

1 **A review of uncertainty in environmental risk: characterising potential natures,**  
2 **locations, and levels.**

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4 Daniel JC Skinner<sup>a</sup>, Sophie A Rocks<sup>b\*</sup> and Simon JT Pollard<sup>c</sup>

5 Cranfield University, Collaborative Centre of Excellence in Understanding and Managing  
6 Natural and Environmental Risks, Cranfield, Bedfordshire, MK43 0AL, UK.

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8 \* Corresponding author

9 <sup>a</sup> tel: +44 1234 750111 x2534 email: d.j.skinner@cranfield.ac.uk

10 <sup>b</sup> tel: +44 1234 750111 x2370 email: s.rocks@cranfield.ac.uk

11 <sup>c</sup> tel: +44 1234 754101 email: s.pollard@cranfield.ac.uk

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26 **Abstract**

27           Uncertainties, whether due to randomness or human or system errors, are inherent  
28 within any decision process. In order to improve the clarity and robustness of risk estimates  
29 and risk characterisations, environmental risk assessments (ERAs) should explicitly consider  
30 uncertainty. Typologies of uncertainty can help practitioners to understand and identify  
31 potential types of uncertainty within ERAs, but these tools have yet to be reviewed in earnest.  
32 Here we have systematically reviewed 30 distinct typologies and the uncertainties they  
33 communicate, and demonstrate that they: (i) use terminology that is often contradictory; (ii)  
34 differ in the frequencies and dimensions of uncertainties that they include; (iii) do not  
35 uniformly use systematic and robust methods to source information; and (iv) cannot be  
36 applied, on an individual basis, to the domain of ERA. On the basis of these observations we  
37 created a summary typology – consisting of seven locations (areas of occurrence) of  
38 uncertainty across five distinct levels (magnitude of uncertainty) – specifically for use with  
39 ERAs. This work highlights the potential for confusion given the many versions of  
40 uncertainty typologies which exist for closely related risk domains and, through the summary  
41 typology, provides environmental risk analysts with information to form a solid foundation  
42 for uncertainty analysis (based on improved understanding) to identify uncertainties within an  
43 ERA.

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50 **Keywords:** uncertainty, typology, environmental, risk, assessment



76 expert judgement (Knol *et al.* 2009), that their successful implementation can depend on the  
77 skill and experience of the end-user (Gillund *et al.* 2008), and that no typology exists which  
78 "includes all of its meanings in a way that is clear, simple, and adequate for each potential use  
79 of such a typology" (Petersen 2006). However, the full extent of these problems and their  
80 potential impacts are not clear.

81         Significantly, uncertainty is interpreted differently by different people (Refsgaard *et*  
82 *al* 2007; Troldborg 2010). For example, protection and regulatory agencies often adopt brief  
83 high-level explanations (Fairman *et al.* 1998; US EPA 1998; DEFRA 2011). In reality,  
84 uncertainty is complex and in many cases the full concept is difficult to communicate or  
85 condense into one or two sentences. Early research into uncertainty focussed on  
86 characterising the physical flaws in acquiring experimental data (Veseley and Rasmuson  
87 1984; Henrion and Fischhoff 1986; Alcamo and Bartnicki 1987; Beck 1987). More recently,  
88 uncertainty has been investigated through its constituent dimensions (Walker *et al.* 2003),  
89 namely its: *nature*, describing how the uncertainty has come to exist, either due to the  
90 incompleteness of knowledge or the inherent variability of natural systems; *location*, where  
91 the uncertainty is manifest in the system of interest, for example in the data being recorded,  
92 the models utilised, or the decisions taken; and *level*, representing the significance of the  
93 uncertainty, ranging from deterministic understanding of the uncertainty at one end of the  
94 spectrum (a low level of uncertainty) to ignorance at the other end (a high level of  
95 uncertainty). If the different types of uncertainty within each dimension were understood by  
96 risk analysts it would then be more likely that they would be identified in applied scenarios.  
97 Uncertainty typologies are integral to this process.

98         In researching this topic, we note that many risk assessments fail to address  
99 uncertainty at all, which does undermine the quality of these assessments and the confidence  
100 placed in risk estimates. A robust uncertainty typology (non-domain specific) may help to

101 address this oversight. Therefore there is a need to review and analyse the typologies  
102 available to environmental risk analysts, in order to ascertain whether they are comprehensive  
103 and applicable, and if not, to highlight the ways in which they could be improved.

104

## 105 **2. Review considerations and methodology**

106 When uncertainty typologies are used to aid uncertainty understanding and  
107 identification, some risk analysts use a single typology, but it is more likely that several will  
108 be used (van Asselt and Rotmans 2002). Whilst individual typologies should be  
109 comprehensive, ideally when combined the typologies should also be consistent in definition  
110 and identification. In order to examine the uncertainty typologies, we have systematically  
111 reviewed distinct versions – individually and as a group – and the uncertainties they  
112 communicate across a range of environmental risk domains, including integrated modelling,  
113 human and ecological risk assessment, and policy analysis. In doing so, we have: (i) explored  
114 the intra and inter-typology conflicts; (ii) examined their applicability to ERAs, drawing from  
115 uncertainties identified within existing assessments; (iii) provided a summary typology for  
116 use with ERAs and (iv) provided suggestions for ways in which we may be able to move  
117 uncertainty typologies, and therefore uncertainty analysis, forward.

118 We identified 30 uncertainty typologies (Table 1) that are either based in the domain  
119 of ‘environmental risk’ or that make reference to it. The typologies were published in peer-  
120 reviewed articles or books and were sourced using online academic search engines. A  
121 thorough check of the references provided by each source was also performed, which ensured  
122 the identification of relevant typologies not identified in the initial search. Some sources are  
123 not specifically labelled as typologies by their authors whilst others are presented as original  
124 typologies that are explained and justified in full. Unlabelled typologies were included in this  
125 research if it was believed that they played the role of a typology – e.g. provided systematic

126 classification of types that have characteristics or traits in common. All relevant typologies  
127 have been included in this review article, to the best of the researchers' knowledge. Each  
128 typology was analysed for the types of uncertainties contained within it, the number of  
129 dimensions communicated, and their applicability to ERAs.

130 [TABLE 1 NEAR HERE]

### 131 **3. Uncertainties communicated by existing typologies**

#### 132 ***3.1 The nature, location, and level of uncertainty in context***

133 The nature of the uncertainty, which describes how the uncertainty has come to exist,  
134 dictates the degree to which it can be managed; knowledge-based (epistemic) uncertainties  
135 can be quantified, reduced, and potentially removed, whilst it may only be possible to  
136 quantify those uncertainties which are inherently random (known as aleatory). Separately, the  
137 location of the uncertainty, where the uncertainty occurs within an assessment, must be  
138 known to implement a management action. Finally, the level (or magnitude) of the  
139 uncertainty will inform the selection of the most appropriate management technique  
140 (Refsgaard *et al.* 2007). Therefore, in order to effectively manage uncertainty, it is essential  
141 that all dimensions are considered (Walker *et al.* 2003; Janssen *et al.* 2003; Refsgaard *et al.*  
142 2007; Knol *et al.* 2009). The uncertainties that the 30 selected typologies communicate are  
143 described in the remainder of this section, and are organised according to these three  
144 dimensions of uncertainty with definitions and examples selected from the evidence base.

145

#### 146 ***3.2 Nature of uncertainty***

##### 147 ***3.2.1 Aleatory uncertainty***

148 Aleatory uncertainty (Bedford and Cooke 2001; Ascough II *et al.* 2008) represents the  
149 inherent randomness displayed in human and natural systems. It is also referred to as physical  
150 (Vesely and Rasmuson 1984), stochastic (Helton 1994), variability (Hoffman and Hammonds

151 1994; Janssen *et al.* 2003; Walker *et al.* 2003; Hayes 2006), random (Bevington and  
152 Robinson 2002; Regan *et al.* 2002), or ontic (Petersen 2006; Knol *et al.* 2009). Aleatory  
153 uncertainty cannot be reduced, although additional research may help to better understand the  
154 complexities of the system(s) of interest. Whilst such systems may actually be chaotic (i.e.  
155 epistemic) rather than random (i.e. aleatory; and are therefore in principle understandable;  
156 Regan *et al.* 2002), many risk analysts find it useful to treat the associated uncertainties as if  
157 they are random, primarily employing stochastic numerical techniques to quantify  
158 uncertainty. In mimicking nature, stochastic methods can produce results that are consistently  
159 more representative than their non-random counterparts (Hromkovic 2005), adding real value  
160 to the ERA process.

161

### 162 *3.2.2 Epistemic uncertainty*

163 Epistemic uncertainty (Bedford and Cooke 2001; Walker *et al.* 2003; Petersen 2006;  
164 Ascough II *et al.* 2008; Knol *et al.* 2009) is the imperfection of knowledge concerning a  
165 system of interest. Epistemic uncertainty is also termed completeness (Vesely and Rasmuson  
166 1984; Rowe 1994), subjective (Helton 1994), knowledge-based (Hoffman and Hammonds  
167 1994; Janssen *et al.* 2003), or systematic (Bevington and Robinson 2002). In contrast to  
168 aleatory uncertainty, epistemic uncertainty can be quantified, reduced, and possibly  
169 eliminated, depending on the specific situation. However, additional information gathered to  
170 reduce uncertainty may instead reveal our true lack of knowledge thereby increasing the  
171 associated uncertainty (Janssen *et al.* 2003; van der Keur 2008).

172

### 173 *3.2.3 Nature of uncertainty in environmental risk assessments*

174 It can be difficult to distinguish between epistemic and aleatory uncertainty in applied  
175 ERAs, since the dividing line can be blurred by problem-specific features and the current

176 level of subject knowledge (Janssen *et al.* 2003). This is important as it is increasingly  
177 recognised that (epistemic) uncertainty and (aleatory) variability need to be treated separately  
178 (Li *et al.* 2008; Kumar *et al.* 2009; Qin and Huang 2009), due to the differing degrees to  
179 which they can be managed.

180           Whether epistemic or aleatory, all uncertainties must also be considered in terms of  
181 their two other dimensions.

182

### 183 **3.3 Location of uncertainty**

#### 184 **3.3.1 System**

185           This refers to the causes, processes, and effects within the investigated systems (or  
186 environment, identified prior to, or at the beginning of, the risk assessment). One or more  
187 conceptual models of a system should be developed in the initial stages of an ERA to help to  
188 identify the attributes that are unique to that system, (Defra 2011). In the conceptual model  
189 the analyst(s) must set boundaries that force the inclusion and exclusion of important  
190 features, potentially affecting the completeness of the assessment (Walker *et al.* 2003;  
191 Janssen *et al.* 2003). Within this process, problems can result from a lack of understanding  
192 about the system of interest (Rowe 1994) or, in some cases, from too much information  
193 leading to multiple frames of reference being used to understand a phenomenon (Dewulf *et*  
194 *al.* 2005). The associated uncertainties are termed contextual (Walker *et al.* 2003; Janssen *et*  
195 *al.* 2003; when the issue is ill-defined), conceptual (Rowe 1994; analysis of the issue),  
196 ambiguity (Dewulf *et al.* 2005; inexactness of data), and process (Ascough II *et al.* 2008).  
197 From either position (too much or too little information), the uncertainties reflect the limits of  
198 scientific understanding about the risk. Generally, where understanding is low, uncertainty  
199 will be high and vice-versa. System uncertainty can therefore impact ERAs wherever  
200 understanding is lacking. However, a field which develops rapidly, such as nanotechnology,



201 can contain high levels of knowledge as well as system-related uncertainties, due largely to  
202 the unknowns associated with novel technologies. For example, the contribution of physical  
203 structure to a nanoparticle's toxicity (i.e. effect) may only be partly understood, whilst its  
204 relevance (i.e. exposure) to different receptors of interest may simply be unknown. (Zalk *et*  
205 *al.* 2009). Such system uncertainties can therefore impact the exposure and effects phases of  
206 ERAs.

207

### 208 3.3.2 Data

209 Whether empirical or experimental, all data carries a level of inherent confidence  
210 associated with its correctness. According to Morgan and Henrion (1990), the most common  
211 data uncertainty concerns errors in direct measurements. This type of uncertainty, either  
212 termed statistical (Morgan and Henrion 1990; Finkel 1990), random (Henrion and Fischhoff  
213 1986), or measurement (Regan *et al.* 2002), refers to the variation across multiple  
214 measurements of the same quantity. All measurable empirical quantities potentially contain  
215 this uncertainty (Morgan and Henrion 1990). The magnitude of this uncertainty can be  
216 quantified through statistical testing of the unexplained variation in measurements (Henrion  
217 and Fischhoff 1986).

218 Systematic uncertainty (Henrion and Fischhoff 1986; Finkel 1990; Morgan and  
219 Henrion 1990; Regan *et al.* 2002) is the difference between the true value of an item and the  
220 value to which the mean of the measurements converge as the sample size increases (Morgan  
221 and Henrion 1990; Regan *et al.* 2002), and can be much harder to quantify. This type of  
222 uncertainty is addressed by detecting errors in the experimental procedure, and generated  
223 data, and attempting to eliminate them. Separate data concerns arise from the analysis and  
224 interpretation of data (Regan *et al.* 2002; Maier *et al.* 2008), and from incomplete or  
225 unavailable data records (Maier *et al.* 2008).

226 In the context of ERAs, data uncertainties are most common in the analysis phase,  
227 where original experimental data is primarily used. For example, McColl *et al.* (2000) discuss  
228 the effect that a limited or erroneous data record can have when determining the dose-  
229 response levels for use in a contaminated site assessment, which may then be adopted in other  
230 assessments, potentially in different disciplines. The data uncertainties discussed should be  
231 managed because they directly impact on estimates of risk and, by extension, the quality of  
232 environmental decision-making (Faucheux and Froger 1995).

233

### 234 3.3.3 Model

235 Modelling, in the form of numerical or computational simulation, can be used to  
236 understand processes and provide evidence to support decision-making (Arhonditsis *et al.*  
237 2007). The associated procedures routinely involve an initial conceptualisation stage (see  
238 Section 3.3.1), which is developed into a numerical and/or computational representation of  
239 the system under study (Stephens *et al.* 1993). Modelling relies heavily on data, primarily for  
240 input and validation purposes.

241 Parameter uncertainty (Alcamo and Bartnicki 1987; Beck 1987; Morgan and Henrion  
242 1990; Bedford and Cooke 2001; Huijbregts *et al.* 2001; Janssen *et al.* 2003; Walker *et al.*  
243 2003; Maier *et al.* 2008; Ascough II *et al.* 2008) is a reflection of the uncertainties associated  
244 with the data used to develop the model (see Section 3.3.2). The parameters are the unvarying  
245 constants within a model and may be exact (e.g.  $\pi$ ), fixed (e.g. the gravitational constant  $g$ ),  
246 measured *a priori*, or derived through calibration (Walker *et al.* 2003; Kraymer von Kraus  
247 2005). The data are collected from different locations, over different scales and time spans  
248 than the required input variables and parameters (Troldborg 2010), requiring the interpolation  
249 between and/or extrapolation beyond known values.

250 Computational and numerical models are simplified versions of real-world  
251 phenomena (Ascough II *et al.* 2008) and as such will include different uncertainties  
252 associated with their representativeness. These are termed model structure uncertainty  
253 (Alcamo and Bartnicki 1987; Beck 1987; Janssen *et al.* 2003; Walker *et al.* 2003), model  
254 uncertainty (Finkel 1990; Bedford and Cooke 2001, Huijbregts *et al.* 2001; Regan *et al.*  
255 2002) or method uncertainty (Maier *et al.* 2008). These uncertainties may concern: the  
256 physical relationships between the variables and parameters used in the model (Ascough II *et*  
257 *al.* 2008; Knol *et al.* 2009); the interpretation of observations and theories and their  
258 subsequent implementation (Regan *et al.* 2002); approximations in numerical solution (van  
259 der Sluijs 1997); and the initial conceptual plans adopted (Alcamo and Bartnicki 1987; see  
260 Section 3.3.1). If a conceptual model presents an oversimplification of the scenario, the  
261 resulting numerical/computational model may fail to capture essential features, leading in  
262 turn to inadequate simulations. Conversely an undersimplification may yield a model that is  
263 too complex, and therefore expensive (or even prohibitive) to build and execute (El-  
264 Ghonemy *et al.* 2005).

265 The technical aspects of computational modelling, also contain uncertainties related to  
266 the software and hardware used (Rowe 1994; van der Sluijs 1997; Janssen *et al.* 2003;  
267 Walker *et al.* 2003; Ascough II *et al.* 2008). Software uncertainties arise from issues  
268 including errors in developer and operational platforms, poorly-designed algorithms, and  
269 mistakes in code (Walker *et al.* 2003). Hardware uncertainties arise, quite simply, from errors  
270 in the hardware, including processors, memory and storage devices (van der Sluijs 1997).

271 The parameter, structural, and technical uncertainties discussed all occur within  
272 models of physical systems and can limit their operational capability, ultimately leading to  
273 uncertainty in their output (Walker *et al.* 2003, Janssen *et al.* 2003; Ascough II *et al.* 2008).  
274 Even those models that are good representations of the real-world and provide consistently

275 accurate results can never be completely exact.. Identifying and managing related  
276 uncertainties helps to ensure that the margin of model error is kept to a minimum.

277         Within ERAs, model uncertainties should be considered wherever numerical or  
278 computational models are used, which is principally during the analysis phase. For example,  
279 ApSimon *et al.* (2002) describe the model uncertainty associated with modelling complex  
280 atmospheric processes, such as particle deposition, within the exposure phase of a trans-  
281 boundary air pollution ERA. Furthermore, the output from the modelling process, which may  
282 be used to help formulate risk estimates, should be treated with due caution at the risk  
283 characterisation stage.

284

#### 285 3.3.4 Human

286         Human uncertainties within ERAs are the unintentional, but potentially avoidable,  
287 human flaws that are not covered by system knowledge, models, and data uncertainties. The  
288 human uncertainties are generally more qualitative, reflective, and interpretive (Janssen *et al.*  
289 2003). These include conflicts between individuals and/or small groups (disagreement  
290 uncertainty; Morgan and Henrion 1990), varying perspectives and values that are not easily  
291 reconciled (value diversity; Rowe 1994; van Asselt and Rotmans 2002), or the perceived  
292 societal importance of an individual, elevating their views above those of others (stakeholder  
293 uncertainty; Maier *et al.* 2008).

294         Human uncertainties can exist at any stage of ERAs, from unintentionally subjective  
295 actions at the problem formulation phase to stakeholder disagreements concerning tolerability  
296 thresholds during risk characterisation or evaluation. For example, in a multi-criteria  
297 approach for prioritising sites in sediment management Alvarez-Guerra *et al.* (2009) account  
298 for the unintentionally biased opinions, brought about by past experiences, when assigning

299 weightings to different criteria. Human-based uncertainties are also strongly linked to the  
300 way in which we use language to communicate.

301

### 302 3.3.5 Language

303 Language uncertainties relate to how information is communicated. The uncertainties  
304 associated with language arise for a number of reasons, but stem primarily from a lack of  
305 clarity (Morgan and Henrion 1990). Language can be controlled; therefore, theoretically, the  
306 associated uncertainties can be eliminated. Linguistic variables may be: ambiguous (Bedford  
307 and Cooke 2001; Regan *et al.* 2002; Ascough II *et al.* 2008), where more than one meaning  
308 can be drawn and it is not clear which meaning is intended; underspecific (Regan *et al.* 2002;  
309 Ascough II *et al.* 2008), where terms do not provide the level of precision required; or vague  
310 (Regan *et al.* 2002; Ascough II *et al.* 2008), where there is a blurring of distinctions between  
311 terms. The use of a single field-specific term may carry these three linguistic uncertainties  
312 (Acosta *et al.* 2010). In addition to these, two further linguistic uncertainties have been  
313 suggested: context dependence (Regan *et al.* 2002), where there is a failure to properly  
314 convey the context in which a term is to be understood; and indeterminacy of linguistic terms  
315 (Regan *et al.* 2002), encompassing unknown future developments of languages and the  
316 resulting effects on incorporated terms.

317 Language, in the context of ERAs, is not phase-specific. As such, the associated  
318 uncertainties should exist in many locations throughout the process, from basic definitions to  
319 the communication of risk levels (Keiter *et al.* 2009). For example, language uncertainties  
320 exist within the expert elicitation exercises that are often used for information gathering,  
321 evidence-checking, or results validation (Acosta *et al.* 2010).

322

### 323 3.3.6 Variability

324 Variability uncertainty is concerned with the randomness within systems. Human  
325 variability (Rowe 1994; van Asselt and Rotmans 2002), the opposite of the controllable  
326 human uncertainties (see Section 3.3.4), occurs from intentionally biased and subjective  
327 human actions (Khan *et al.* 2002), which, from the viewpoint of the risk analyst, are  
328 uncontrollable. Humans invariably display bias when they have something to gain, and  
329 display subjectivity when they believe their own views to be more correct than those of  
330 others (Chen *et al.* 2007). Human variability can be exhibited by those with close links to  
331 ERAs (e.g. decision-makers, stakeholders, and scientists), as well as those with a lower  
332 vested interest (e.g. short-term employees such as laboratory technicians or computer  
333 modellers; Croke *et al.* 2007).

334 Conversely, natural randomness may be considered unexpected but free from  
335 intentional bias (Jørgensen *et al.* 2009). The associated uncertainty, termed natural variability  
336 (Finkel 1990; Rowe 1994; van Asselt and Rotmans 2002; Huijbregts *et al.* 2001; Regan *et al.*  
337 2002; Ascough II *et al.* 2008) relates to the unpredictable quality of natural processes  
338 (Ascough II *et al.* 2008; Regan *et al.* 2002), which can vary across both spatial and temporal  
339 scales (Rowe 1994; Huijbregts *et al.* 2001; Regan *et al.* 2002). Since natural variability is  
340 intrinsic to nature, it is also intrinsic to the corresponding aspects within ERAs; from factors  
341 affecting the fate and transport of a stressor in exposure assessment (Schwartz *et al.* 2000),  
342 the difference in responses shown by receptors of the same species during effects assessment  
343 (Borsuk *et al.* 2006), to the variability in determining appropriate tolerance thresholds in risk  
344 characterisation (Chen and Ma 2007).

345 Two further categories of variability are also identified from the evidence base.  
346 Technological variability (van Asselt and Rotmans 2002; Ascough II *et al.* 2008) refers to  
347 unexpected issues that result from technological developments. Institutional variability  
348 (Funtowicz and Ravetz 1990; van Asselt and Rotmans 2002; Ascough II *et al.* 2008) is where

349 human variability is exhibited throughout large groups (e.g. societies), and includes aspects  
350 such as social values, economic principles, and cultural dynamics (van Asselt and Rotmans  
351 2002). With respect to ERAs, technological variability can occur wherever such systems are  
352 in place, and institutional variability is most likely to exist in assessments at the community  
353 or population scale (e.g. epidemiological studies).

354

### 355 *3.3.7 Decision*

356 Decision uncertainty (Finkel 1990; Ascough II *et al.* 2008), also termed volitional  
357 (Bedford and Cooke 2001) or choice-laden uncertainty (Huijbregts *et al.* 2001), exists when  
358 there is doubt about the optimal course of action. This often occurs where there are differing  
359 objectives (Finkel 1990). These uncertainties exist within the ERA process, principally at the  
360 risk characterisation phase, but also in a wider risk management context. For example,  
361 management of ecological and environmental resources requires decision-makers to evaluate  
362 multiple and often conflicting strategies, whilst balancing objectives of productivity and  
363 sustainability (Ducey and Larson 1999). Such decisions can also contain any or all of the  
364 other outlined uncertainties (Ascough II *et al.* 2008).

365

### 366 *3.3.8 Location of uncertainty in environmental risk assessments*

367 The location in which uncertainty manifests depends on the different aspects of the  
368 system being explored. For example, an ERA of a novel technology (e.g. engineered  
369 nanomaterials) in an open, natural, environment can potentially contain all of the wide range  
370 of uncertainties discussed above. In cases where certain aspects do not feature, such as  
371 modelling processes, the related uncertainties will not be an issue. However, whilst  
372 uncertainties can manifest individually several are likely to exist, meaning that the full range  
373 should be considered (Refsgaard *et al.* 2007).

374 In addition to the nature and location, one further dimension must be considered,  
375 which is discussed in the following sub-section.

376

### 377 ***3.4 Level of uncertainty***

#### 378 *3.4.1 Assessing the level of uncertainty*

379 Humans exhibit a variety of distinct levels of knowledge, ranging from determinism  
380 (perfect knowledge) to indeterminacy (lack of knowledge; Wynne 1992). The further we  
381 move from a deterministic understanding of a system, the more severe the uncertainty  
382 becomes (Walker *et al.* 2003; Figure 2). The level of uncertainty is specifically described  
383 according to two factors, namely the degree of confidence attached to the likelihood of an  
384 event occurring and the degree of confidence attached to the severity of the potential  
385 outcomes (Wynne 1992; Stirling 1999). These metrics are used to convey the level of  
386 understanding and the level of the associated uncertainty.

387 [FIGURE 2 NEAR HERE]

#### 388 *3.4.2 State 1: knowing a lot*

389 At the deterministic end of the spectrum (here termed state 1) the uncertainty is low.  
390 This state, first described by Funtowicz and Ravetz (1990; and later by van der Sluijs 1997  
391 and van Asselt and Rotmans 2002) as inexactness, refers to the specified events for which we  
392 “roughly know” the likelihoods and outcomes, and where significant digits and error bars are  
393 the representations of choice (Funtowicz and Ravetz 1990). Due to the applicability of  
394 common risk assessment tools (e.g. frequency distributions) in addressing this level of  
395 uncertainty, the term risk has also been applied (Wynne 1992; Stirling 1999). Other proposed  
396 terms include probabilistic (Beer 2006), statistical (Brouwer and Blois 2008; Knol *et al.*  
397 2009) and certainty (Faucheux and Froger 1995).

398

#### 399 *3.4.3 State 2: knowing the probabilities*



400           After deterministic understanding, we come to the state where we can confidently  
401 assign probabilities to events but have little understanding of the ramifications of the events  
402 (state 2). Termed ambiguity (Stirling 1999), conflicting evidence (van Asselt and Rotmans  
403 2002), statistical (Walker *et al.* 2003; Janssen *et al.* 2003; Petersen 2006), incertitude (Beer  
404 2006), or qualitative (Brouwer and Blois 2008), this level of uncertainty refers to a situation  
405 in which “we don’t know what we know” (van Asselt and Rotmans 2002). Statistical  
406 measures can be used to constrain likelihoods (i.e. probability distributions; Janssen *et al.*  
407 2003) with techniques such as sensitivity analysis and fuzzy logic used to better understand  
408 the outcomes (Stirling 1999).

409

#### 410 *3.4.4 State 3: knowing the outcomes*

411           The third level of uncertainty is where there is confidence about the outcomes but not  
412 likelihoods of an event (i.e. the reverse of state 2). Termed unreliability (Funtowicz and  
413 Ravetz 1990; van der Sluijs 1997), uncertainty (Wynne 1992; Stirling 1999), practically  
414 immeasurable (van Asselt and Rotmans 1999), or ambiguity (Beer 2006), it refers to the  
415 position in which “we know what we do not know” (van Asselt and Rotmans 1999). The term  
416 scenario is also used when referring to this state (Walker *et al.* 2003; Janssen *et al.* 2003;  
417 Brouwer and Blois 2008; Knol *et al.* 2009), because of a reliance on the analysis of scenarios  
418 when attempting to resolve unknown probabilities.

419

#### 420 *3.4.5 State 4: knowing a little*

421           If it is not possible to define probabilities or a complete set of outcomes, we move  
422 into a state of ignorance (state 4; Wynne 1992; Faucheux and Froger 1995; Stirling 1999; van  
423 Asselt and Rotmans 2002; Brown 2004; Beer 2006), and it becomes necessary to proceed  
424 with due caution (Stirling 1999). The terms borderline ignorance (Funtowicz and Ravetz

425 1990; van der Sluijs 1997) and recognised ignorance (Walker *et al.* 2003; Janssen *et al.* 2003;  
426 Brouwer and Blois 2008; Knol *et al.* 2009) are also used, since, by definition, “we cannot say  
427 anything useful about that of which we are ignorant”. The ideal solution is to increase  
428 knowledge of the problem, thus reducing uncertainty, and move back towards determinism  
429 (Walker *et al.* 2003).

430

### 431 *3.4.6 State 5: not knowing*

432 The inverse of deterministic knowledge is indeterminacy (state 5; Wynne 1992; van  
433 Asselt and Rotmans 2002; Brown 2004), the most important form of uncertainty since it is  
434 the uncertainty of which we know nothing and to which we are completely ignorant (Walker  
435 *et al.* 2003). Only when an event occurs will we be in a position to observe its origins and  
436 effects, and move ourselves into a state of awareness.

437

### 438 *3.4.7 Level of uncertainty in environmental risk assessments*

439 Determining the level of uncertainty helps to focus attention toward the features of  
440 ERAs that are most uncertain, and, when approached with the nature and location, allows  
441 selection of the most appropriate managing tool(s). Resolving the level also allows the  
442 uncertainty to be described in an appropriate manner. For example, using statistical measures  
443 to describe uncertainties closest to the indeterminacy end of the spectrum is inappropriate  
444 because we know nothing of the associated statistical distributions (Kraye von Krauss 2005).

445 Uncertainty typologies should be analysed for the presence of the three dimensions  
446 (location, nature, level), since they strongly influence uncertainty management, as well as for  
447 the definitions and frequencies of the uncertainties that they communicate.

448

## 449 **4. Analysis of existing uncertainty typologies**

450 **4.1 Comparison of uncertainty terms used**

451 Contradictions between terms used in different uncertainty typologies can cause  
452 confusion and, if definitions are inappropriate, potentially lead to management issues.  
453 Contradictions either exist where one term is used for a range of different uncertainties (the  
454 same term has multiple definitions; Table 2), or where several distinct terms are used to  
455 describe the same uncertainty (different terms have the same definition; Table 3). We have  
456 identified a number of different discrepancies between the 30 uncertainty typologies.

457 [TABLE 2 NEAR HERE]

458 [TABLE 3 NEAR HERE]

459 When the level of the uncertainty is described, the term ‘statistical’ is used to  
460 represent both the state of determinism (state 1; Brouwer and Blois 2008; Knol *et al.* 2009)  
461 and the state in which probabilities can be defined but outcomes remain unclear (state 2;  
462 Janssen *et al.* 2003; Walker *et al.* 2003; Petersen 2006; Table 2). Similarly, the term  
463 ‘ambiguity’ is used to refer to state 2 (Stirling 1999), and also state 3 where outcomes can be  
464 defined but associated probabilities remain unresolved (Beer 2006). Furthermore, Beer  
465 (2006) makes use of the term ‘incertitude’ to describe a single level of uncertainty (state 2),  
466 while Stirling (1999) uses the same term to describe the uncertainties across all levels.

467 The term ‘ambiguity’ is also used when describing the location in which the  
468 uncertainties occur, with specific reference to system-related uncertainty (Dewulf *et al.* 2005)  
469 and language-related uncertainty (Bedford and Cooke 2001; Regan *et al.* 2002; Ascough II *et*  
470 *al.* 2008). Indeed, within our data set this term was identified to have four separate meanings  
471 across the six typologies in which it features (see Table 2). Similarly, the term ‘statistical’ is  
472 also used to represent a form of data uncertainty (Morgan and Henrion 1990; Finkel 1990),  
473 resulting in three different definitions across seven typologies within our data set. Alternate

474 interpretations are also presented for the terms ‘indeterminacy’, ‘random’, ‘variability’, and  
475 ‘systematic’, with very different meanings attached to each.

476         There are similarities between the studied typologies. For example, ‘parameter  
477 uncertainty’ is listed by nine typologies out of the 30 identified, with all nine agreeing on its  
478 use. The uncertainty relating to the inherent variability of natural systems also has a single  
479 associated term, ‘natural variability’, which is adopted by five typologies. However, the use  
480 of competing terms to describe the same uncertainties is commonplace. Parameter and natural  
481 variability are the only terms in the selected typologies which are used consistently.  
482 Epistemic, used to describe knowledge-based failings, is used in five separate cases with  
483 another six competing terms used by eight other typologies, resulting in the use of seven  
484 terms over 13 typologies that describe the same type of uncertainty (Table 3). A similar  
485 pattern is observed for the terms associated with aleatory uncertainty, with six separate terms  
486 used across 14 typologies.

487         Of the 188 (non-distinct) uncertainties communicated by the 30 studied typologies, 98  
488 (52%) are contained within eight of the typologies (Rowe 1994; van Asselt and Rotmans  
489 2002; Walker *et al.* 2003; Janssen *et al.* 2003; Petersen 2006; Maier *et al.* 2008; Ascough II *et*  
490 *al.* 2008; Knol *et al.* 2009). Within these eight typologies, 14 terms (occurring 38 times out of  
491 98 recorded) are used to describe the same form of uncertainty in more than one typology.  
492 Therefore, there are 60 instances in which the terminology differs – either different terms are  
493 used to refer to the same uncertainty or the same terms are used to refer to different  
494 uncertainties. In either case, the terminology used in these eight main typologies differs 61%  
495 of the time, which may lead to confusion..

496

#### 497 ***4.2 Comparison of the number of types of uncertainties within typologies***



523 complete (in the context of this article) it should communicate all three dimensions (nature,  
524 location and level) effectively and in particular provide accurate descriptions of all relevant  
525 location-based uncertainties, which will allow practitioners to identify the specific issues in  
526 their own assessments. On this basis, only seven of the typologies identified in this work  
527 were considered to meet these criteria. However, six of the seven typologies that did consider  
528 the three dimensions did not include language-based uncertainties in their definitions, with  
529 the exception of Ascough II *et al.* (2008).

530

### 531 ***4.3 Comparison of evidence used to develop typologies***

532 Each of the 30 identified typologies that we investigated used a limited body of  
533 evidence which was sourced by expert elicitation, small scale literature review or a  
534 combination of research areas (Table 1). Most commonly, the views and opinions of a  
535 relatively small number of researchers were used to develop the typology, but this method  
536 can introduce additional uncertainties including subjectivity, intentional bias, and the ability  
537 of researcher(s) to communicate effectively. Secondly, small-scale literature reviews  
538 (compared to the available relevant body of evidence) were conducted across a relatively  
539 restricted topic. In such cases, the selection of inappropriate materials or a lack of quality  
540 sources may result in an incomplete typology. Furthermore, the content may only be  
541 applicable to the subject domain of the literature (e.g. atmospheric modelling, habitat  
542 conservation, or toxicology assessments), and may reduce the accuracy when applying the  
543 typology to other domains. Finally, existing typologies were combined from related but non-  
544 identical research domains. The most comprehensive and robust typology presented here  
545 (Ascough II *et al.* 2008, on the basis of the criteria laid out in this discussion) is sourced in  
546 this way. Whilst this ensures that a large body of relevant research is taken into consideration,  
547 the reliability of the output relies on the accuracy of the input. In this sense, combining

548 existing information can mean that shortcomings are transferred into the new typology which  
549 may impact on its use.

550

## 551 **5. Uncertainty in environmental risk assessments**

### 552 *5.1 Assessment of existing uncertainty typologies for environmental risk assessments*

553 The uncertainties discussed in this review have, through the use of examples, been  
554 shown to exist in published ERAs, yet it is not clear whether the compilers of the ERAs used  
555 uncertainty typologies to identify the uncertainties. The 30 identified typologies largely focus  
556 on specific aspects of the environmental management process, such as modelling, decision-  
557 making, or policy setting and do not cover all of the processes within an ERAs nor their  
558 associated uncertainties. Ten of the studied typologies are based in either ERA or  
559 environmental risk management (incorporating ERA). Of these ten, three provide extensive  
560 descriptions of potential uncertainties across all three dimensions (nature, location and level).  
561 However, of these three, two do not communicate language uncertainties (Janssen *et al.* 2003;  
562 Knol *et al.* 2009), and the other does not include a comprehensive description of modelling  
563 uncertainties (Regan *et al.* 2002). Therefore, we were not able to identify an individual  
564 typology which we believe depicts the full range of potential uncertainties within ERAs.

565

### 566 *5.2 A summary uncertainty typology for environmental risk assessments*

567 The current lack of a single comprehensive typology for ERAs suggests a significant  
568 knowledge gap in uncertainty analysis. Derived from the analysis in this review, we have  
569 integrated common attributes (identified from the 30 studied typologies) to represent the  
570 uncertainties that can occur within different parts of ERAs (Figure 3; see Section 3 for  
571 definitions and descriptions of the contained uncertainties and their relevance to the different  
572 phases of ERAs).

[FIGURE 3 NEAR HERE]

573

574         The summary typology (Figure 3) consists of two types of uncertainty within the  
575 nature dimension (epistemic and aleatory), seven main kinds of location-based uncertainty  
576 (system processes, data, model, human, language, variability, and decision), and five levels of  
577 uncertainty (determinacy, statistical, scenario, ignorance, and indeterminacy). The majority of  
578 the uncertainties within the typology are well understood however we have modified the  
579 inclusion and organisation of the categories and sub-categories to aid the identification of  
580 uncertainties. Language uncertainties, for example, are often treated as a standalone group  
581 (Morgan and Henrion 1990; Regan *et al.* 2002; Ascough II *et al.* 2008), but are here  
582 considered differently. Since language, and its use, is theoretically controllable, the related  
583 uncertainties are similar to others that are epistemic in nature. Whilst not always achievable,  
584 it is possible to quantify, reduce or remove the effect that language has on different aspects  
585 within ERAs, using techniques such as fuzzy logic (Acosta *et al.* 2010). Furthermore, since  
586 language can manifest in many functions and tasks across ERAs, the associated uncertainties  
587 can be labelled as specific location-based concerns.

588         The distinction between potential human uncertainties has not been made by a single  
589 typology. Within ERAs, human actions are either controllable or uncontrollable: the former  
590 must, by definition, belong to the epistemic set, whilst the latter must reside within the  
591 aleatory set. Within ERAs, human uncertainties are of concern only where there is human  
592 input or influence. They are not a continual concern, and need not be evaluated in the same  
593 manner as the nature or level of uncertainty. For these reasons, two types of location-based  
594 human uncertainty are considered within the summary typology, segregated by their different  
595 natures.

596         Within the aleatory uncertainties, the variability sub-set (in the nature dimension)  
597 identifies four potential locations of uncertainty that share the same irreducible variable



598 qualities: human; natural; institutional; and technological. It should be noted that these four  
599 locations could be considered direct subsets of the aleatory category, but that a grouping  
600 according to their common attribute of variability is also pertinent.

601 This presented summary typology has been developed from the outputs of the 30  
602 studied typologies and as such can aid uncertainty identification and characterisation in  
603 ERAs, but should be framed with the same caveats as discussed previously (in Section 4.3)  
604 concerning information sourcing. Further work should concentrate on the characterisation  
605 and identification of uncertainties within case studies to enable generic definitions and  
606 characteristics to be elucidated. The summary typology (Figure 3) and uncertainty  
607 descriptions (Section 3) provide analysts with a more complete understanding of uncertainty  
608 in ERAs than typically exists at present, potentially aiding the uncertainty identification  
609 process (Figure 1). Once identified, and depending on the mix of the three dimensions, the  
610 uncertainties can be managed using one (or more) of a number of existing uncertainty  
611 management techniques, ranging from Monte-Carlo simulation to uncertainty factors to  
612 adaptive management. Many articles discuss the appropriateness of such techniques with  
613 respect to different uncertainties (e.g. van der Sluijs *et al.* 2005; Refsgaard *et al.* 2007; Knol  
614 *et al.* 2009), a topic that is beyond the extent of this review. However, we are aware that  
615 much more could be done to improve both uncertainty typologies and the guidance related to  
616 their implementation, in the context of ERAs and uncertainty analysis in general.

617

## 618 **6. Identified knowledge gaps for uncertainty typologies**

### 619 ***6.1 Using the evidence base***

620 Basing the content of typologies on researcher views, small-scale literature reviews,  
621 or existing typologies has implicit problems, as previously discussed. There exists a large  
622 evidence base of peer-reviewed environmental risk-based research. A structured interrogation

623 of this evidence base, which spans a number of approaches (e.g. modelling, assessments, and  
624 management) and environmental concerns, would enable a more comprehensive  
625 characterisation of potential uncertainties. Specifically, the analysis of information from  
626 competing (but related) research domains will ensure that the full scope of uncertainties are  
627 identified. Additionally, such a typology would be able to point to individual occurrences  
628 within the evidence base, making it defensible and transparent.

629

## 630 ***6.2 Factors influencing uncertainty***

631 Extending the traditional typology format to include a system for direct identification  
632 of uncertainties would help to minimise any intentional or unintentional bias on the part of  
633 the analyst. By analysing the evidence base for any relationships that exist between identified  
634 uncertainties and other aspects (e.g. sources, pathways, receptors, the evidence utilised), key  
635 associations can be established and statistically evaluated through bivariate analysis. Strong  
636 relationships, if deemed to be transferrable, may then form the basis of such an identification  
637 system.

638

## 639 ***6.3 Structuring uncertainty typologies***

640 Uncertainty identification requires a level of subjectivity on the part of the practitioner  
641 – even when typologies are adopted – and can be further influenced by a lack of familiarity  
642 with concepts (Gillund *et al.* 2008). Structuring the typology for the risk domain in which it is  
643 intended to be used (e.g. ERA) may prove beneficial. Relating the unfamiliar abstract  
644 concepts of uncertainty to more familiar processes (e.g. within problem formulation,  
645 exposure/effects assessment, and risk characterisation) may make the typology more intuitive  
646 to analysts, making it more robust and ultimately more useful during uncertainty  
647 identification.

648

## 649 **7. Conclusion**

650           Uncertainty typologies should be well-defined, defensible, and, most importantly,  
651 accurate. This paper provides the first major review and analysis of these tools, which are  
652 integral to the identification of uncertainty within environmental risk systems. We have  
653 shown that existing uncertainty typologies across environmental risk domains:

- 654 (i)     use terminology that is often contradictory;
- 655 (ii)    communicate varying frequencies and dimensions of uncertainties;
- 656 (iii)   source information from limited data sets; and
- 657 (iv)    cannot be applied, on an individual basis, to ERAs in order to characterise the wide  
658         range of potential uncertainties.

659 To attempt to address these issues, we have integrated the salient attributes of environmental  
660 uncertainty, identified in this review, into a summary uncertainty typology – consisting of  
661 seven locations of uncertainty across five distinct levels - that is specifically for use with  
662 ERAs.

663           This review has highlighted the need to use existing uncertainty typologies with  
664 caution. We believe that this research will be of benefit to environmental risk analysts in their  
665 attempts to better qualify uncertainties, and thus statements about risk, within ERAs.

666

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672

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## Figure Captions

**Figure 1** A basic overview of uncertainty analysis, including the stages of understanding, identifying, and managing uncertainty, as performed in environmental risk assessments.

**Figure 2** Schematic showing the spectrum of uncertainty levels, defined through knowledge about likelihoods and knowledge about outcomes (after Walker *et al.* 2003 and Kraye von Kraus 2005).

**Figure 3** A summary uncertainty typology for use with environmental risk assessments, derived from a review of 30 identified typologies. The inner segments represent the potential nature(s) and location(s) of the uncertainty. The outer ring depicts the level(s) of uncertainty and is such that any location of uncertainty can exist at any level of uncertainty. This typology is suggested as an aid to uncertainty understanding and identification as it can be applied to the components within the different phases of ERAs.

Table 1. Information about the 30 uncertainty typologies examined in this review, including the risk domains in which they are based, the methods for data sourcing, and the uncertainties that they contain.

Typology source	Risk research domain	Typology based on	Uncertainties considered
Vesely and Rasmuson (1984)	Environmental risk management	Empirical evidence (literature)	Data; model (understanding, approximation); completeness; physical variability
Henriion and Fischhoff (1986)	Uncertainty analysis	Empirical evidence (literature)	Random; systematic
Alcamo and Bartnicki (1987)	Environmental modelling	Researcher opinion	Model (structure, parameters, forcing, initial state, operation)
Beck (1987)	Environmental modelling	Empirical evidence (literature)	Model (aggregation, structure, numerical, parameter); variability; errors
Morgan and Henriion (1990)	Environmental policy analysis	Researcher opinion	Statistical variation; systematic error; linguistic; variability; inherent randomness; disagreement; model (approximation, form)
Finkel (1990)	Environmental risk management	Empirical evidence (literature)	Model; parameter; decision; natural variability
Funtowicz and Ravetz (1990)	Environmental policy analysis	Researcher opinion	Inexactness; unreliability; border with ignorance
Wynne (1992)	Environmental policy analysis	Researcher opinion; Empirical evidence (literature)	Risk; uncertainty; ignorance; indeterminacy
Helton (1994)	Uncertainty analysis	Researcher opinion	Stochastic; subjective
Hoffman and Hammonds (1994)	Uncertainty analysis	Researcher opinion	Lack of knowledge; variability
Rowe (1994)	Uncertainty analysis	Researcher opinion	Temporal; structural; metrical; translational
Faucheux and Froger (1995)	Environmental decision-making	Empirical evidence (literature)	Ignorance; strong uncertainty; uncertainty; certainty

(Continued)

Table 1. (Continued).

Typology source	Risk research domain	Typology based on	Uncertainties considered
van der Sluijs (1997)	Environmental modelling	Researcher opinion; Empirical evidence (existing typologies)	Inexactness; unreliability; ignorance; model (input data, conceptual model structure, technical model structure, bugs, model completeness)
Stirling (1998)	Environmental policy analysis	Researcher opinion; Empirical evidence (literature)	Risk; uncertainty; ambiguity; ignorance
Bedford and Cooke (2001)	Environmental risk management	Researcher opinion	Alcatory; epistemic; parameter; data; model; ambiguity; volitional
Huijbregts et al. (2001)	Environmental risk management	Researcher opinion	Parameter; model; choices; variability (spatial, temporal, between source and object)
Bevington and Robinson (2002)	Uncertainty analysis	Researcher opinion	Systematic errors; random errors
Regan, Colyvan, and Burgman (2002)	Environmental risk management	Researcher opinion; Empirical evidence (literature)	Epistemic (measurement error, systematic error, natural variation, inherent randomness, model, subjective judgement); linguistic (vagueness, context dependence, ambiguity, underspecificity, indeterminacy of theoretical terms)
van Asselt and Rotmans (2002)	Environmental modelling	Empirical evidence (existing typologies)	Variability (nature, cognitive, behavioural, societal, technological); knowledge (inexactness, lack of measurements, practically immeasurable, conflicting evidence, ignorance, indeterminacy)
Janssen et al. (2003)	Environmental risk management	Researcher opinion; Empirical evidence (literature)	Statistical; scenario; recognised ignorance; knowledge-based; variability-based; context; expert judgement; model (structure, technical, parameters, input); data; outputs
Walker et al. (2003)	Environmental decision-making	Researcher opinion; Empirical evidence (literature)	Statistical; scenario; recognised ignorance; total ignorance; epistemic; variability; context; model (structure, technical, parameters, input, outputs)
Brown (2004)	Uncertainty analysis	Researcher opinion; Empirical evidence (literature)	Bounded uncertainty; unbounded uncertainty; indeterminacy; ignorance
Dewulf et al. (2005)	Environmental risk management	Empirical evidence (existing typologies)	Inherent nature of phenomena; lack of knowledge; ambiguity in system understanding

(Continued)

Table 1. (Continued).

Typology source	Risk research domain	Typology based on	Uncertainties considered
Beer (2006)	Environmental risk assessment	Empirical evidence (literature, existing typologies)	Probabilistic; ambiguity; incertitude; ignorance; indeterminacy
Petersen (2006)	Environmental modelling	Researcher opinion; Empirical evidence (literature, existing typologies)	Location; nature; range; recognised ignorance; methodological unreliability; value diversity
Hayes et al. (2006)	Environmental risk assessment	Researcher opinion; Empirical evidence (literature)	Linguistic; variability; incertitude
Maier et al. (2008)	Environmental decision-making	Researcher opinion; Empirical evidence (literature)	Data (measurement error, type of data, length of record, analysis); model (method, record quality, calibration, validation, experience); human (stakeholder, politics)
Ascough II et al. (2008)	Environmental decision-making	Empirical evidence (existing typologies)	Knowledge; variability; linguistic; process; model; variability; linguistic; decision
Brouwer and Blois (2008)	Environmental modelling	Empirical evidence (existing typologies)	Statistical; scenario; qualitative; recognised ignorance
Knol et al. (2009)	Environmental risk assessment	Researcher opinion; Empirical evidence (existing typologies)	Statistical; scenario; recognised ignorance; epistemic; ontic (process, normative); model (structure, parameters, input data); methodological; analyst uncertainty



Table 2. Contradictions in terms (where the same single term is used to represent two or more distinct uncertainty types) between the 30 typologies, with regard to the location, level and nature of uncertainty, and featuring the terms ambiguity (as denoted by the symbol (1), indeterminacy (2), natural variability (3), parameter (4), random (5), statistical (6), systematic (7) and variability (8).

Uncertainty Type	Location					Level					Nature			
	System	Data	Model	Human	Language	Variability	Decision	State 1 (determinism)	State 2 (statistical)	State 3 (scenario)	State 4 (recognised ignorance)	State 5 (total ignorance)	Knowledge-based	Randomness-based
Vesely and Rasmuson (1984)														8
Alcarno and Bartnicki (1987)			4											
Beck (1987)			4											
Morgan and Henrion (1990)		6,7				8								
Finkel (1990)		6,7	4			3					2			
Wynne (1992)														
Hoffman and Hammonds (1994)														8
Rowe (1994)														
Stirling (1998)									1					
Bedford and Cooke (2001)			4		1									
Huijbregts et al. (2001)			4											
Bevington and Robinson (2002)													7	
Regan, Colyvan, and Burgman (2002)		7			1,2	3						2		5
van Asselt and Rotmans (2002)						3,8								8
Janssen et al. (2003)			4						6					8
Walker et al. (2003)			4						6					8
Brown (2004)												2		
Devulif et al. (2005)	1								6					
Petersen (2006)														
Hayes et al. (2006)														
Ascough II et al. (2008)			4		1	3,8								8
Brouwer and Blois (2008)								6						
Knol et al. (2009)			4					6						

Table 3. Identified contradictions in description terms between the 30 typologies where distinct terms are used to describe the same uncertainty type, with regard to the nature dimension (knowledge or randomness) of uncertainty.

Typology	Term describing knowledge uncertainty	Term describing random uncertainty
Vesely and Rasmuson (1984)	Completeness	Variability
Helton (1994)	Subjective	Stochastic
Hoffman and Hammonds (1994)	Knowledge	Variability
Rowe (1994)	Completeness	N/A
van Asselt and Rotmans (2002)	N/A	Variability
Bedford and Cooke (2001)	Epistemic	Aleatory
Bevington and Robinson (2002)	Systematic	Random
Regan, Colyvan, and Burgman (2002)	N/A	Random
Janssen et al. (2003)	Knowledge	Variability
Walker et al. (2003)	Epistemic	Variability
Dewulf et al. (2005)	Uncertainty	Indeterminacy
Petersen (2006)	Epistemic	Ontic
Hayes et al. (2006)	Incertitude	Variability
Ascough II et al. (2008)	Epistemic	Aleatory
Knol et al. (2009)	Epistemic	Ontic

Table 4. The number of distinct uncertainties and dimensions communicated by each of the 30 uncertainty typologies featured in this review.

Typology source	Risk research domain	Uncertainty frequency	Dimension frequency
Vesely and Rasmuson (1984)	Environmental risk management	5	2
Henrion and Fischhoff (1986)	Uncertainty analysis	2	1
Alcamo and Bartnicki (1987)	Environmental modelling	5	1
Beck (1987)	Environmental modelling	6	2
Morgan and Henrion (1990)	Environmental policy analysis	8	2
Finkel (1990)	Environmental risk management	4	1
Funtowicz and Ravetz (1990)	Environmental policy analysis	3	1
Wynne (1992)	Environmental policy analysis	4	1
Helton (1994)	Uncertainty analysis	2	1
Hoffman and Hammonds (1994)	Uncertainty analysis	2	1
Rowe (1994)	Uncertainty analysis	9	3
Faucheux and Froger (1995)	Environmental decision-making	4	1
van der Sluijs (1997)	Environmental modelling	7	2
Stirling (1998)	Environmental policy analysis	4	1
Bedford and Cooke (2001)	Environmental risk management	11	3
Huijbregts et al. (2001)	Environmental risk management	7	2
Bevington and Robinson (2002)	Uncertainty analysis	6	1
Regan, Colyvan, and Burgman (2002)	Environmental risk management	2	1
van Asselt and Rotmans (2002)	Environmental modelling	11	2
Janssen et al. (2003)	Environmental risk management	13	3
Walker et al. (2003)	Environmental decision-making	10	3
Brown (2004)	Uncertainty analysis	4	1
Dewulf et al. (2005)	Environmental risk management	3	2
Beer (2006)	Environmental risk assessment	4	1
Petersen (2006)	Environmental modelling	8	3
Hayes et al. (2006)	Environmental risk assessment	3	1
Maier et al. (2008)	Environmental decision-making	11	1

(Continued)

Table 4. (Continued).

Typology source	Risk research domain	Uncertainty frequency	Dimension frequency
Ascough II et al. (2008)	Environmental decision-making	16	3
Brouwer and Blois (2008)	Environmental modelling	4	1
Knol et al. (2009)	Environmental risk assessment	10	3

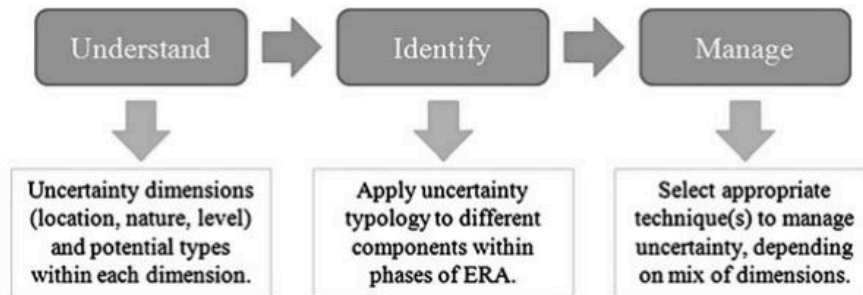


Figure 1. A basic overview of uncertainty analysis, including the stages of understanding, identifying and managing uncertainty, as performed in environmental risk assessments.

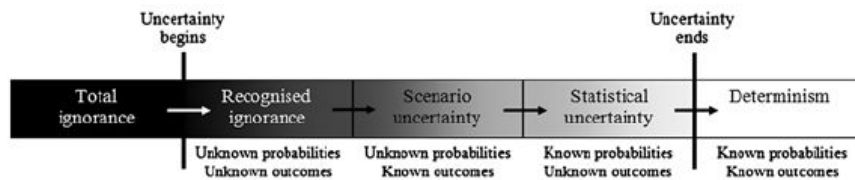


Figure 2. Schematic showing the spectrum of uncertainty levels, defined through knowledge about likelihoods and knowledge about outcomes (after Walker et al. 2003; Krayen von Kraus 2005).

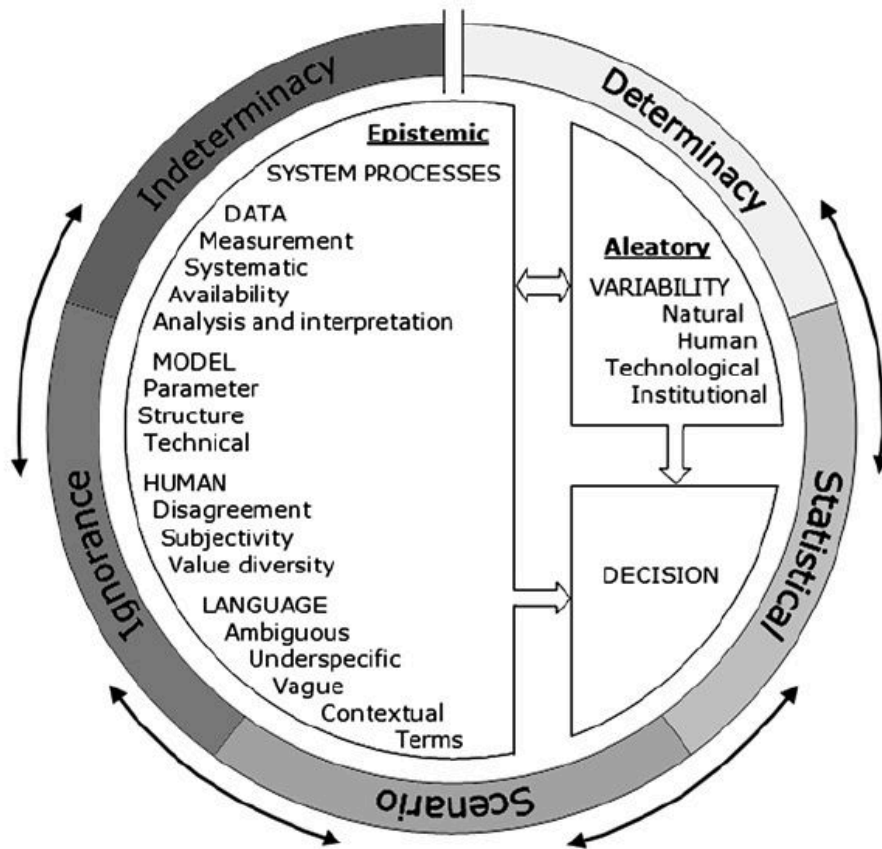


Figure 3. A summary uncertainty typology for use with environmental risk assessments, derived from a review of 30 identified typologies. The inner segments represent the potential nature(s) and location(s) of the uncertainty. The outer ring depicts the level(s) of uncertainty and is such that any location of uncertainty can exist at any level of uncertainty. This typology is suggested as an aid to uncertainty understanding and identification as it can be applied to the components within the different phases of ERAs.