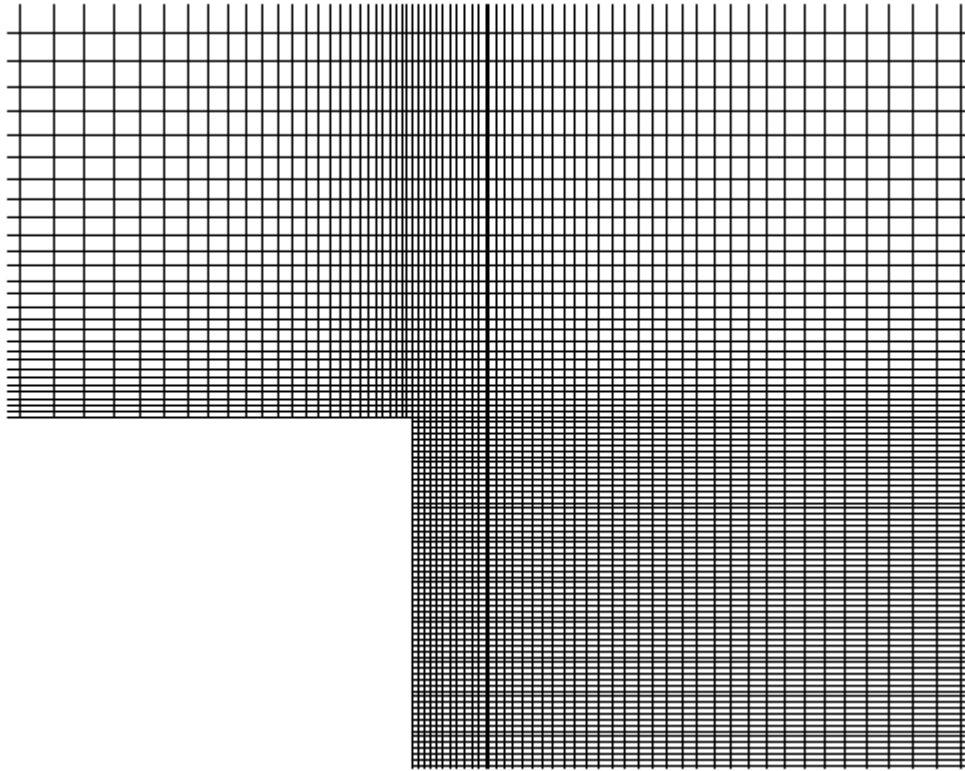


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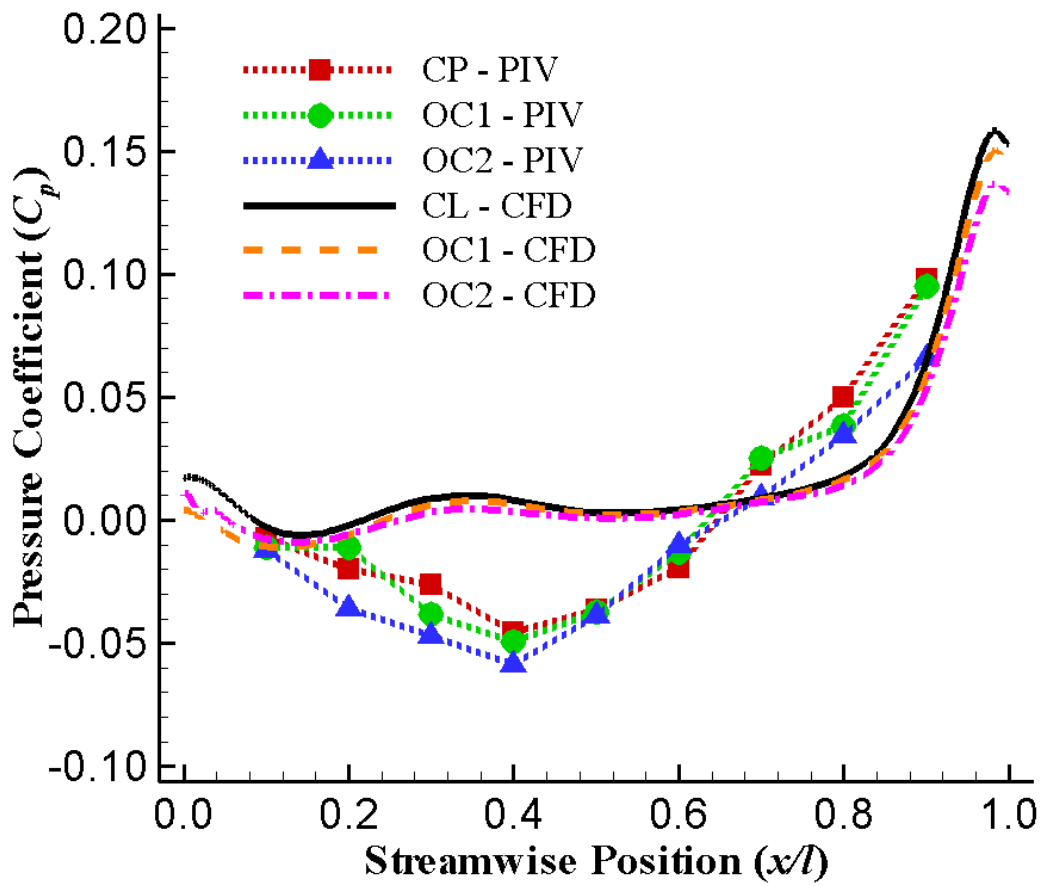
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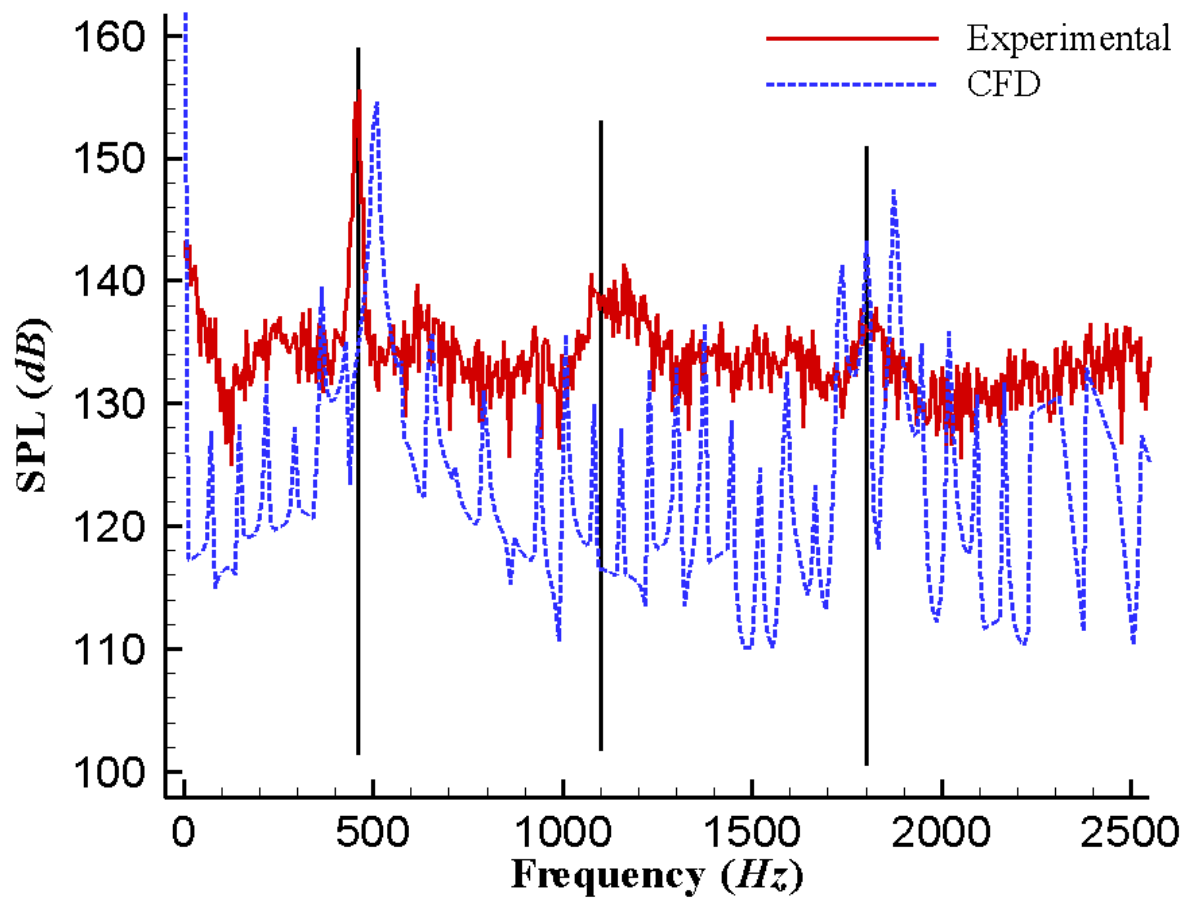


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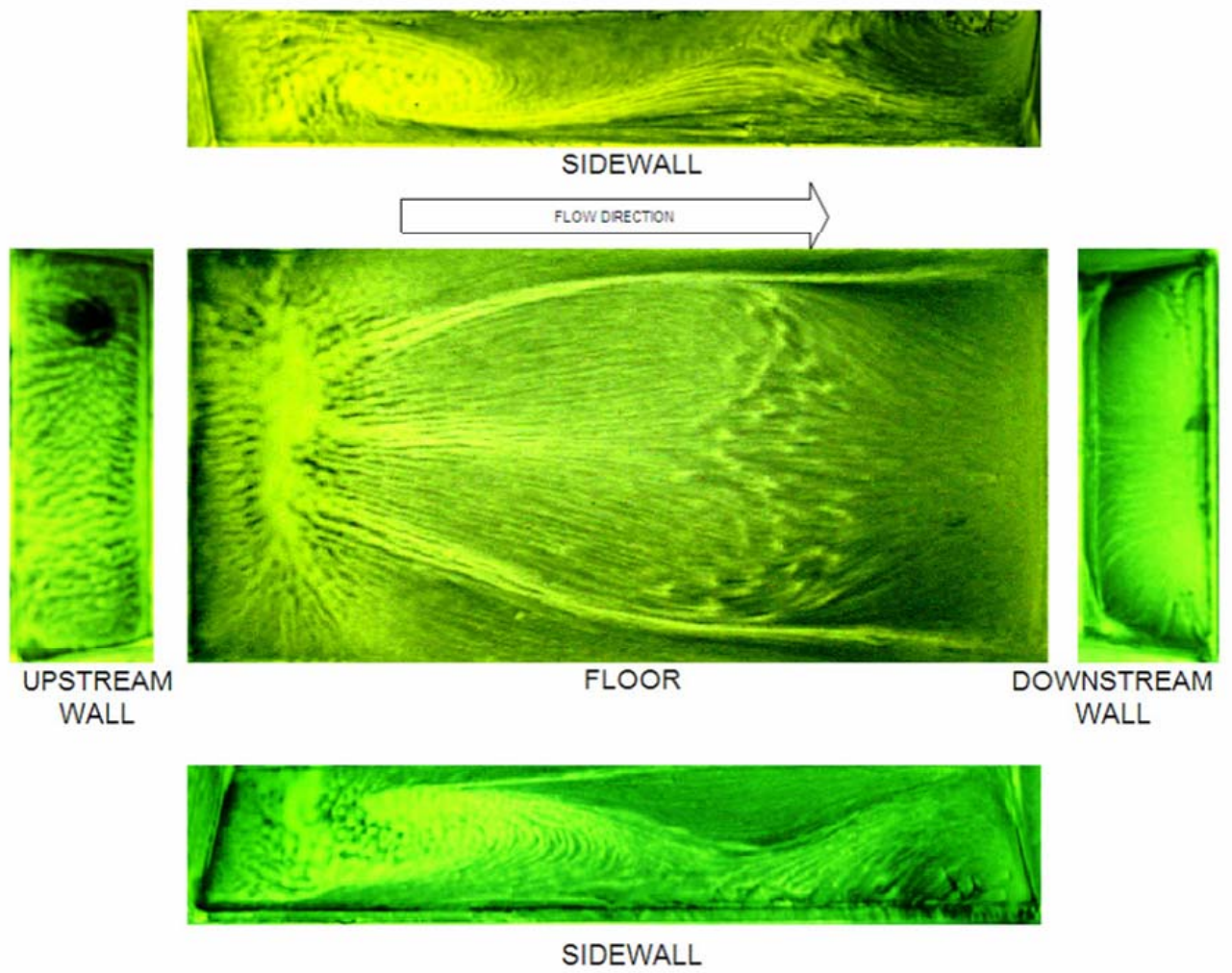
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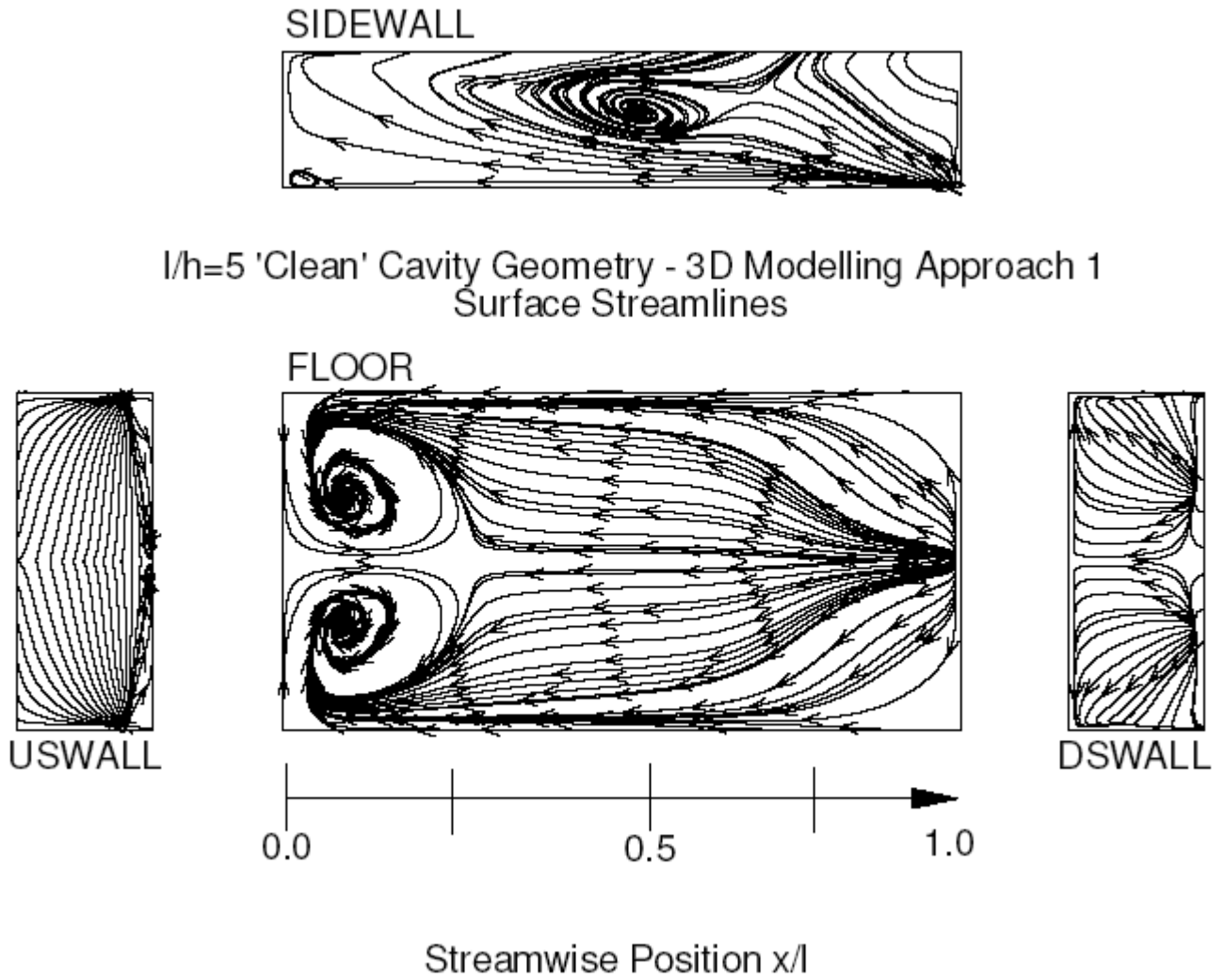
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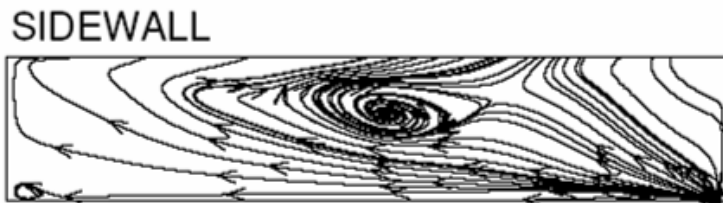
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a)

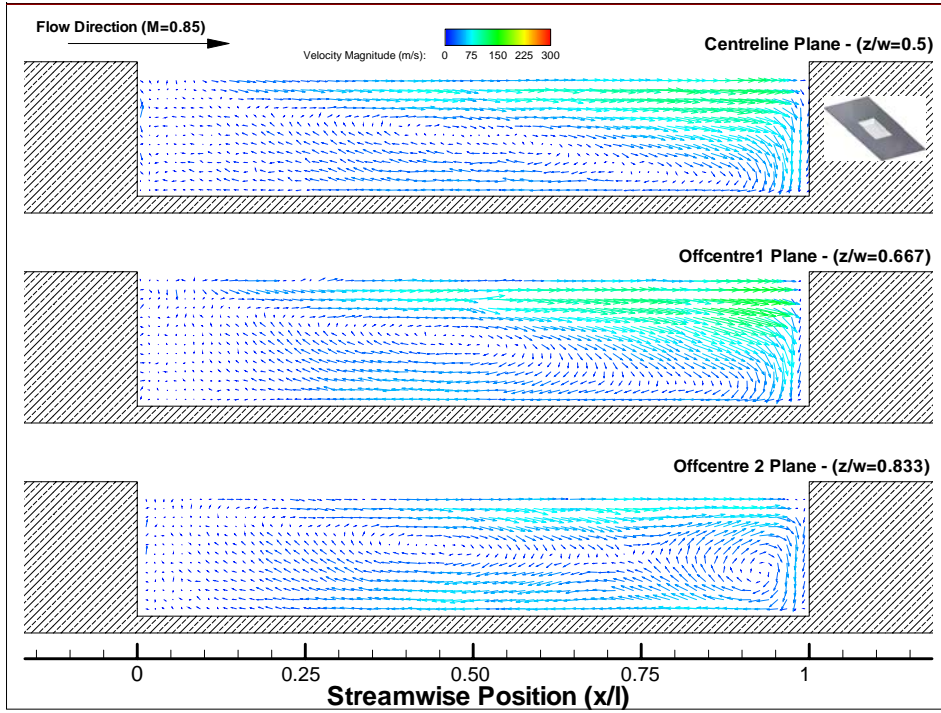


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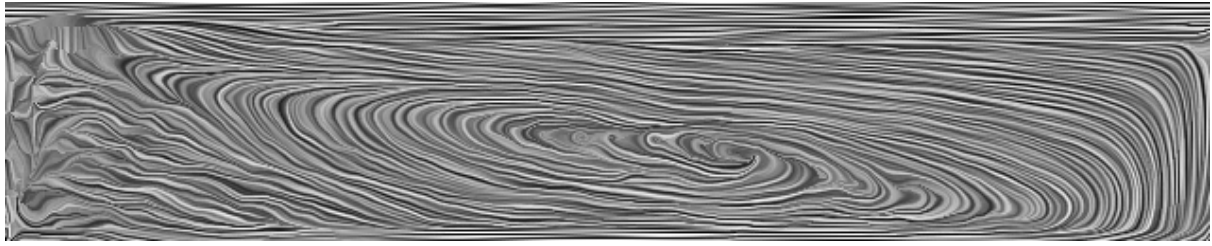


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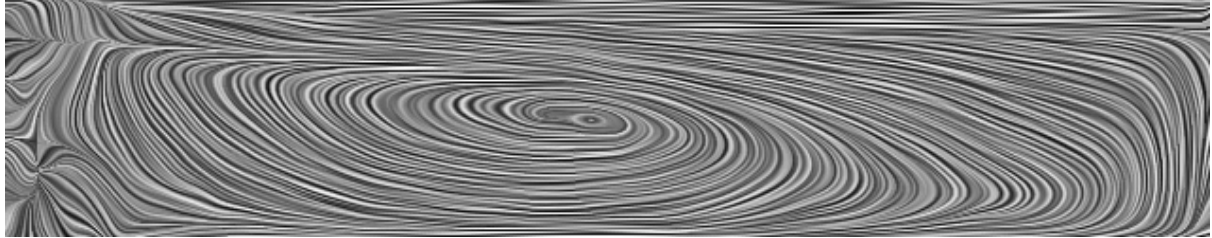
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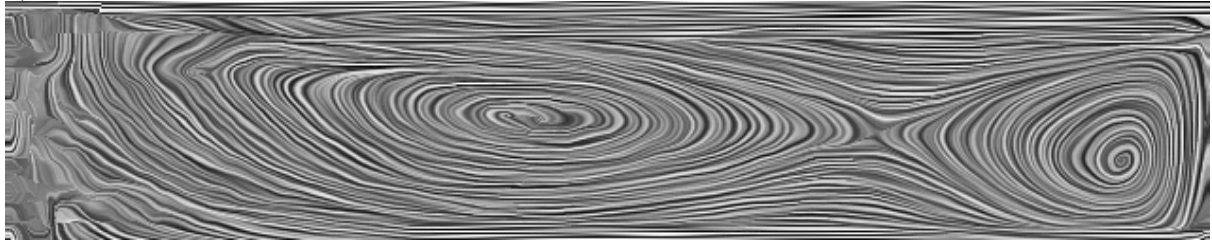
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a)

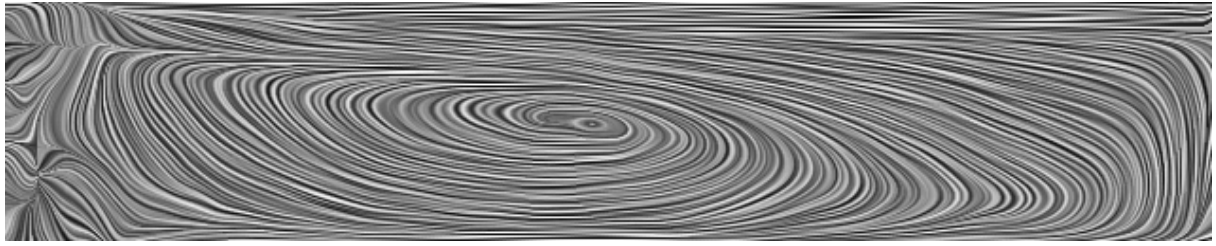


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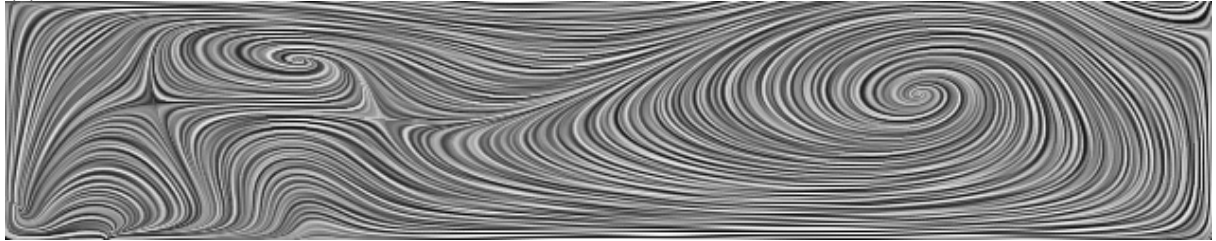


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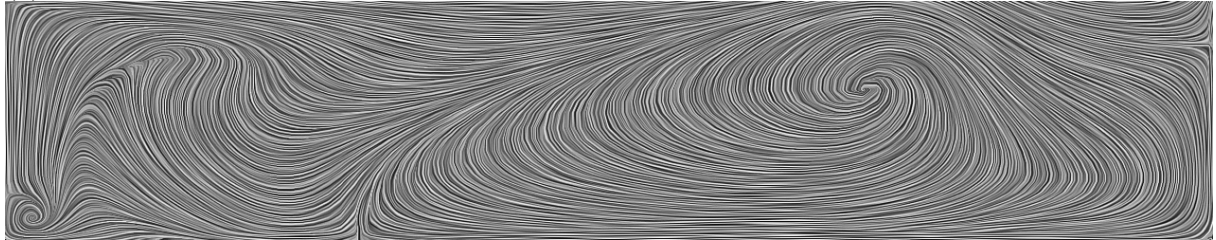
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(a)



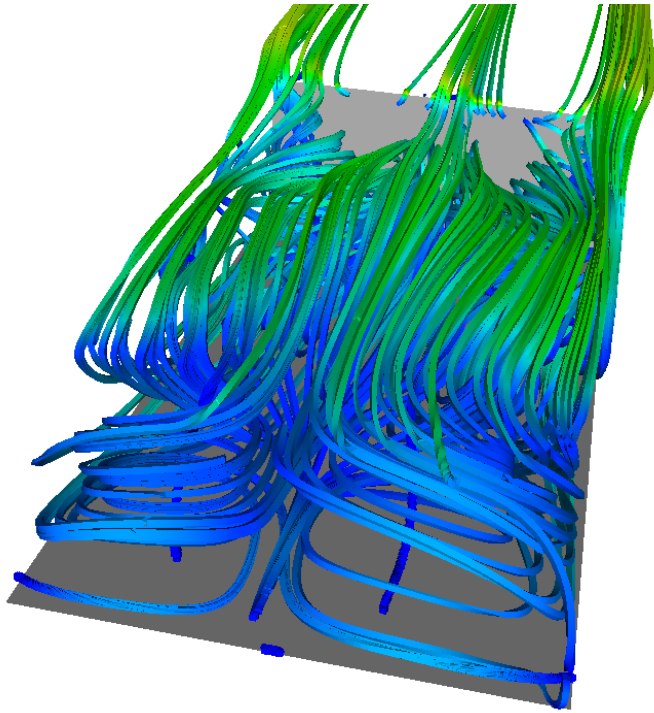
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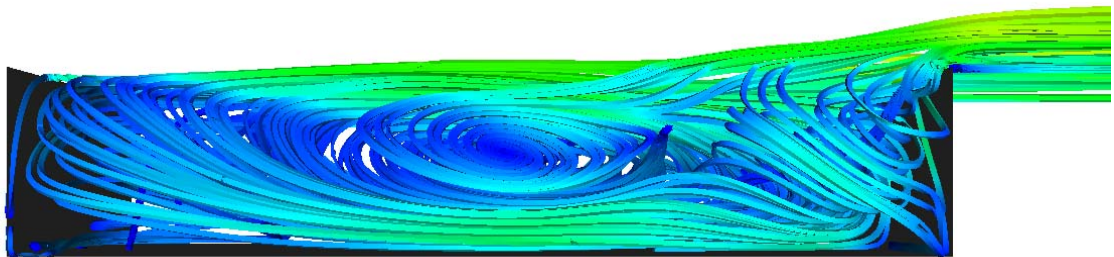
(c)

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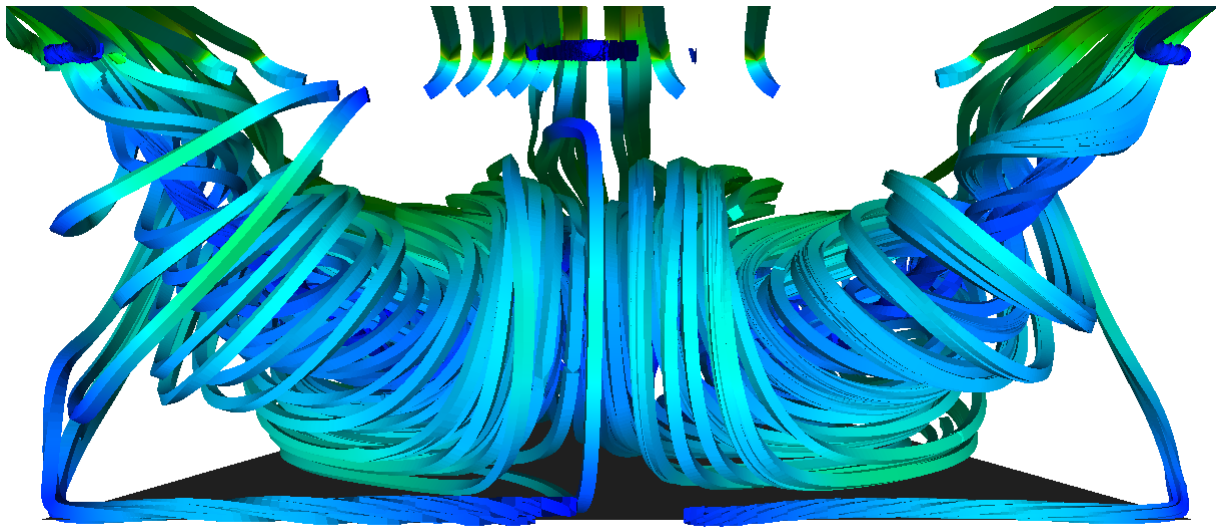




a)

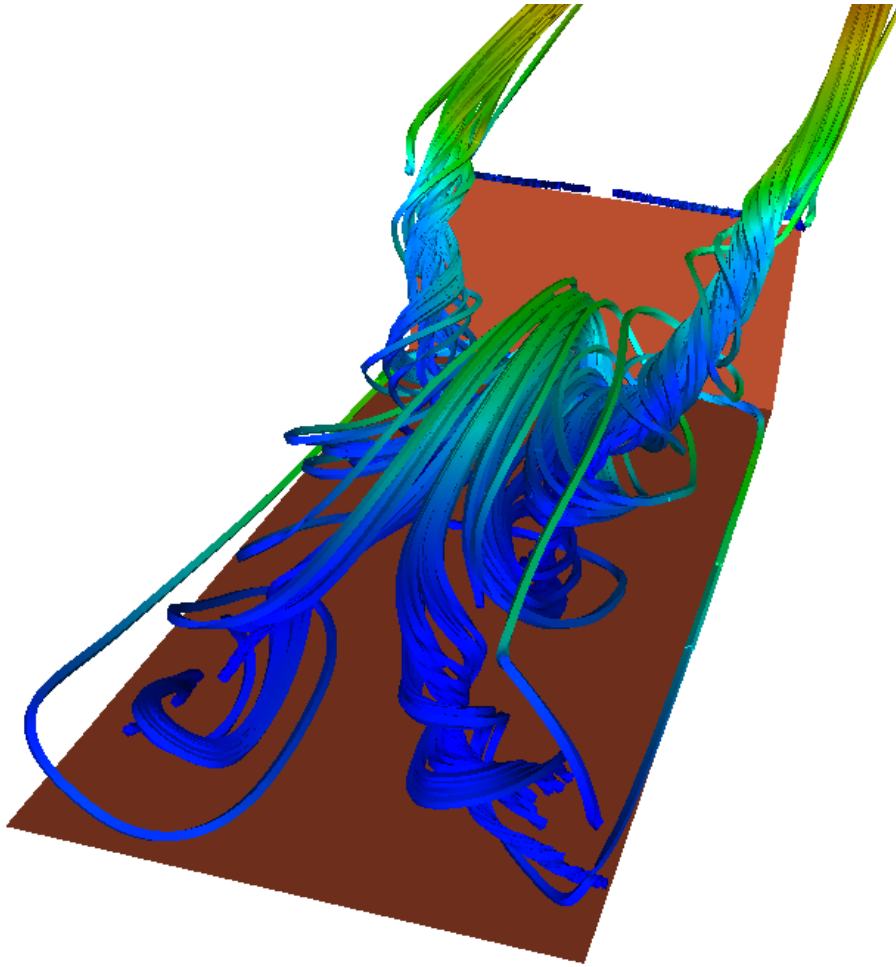


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