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A time-series turbofan engine successive fault diagnosis under both steady-state and dynamic conditions

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ABSTRACT

8 In recent years there has been a growing interest in gas turbine fault diagnosis, especially 9 under dynamic conditions, due to the evolving operating profile of gas turbines and the need to 10 deploy computationally efficient and high-precision diagnostic solutions in real-time. One of the 11 main challenges of fault diagnosis in real-time is the power imbalance between the compressor 12 and turbine that occurs during transient operation. In addition, the heat soakage phenomenon characterizing the transient conditions has a substantial impact on the accuracy of the diagnosis. 13 14 Finally, any sudden failure that might happen during transient operating conditions creates an 15 additional challenge to fault diagnostics. The present study proposes a gas turbine diagnostic 16 approach based on time-series measurements encapsulating steady-state and transient 17 operating conditions. Specifically, the introduced novel approach is capable of quantifying the surplus/deficit of the power between the compressor and the turbine by utilizing the time-series 18 19 data representing the observed deviations in the shaft rotational speed in order to determine the 20 power balance in the shaft. The maximum diagnostic errors for constant fault and sudden 21 failure are less than 0.006% during the dynamic maneuver. The results demonstrate and 22 illustrate that the proposed method could effectively and accurately diagnose the severity of 23 aero-engine faults at both steady-state and transient conditions. Therefore, this study has great 24 potential for gas turbine practitioners since the diagnosis under transient conditions in real-

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25 time can enhance the capability of engine online condition monitoring and improve the

26 condition-based maintenance of gas turbine assets.

Key Words: Turbofan Engine Degradation; Time-series Fault Diagnosis; Real-time Engine Fault
 Monitoring.

30 31			Nomenclature
32	Α	=	Area [m ²]
33	AW	=	Auxiliary work [W]
34	СР	=	Characteristic parameter
35	CW	=	Compressor work [W]
36	HP	=	High-pressure
37	Ι	=	Shaft inertia $[kg \cdot m^2]$
38	LP	=	Low-pressure
39	n	=	Number of measurements
40	Ν	=	Shaft rotational speed [rpm]
41	Р	=	Pressure [atm]
42	PR	=	Pressure ratio
43	Q	=	Heat rate [W]
44	RMSE	=	Root mean square error
45	SP	=	Engine shaft surplus power [W]
46	Т	=	Temperature [Kelvin]
47	TW	=	Turbine work [W]
48	U	=	Heat transfer coefficient $[W/(m^2 \cdot K)]$
49	W	=	Mass flow rate $[kg/s]$
50	X	=	Degradation index
51	Ζ	=	Measurements

52			
53 54			Greek Letters
55	τ	=	Time constant [s]
56			
57 58			Subscripts
59	а	=	Actual condition
60	С	=	Clean condition
61	Ε	=	Efficiency
62	F	=	Flow capacity
63	g	=	Gas flow
64	ht	=	heat transfer
65	in	=	Inlet
66	loc	=	Local component characteristic
67	т	=	Metal
68	out	=	Outlet
69			
70			1. Introduction

The gas turbine engine is among the most important process engines for commercial and military aircraft [1]. Over the past years, there has been a dramatic development in gas turbine technology with more and more complex engine structures [2,3]. Gas path fault diagnosis is crucial to ensure the safety, economy, and reliability of aero-engine operations. Accordingly, a growing interest in gas path analysis (GPA) of gas turbine engines has been witnessed to guarantee effective condition-based maintenance. GPA is a gas path fault diagnosis technique that establishes the relationship between unmeasurable health parameters and measurable operating parameters [4]. GPA, established in 1969 by Urban [5], plays an essential role in the condition monitoring of gas turbine engines. As sudden failure has

dramatically impacted engine safety, real-time fault diagnosis is becoming a significant area of research in gas turbine
 engine condition monitoring.

80 The majority of aero-engine gas path analysis methods are based mainly on gas path measurements available from 81 steady-state operating conditions [6]. In contrast, the gas path measurements obtained during transient conditions are 82 mainly analyzed and processed offline, which cannot meet the requirement of online and real-time health monitoring. 83 If the engine encounters a sudden fault during any transient maneuver, the steady-state gas path fault diagnostic system 84 will not be able to respond promptly. In addition, engine component performance degradation will affect the 85 compressor surge margin [7]. Therefore, real-time assessment of the compressor surge margin is crucial for safe 86 control and operation of the engine transient process. Consequently, there is an urgent need to address the fault 87 diagnosis in real-time under dynamic maneuvers for gas turbine engines on continuous feedback of gas path fault and 88 improve the engine's emergency response capability. Until recently, little attention has been paid to the real-time 89 monitoring of engines under transient conditions.



(a) Sliding window method

(b) Steady-state approximation method

90

Fig. 1 Fault diagnosis methods at transient conditions.

91 In recent years, several attempts have been made to diagnose gas turbine degradation under both steady-state and 92 transient conditions, where two different approaches have been proposed. The first one, the sliding window method, 93 is to simulate the gas path measurements during the whole dynamic maneuver with estimated degradation and then 94 compare them to the actual engine measurements from the monitoring system in order to iterate the predicted fault 95 (Fig. 1 (a)). Li (2003) [8] developed a fault diagnosis method for turbofan engines under transient conditions based 96 on the sliding window method. Ogaji et al. (2003) [9] conducted a gas turbine fault diagnosis based on artificial neural 97 networks during a dynamic maneuver. Tsoutsanis et al. (2015) [10] proposed a fault diagnostic method by map tunning 98 with selected sliding windows for the targeted gas path measurements, where the average prediction error is 0.15%. 99 In the following two years, the GPA method has been further developed by Tsoutsanis et al. [11,12] to incorporate the

fault prognosis for gas turbines under dynamic conditions. Chen et al. (2022) [13] conducted an aero-engine fault diagnosis based on a sequential method under dynamic conditions. However, the above methods considered only soft degradation during a dynamic maneuver, which is the most common in gas turbines, but attention should be paid to the abrupt degradation scenarios in transient conditions.

104 The second method, the steady-state approximation method, considers time-series measurements independent. A 105 steady-state fault diagnosis model is applied to each set of discrete measurements for both steady-state and dynamic 106 conditions in the timeline (Fig. 1 (b)). Li and Ying (2020) [14] attempted to evaluate the degradation indices of a 107 heavy-duty industrial gas turbine engine based on a steady-state approximation method for both steady-state and 108 dynamic conditions. The diagnostic results were promising for the examined test cases, but the diagnosis accuracy 109 might be compromised for other types of engines. The reason for this lies in the fact that the impact of transient 110 conditions in the fault diagnosis, as expressed by a power imbalance, heat soakage, and lag response under dynamic 111 conditions, has not been considered. Heavy-duty industrial gas turbine engines could ignore the aforementioned 112 transient effects as they have the inertia of slow dynamic response. Still, they should be accounted for faster response 113 gas turbine engines such as aero-derivative and aero-engines. Especially for engines with rapid transient maneuver 114 capabilities and larger temperature and pressure variations in different operation conditions, the above method will be 115 inappropriate, and the integrity of the diagnosis will be severely affected by transient effects. The power imbalance 116 among different components on the same shafts and the heat soakage effect will greatly impact estimating the health 117 parameters during dynamic conditions. Although the method could predict the health state in real-time, the predicted 118 results will not be accurate, In such a situation.

The main challenge of fault diagnosis in real-time is the dynamic effect during transient maneuvers. Currently, fault diagnosis methods under transient conditions proceed either with the fault diagnosis after selecting a sliding window [2–5] or the steady-state approximation method without considering the dynamic effects such as heat soakage and power imbalance [14]. Therefore, it is of paramount importance for the condition-based maintenance of gas turbine engines to have a fault diagnosis algorithm that is capable of capturing the actual health state in real-time, even with sudden failure during dynamic operating conditions.

A time-series diagnostic method is proposed for gas turbine engines operating under both steady-state and dynamic conditions to address the gap mentioned above in the literature. The novelty of this study lies in the fact that we proposed a diagnostic method for transient conditions which could quantify the dynamic effects during transient

128 maneuvers at each time instant. The fault diagnosis captures the transient effect in the gas turbine in accordance with 129 time series gas path measurement data. More specifically, the power imbalance between turbine and compressor is 130 addressed by accounting for the shaft acceleration rate in order to determine both the surplus power under dynamic 131 conditions and the power equality constraints for each shaft. The heat soakage effect during transient conditions could 132 also be considered in the diagnosis model when previous measurements in the timeline are utilized to calculate the 133 new metal temperature in the following timeline. In addition, the lag response that characterizes the transient 134 conditions could be addressed by considering the first-order lag. Finally, as the measurements are successive, the 135 sudden failure could also be diagnosed accurately during any time point of a dynamic maneuver. Based on the 136 literature review, no publications have been found so far that could correctly diagnose the fault level in real-time under 137 transient conditions. The main contributions of this study are summarized as follows:

- A new real-time successive fault diagnosis method is proposed by considering the engine monitoring system
 under dynamic conditions.
- 140 2) The proposed algorithm considers transient effects on fault diagnosis based on time-dependence data.
- The fault level of five engine components that experience degradation simultaneously could be reflected in
 real-time when new time-series data is transferred to the diagnostic system while the constant engine
 degradation is implanted.
- In all previous research efforts, the sudden failure during dynamic conditions had a severity level that made
 it difficult to be monitored in real-time. This study could observe the sudden failure during a transient
 maneuver with excellent diagnosis accuracy.

147 The remaining part of the paper proceeds as follows: The second section of this paper will describe the 148 methodology for the related methods. The third and fourth section of the paper deals with the application and the 149 analysis, respectively. The final section summarizes the main findings and implications of this study.

150

2. Methodology

151 **2.1** Assumptions

152 The methodology and test cases are based on the following assumptions since these will facilitate the comparison

153 of the proposed method to a recently published benchmark method [14].

- Measurement noise/bias is ignored because there are mature methods for noise filtering and sensor
 verification [15,16]. Furthermore, rather than sensor-related issues, this research attempts to improve the
 performance of the diagnostic algorithm.
- The efficiency, flow capacity, and pressure ratio indices are used to quantify the fault level as health parameters. Furthermore, the pressure ratio index is assumed to be the same as the flow capacity index [17].
- All turbofan engine rotating components are experiencing degradation simultaneously. Moreover, any sudden
- 160 failure will cause concurrent degradation of all engine components.

161 2.2 Turbofan Engine Performance and Degradation Modelling

162 2.2.1 Performance Modelling

Our previous publications have validated the steady-state and transient engine performance models [13,18] in the C # environment. Fig. 2 [13] presents the turbofan engine configuration with station numbering that includes a fan, a low-pressure compressor, a high-pressure compressor, a combustor, a high-pressure turbine, and a low-pressure turbine. The design point specification of the turbofan engine in concern is presented in Table 1. The turbofan engine measurements on-wing for fault diagnosis are listed in Table 2 [19].



- 168 169
- 170
- 171

Item	Symbol	Unit	Value
Flight Mach Number	MN	-	0.8
Flight Altitude	ALT	km	11
Intake Airflow Rate	W_{in}	kg/s	222
Burner Fuel Flow	W_{BFF}	kg/s	0.1876
Low Heating Value	LHV	MJ/kg	118.429
Engine Pressure Ratio	EPR	-	33.8
Engine Bypass Ratio	EBR	-	9

Table 1 Turbofan engine design point specification.

172

174

Table 2 Turbofan engine measurements on-wing [19].

No	Measurement	Symbol
1	Ambient pressure	P_1
2	Ambient temperature	T_1
3	Bypass inlet total pressure	P ₃₃
4	Low-pressure compressor (LPC) exit total pressure	P_4
5	LPC exit total temperature	T_4
6	High-pressure compressor (HPC) exit total pressure	P_5
7	HPC exit total temperature	T_5
8	Low-pressure turbine (LPT) inlet total pressure	P_9
9	LPT inlet total temperature	T_9
10	LPT exit total pressure	P_{10}
11	LPT exit total temperature	T_{10}
12	Flight Mach Number	MN
13	<i>LP</i> shaft rotational speed	N_{LP}
14	HP shaft rotational speed	N_{HP}
15	Burner fuel flow rate	W_{Fuel}

175

176 2.2.2 Degradation Modelling

Normally, the performance of gas turbines is related to the performance of each sub-component [12,20]. Therefore, Eq. (1) defines the degradation index (X) which is related to the degradation of each component characteristic parameter[21,22].

$$X = \frac{CP_a}{CP_c} \tag{1}$$

180 where the subscript "a" and "c" represent the actual and clean conditions, respectively. If X is 1, it means that the

181 engine is at a nominal clean condition where the denominator is the same as the numerator [23,24].

Table 3 [25] summarizes the health parameters relevant to the turbofan engine in concern. The 'Health State 1' refers to constant/smooth degradation of the engine in concern, whereas the 'Health State 2' refers to a more severe level of degradation, which is double that in 'Health State 1'. The magnitude of 'Health State 2' refers to a large bypass turbofan engine that has completed 6000 flight cycles [25]. The 'Health State 1' is also applied to the engine degradation level before sudden failure, whereas 'Health State 2' represents the engine degradation level after sudden failure.

188

Table 3 Degr	adation indic	es of turbof	an engine	[25]	•

Component	nent Symbol		Health Parameter	Health State 1	Health State 2 [25]
EAN	v	$X_{FAN,E}$	FAN efficiency index	-1.425 %	-2.85 %
FAN	Λ_{FAN}	$X_{FAN,F}$	FAN flow capacity index	-1.825 %	-3.65 %
IDC	v	$X_{LPC,E}$	LPC efficiency index	-1.305 %	-2.61 %
LPC	ALPC	$X_{LPC,F}$	LPC flow capacity index	-2.00 %	-4.00 %
IIDC	X _{HPC}	$X_{HPC,E}$	HPC efficiency index	-4.70 %	-9.40 %
прс		$X_{HPC,F}$	HPC flow capacity index	-7.03 %	-14.06 %
דמוו	V	$X_{HPT,E}$	HPT efficiency index	-1.905 %	-3.81 %
ΠΓΙ	ΛΗΡΤ	$X_{HPT,F}$	HPT flow capacity index	+1.285 %	+2.57 %
I D/T	V	$X_{LPT,E}$	LPT efficiency index	-0.539 %	-1.078 %
LPI	X_{LPT}	$X_{LPT,F}$	LPT flow capacity index	+0.2113 %	+0.4226 %

189

190 2.3 Benchmark Method

191 Nonlinear gas path analysis is widely used for model-based fault diagnosis, where the engine thermodynamic 192 performance model may be defined by Eq. (2). The iteration solver is applied to update the degradation index X during 193 fault diagnosis in order to minimize the difference between the predicted measurements ($Z_{Predict}$) from the engine 194 model and the actual measurements (Z_{Actual}) available from a service engine. In this study, the Newton-Rapson 195 method [26] is chosen as the iteration solver for all the cases regarding performance simulation and fault diagnosis.

$$Z = f(X) \tag{2}$$

196 where Z denotes measurements of the engine, and X denotes the degradation indices of engine components.

197 The root mean square error (*RMSE*) defined by Eq. (3) [27,28] is selected to evaluate the convergence with a

198 threshold of 1E-5 as the convergence criteria.

$$RMSE = \sqrt{\sum_{i=1}^{n} \frac{(Z_{Predict,i} - Z_{Actual,i})^2}{n}}$$
(3)

199 where *n* is the number of measurements.



200 201

202

Fig. 3 Schematic of benchmark fault diagnosis method [13].

The method proposed by Li and Ying in 2020 [14] will be used as the "benchmark method" in this study. The schematic of the benchmark method is shown in Fig. 3 [13]. It is clear that the steady-state fault diagnosis model is characterized by time independence as the steady-state approximation is employed. The method will be applied to a high bypass ratio civil turbofan engine in order to generate some baseline diagnostic results.

The performance simulation and fault diagnosis processes are invoked in the same iteration loop. The iteration variables of the benchmark method are the ten degradation indices listed in Table 3 and the blocks with a purple color in Fig. 4. The convergence is checked based on compatibility shown in the blocks with blue color in Fig. 4. The detailed process is explained as follows:

The flight altitude, Mach Number, and inlet condition are known through on-wing measurements. Then, the fan inlet condition could be obtained by the intake model. It follows that the fan bypass pressure ratio could be calculated based on Eq. (4) [29] where P_{33} is a gas path measurement. As the fan inlet condition, shaft speed, and bypass pressure ratio are known, the fan outlet temperature and pressure at both core and bypass could be determined through the fan model [13].

$$PR_{FAN,BP} = P_{33}/P_2 \tag{4}$$

The *LPC* pressure ratio is obtained by Eq. (5) [30] where P_4 is a gas path measurement and P_3 could be determined from the fan model. Then, the *LPC* model calculation will follow as the pressure ratio, shaft speed, and inlet condition are known. It is worth noting that the core mass flow rate obtained in the *LPC* model is used to update the core flow and bypass flow rates in the fan model, which will also determine the bypass ratio. Moreover, the fan work is also updated according to the new bypass ratio.

$$PR_{LPC} = P_4/P_3 \tag{5}$$

The *HPC* pressure ratio can be obtained by Eq. (6) where P_5 and P_4 are gas path measurements. Then the *HPC* model could be used to calculate the outlet condition as the pressure ratio, shaft speed, and inlet condition are known.

$$PR_{HPC} = P_5 / P_4 \tag{6}$$

As the *HPC* outlet condition is known, the burner outlet condition could be calculated as the fuel flow rate is also known. The mixture model is applied to calculate the *HPT* inlet condition. The *HPT* pressure ratio could be obtained by Eq. (7) where P_9 is gas path measurements and P_7 could be known from the mixture model after the combustor.

$$PR_{HPT} = P_7 / P_9 \tag{7}$$

The *LPT* inlet condition could be obtained by the mixture after *HPT*. The *LPT* pressure ratio could be obtained by Eq. (8) [31] where P_9 and P_{10} are gas path measurements. Finally, two sets of duct and nozzle are applied to calculate main flow and bypass flow exhaust condition.

$$PR_{LPT} = P_9 / P_{10} \tag{8}$$



There are eleven convergence criteria in the diagnostic algorithm represented in blue blocks in Fig. 4. The convergence criteria could be classified into two categories. One set of convergence criteria is obtained from gas path measurements, including T_4 , T_5 , T_9 , and T_{10} . The other set of convergence criteria is required to satisfy the mass flow compatibility, shaft power balance, and design nozzle area at the design point. It is worth noting that the LP and HP

shaft power compatibility in blue blocks means that the turbine work has to be equal to the compressor work plus any auxiliary work at all times, as the steady-state approximation fault diagnosis method is employed. This is one of the main assumptions of the benchmark method that may lead to diagnostic errors since the surplus power during dynamic conditions is ignored. Another source of uncertainty is the assumption that the typical phenomenon of heat soakage and lag response during dynamic conditions is ignored when the steady-state model is implemented. In such a condition, diagnostic accuracy may be compromised.

242 2.4 Proposed Method



Time

243

244

Fig. 5 Schematic of proposed fault diagnosis method.

245 The benchmark method may be sufficient for slow transient maneuvers which characterize heavy-duty industrial 246 gas turbines as the steady-state approximation is employed in their study. However, the performance of the benchmark 247 method is limited in transient conditions if the power imbalance among shaft, heat soakage, and lag response are not 248 considered. This study intends to diagnose the health of a civil turbofan engine with time-series data during steady-249 state and transient conditions. The transient effect could not be ignored for the turbofan engine in concern as it exhibits 250 a fast and dynamic response. The schematic of the proposed method is demonstrated in Fig. 5, where shaft speeds 251 derive the surplus power during dynamic processes among adjacent measurement steps in the diagnostic system for 252 the consideration of shaft power compatibility in Fig. 4. Moreover, the heat soakage is also considered in the engine

253 sub-models to represent the heat transfer between gas and engine metal during the transient maneuver for the 254 temperature compatibility check in Fig. 4. the first order lag is selected in this study to represent the lag response of 255 sensor property in Fig. 4 under dynamic conditions. It is clear that the measurements are time-dependent in the 256 proposed method, where the surplus power, transient heat transfer, and lag response are needed to be considered in 257 consecutive time steps, which are highlighted in the green block in Fig. 5. In addition, the shaft model also takes lag 258 response into account to capture the dynamic response with increased precision. Although the two red points under 259 dynamic conditions are selected to illustrate the new method in Fig. 5, the proposed method is also suitable for steady-260 state conditions.

261

262 2.4.1 Rotor Dynamics

Gas path measurements could not directly monitor the surplus power among each shaft. As the engine shaft speed is monitored in time-series, the rotor acceleration rate could be derived through the deviation of shaft speed in finite time steps by Eq. (9) [32,33].

$$\frac{dN}{dt} = \frac{N(t + \Delta t) - N(t)}{\Delta t}$$
(9)

In such a condition, the surplus power (*SP*) could be calculated by Eq. (10) [34,35] by rotor acceleration rate, shaft speed, and shaft inertia (*I*).

$$SP = \frac{4\pi^2}{3600} \cdot I \cdot N \cdot \frac{dN}{dt} \tag{10}$$

Then, the power balance among each shaft could be obtained by (11) [36,37]. The equation is tenable for both steady-state and dynamic conditions where the *SP* is zero during the steady-state condition. Hence, the proposed method could satisfy the shaft power compatibility when surplus power is considered for both steady-state and dynamic conditions in a more coherent fashion than the benchmark method.

$$TW = SP + CW + AW \tag{11}$$

272 where TW is turbine work, CW is compressor work, and AW is auxiliary work for power offtake.

273 2.4.2 Heat Soakage

274 During transient maneuvering, changing gas temperature in a turbofan engine will affect the engine metal

temperature. This phenomenon is called heat soakage and is not considered in the steady-state fault diagnosis of thebenchmark method.

277 The heat soakage is considered in the dynamic engine model in the proposed method. The heat transfer between

gas flow and engine metal is obtained by Eq. (12) with exponential decay [38].

$$Q = U_{ht} \cdot A_{ht} (T_{g,k+1}^b - T_{m,k}) \cdot (e^{-\Delta t/\tau} - 1)$$
(12)

279 where Q is heat rate, U_{ht} is heat transfer coefficient, A_{ht} is the effective contact surface, $T_{g,k+1}^b$ is the gas temperature

in the current step before considering heat soakage, $T_{m,k}$ is the metal temperature in the previous step, Δt is the time

281 step, and τ is the time constant.

282 The heat transfer coefficient is calculated as follows:

$$U_{ht} = \frac{1}{\frac{1}{FC} + \frac{l_{eff}}{k_m}}$$
(13)

Additionally, the time constant is determined by Eq. (14).

$$\tau = \frac{c_m \cdot W_m}{U_{ht} \cdot A_{ht}} \tag{14}$$

where W_m is the effective mass of engine component, c_m is the specific heat of the engine material.

285 The change of engine metal temperature (dT_m) could be obtained by Eq. (15).

$$\frac{dT_m}{dt} = \frac{Q}{c_m \cdot W_m} \tag{15}$$

The metal temperature of the engine component in the current step $(T_{m,k+1})$ could be obtained as follows:

$$T_{m,k+1} = T_{m,k} - dT_m$$
(16)

287 The change of gas enthalpy (ΔH_g) when considering the heat transfer could be determined by Eq. (17).

$$\Delta H_g = \frac{Q}{W_g} \tag{17}$$

288 where W_g is the mass flow rate of gas.

The gas enthalpy at the current step with the consideration of heat soakage $(H_{q,k+1})$ could be obtained as follows:

$$H_{g,k+1} = H_{g,k+1}^b + \Delta H_g \tag{18}$$

290 where $H_{g,k+1}^b$ is gas enthalpy at current step before considering heat soakage.

The gas temperature at the current step with the consideration of heat soakage $(T_{q,k+1})$ could be determined by Eq.

292 (19).

$$T_{g,k+1} = GasProp_{[H,P]}(H_{g,k+1}, P_{g,k+1}, FAR, WAR)$$
(19)

293 2.4.3 Lag Response of Engine Shafts

The time delay phenomenon of the engine shafts during transient maneuvering is represented using the first-order lag. As $N_{out}(s)$ is measured through an on-wing monitoring system, the $N_{in}(s)$ could be derived by Eq. (20) [39,40] for the engine model.

$$\frac{N_{out}(s)}{N_{in}(s)} = \frac{1}{\tau \cdot s + 1}$$
(20)

297 where τ is the characteristic time, $N_{out}(s)$ is the input with delay and $N_{in}(s)$ is the input value without delay.

298 **3.** Application and Analysis

Four case studies are examined in this paper. In order to make a direct comparison between the proposed and the benchmark methods [14], the same computer environment is used. To be more specific, a personal computer with Intel(R) i7 CPU @2.90GHz and 16 GB RAM is used to evaluate the computational time of the diagnostic process for all case studies. The four cases are specified as follows:

303 **Case 1**. This case study aims to evaluate the effectiveness of the benchmark diagnostic method [14] when the 304 engine gas path measurements represent dynamic operating conditions without consideration of heat soakage.

305 **Case 2.** The measurements in this case study represent the dynamic performance with the effect of heat soakage

306 included. This case study aims to investigate the effectiveness of the benchmark diagnostic method [14] for diagnosing

- 307 the health of the engine from transient measurements by taking into account the heat soakage phenomenon in order to
- set a baseline diagnostic data set that will be further used for comparing it with the proposed method.

309 Case 3. This case study demonstrates and illustrates the proposed method's advantage compared to the baseline

310 diagnostic results from Case 2, which implemented the benchmark method [14].

311 **Case 4**. While the previous three case studies tested the diagnostic results under constant fault levels during a 312 transient maneuver, this case study is designed to demonstrate the capability of the proposed method to deal with 313 sudden failure during transient operation.

The first three cases have a constant degradation level called 'Health State 1' as shown in Table 3 [25]. In Case study 4, we inject the degradation level denoted as 'Health State 1' between [0-3) s and 'Health State 2' between [3-15] s with the sudden failure initiated at the time mark of 3.0 s.

317 **3.1** Case 1: Benchmark Method - Transient Measurements without Considering Heat Soakage

As mentioned in the methodology, the benchmark method [14] did not take into account the surplus power in the fault diagnosis during dynamic conditions. This may be true as the focus of that study was a heavy-duty industrial gas turbine engine. Due to its large shaft inertia, the transient maneuver for heavy-duty gas turbine engines is relatively slower than other gas turbines (i.e., aero-derivative engines and turbofans). However, such an assumption will compromise the diagnostic performance of other gas turbines.

323 Fig. 6 (top) demonstrates an acceleration fuel schedule with a 0.1 s time step during a dynamic maneuver for the 324 turbofan engine in concern. It is well known that the power balance between compressor work and turbine work will 325 not be satisfied during the transient maneuver. As shown in Fig. 6 (middle), the maximum surplus power obtained 326 from the power imbalance between the compressor and turbine is close to 320 kW during the maneuver for both LP 327 and HP shafts. The maximum difference between compressor work and turbine work is 5.3% and 3.0% for LP and HP shaft in Fig. 6 (bottom), respectively. Therefore, if the surplus power is ignored, the relative error will propagate 328 329 to the diagnostic results. It follows that the larger the surplus power, the less accurate the diagnostic results will worsen 330 in steady-state approximation.

331 The average computation time for diagnosis with the benchmark method is 0.2024 s. Fig. 7 presents the diagnostic 332 results based on the benchmark method. It is apparent from this figure that the surplus power impacts the accuracy of 333 the diagnosis. The error of the diagnosis keeps increasing until approximately the 3 s mark, where the maximum 334 prediction error is observed. Then, the prediction error of health parameters decreases as the surplus power falls off. 335 In such a condition, the benchmark method will lead to fluctuation of the diagnostic results and may set a false alarm of sudden engine degradation. Moreover, the faster the variation of the fuel schedule is, the larger the surplus power 336 337 and the bigger the prediction errors are going to be. The average prediction error of all ten health parameters during the transient maneuver is shown in Fig. 8. Although the average maximum prediction error of ten health parameters 338

- hovers at 1.4265% in Fig. 8, the maximum prediction error during the dynamic maneuver is 6.3396 % at 2.6 s for
- 340 $X_{FAN,E}$. Such a prediction error may lead to inaccurate diagnosis.





Fig. 6 Fuel schedule and power imbalance between CW and TW during a transient maneuver.

In summary, the benchmark method could be beneficial if the surplus power is negligible. This typically happens when there is a slow variation of fuel flow rate with respect to time during a transient maneuver. In other cases, the benchmark method will significantly fluctuate its diagnostic results. Consequentially, the benchmark method cannot monitor the engine health state in real-time when each set of measurements is recorded. Thus, such a method is not capable of monitoring the sudden engine failure that a bird strike may cause.





Fig. 7 Predicted health parameters during a transient maneuver.





Fig. 8 Average relative error of health parameters during a transient maneuver.



353 During dynamic operating conditions, the gas turbine is not only facing power imbalance among shafts but also 354 experiences heat transfer between gas and engine components. Fig. 9 presents the effect of heat soakage on exhaust 355 gas temperature with time during a transient maneuver with and without considering heat soakage. It is evident that 356 heat soakage impacts the gas path measurement of the exhaust temperature by delaying its increase in comparison 357 with the case where heat soakage is ignored, as seen in Fig. 9. If the engine is faced with a slam transient maneuver, 358 the predicted engine health parameters are likely to be affected.





Fig. 9 Effect of heat soakage on exhaust gas temperature.





higher deviation from the actual health state when compared with Case 1. Apart from the HPT efficiency degradation 365 index, the heat soakage phenomenon will increase the prediction error when considering the heat soakage in transient 366 367 measurements. The surplus power will lead to over-prediction of the HPT efficiency degradation, while the heat 368 soakage will under-predict the HPT efficiency degradation. Fig. 11 provides the summary of the average prediction 369 error for ten health parameters. The maximum average error of the benchmark method has increased from 1.4265 % 370 in Case 1 to 5.8738 % in Case 2 when the transient measurements consider heat soakage. Moreover, the maximum 371 error during the entire transient maneuver is 13.3647 in Case 2 at 3.0 s for $X_{FAN,E}$. The consideration of heat soakage 372 in the engine measurements will delay the prediction of the maximum degradation for all ten degradation indices. 373 Ignoring the heat soakage during transient diagnosis will impact the prediction accuracy during transient conditions. 374 The results of this case study provide important insights into the applicability of the benchmark method for engine 375 transient maneuvers. It becomes clear that using transient measurements in a steady-state approximation fault 376 diagnostic system will have noticeable prediction errors during dynamic operating conditions. Moreover, the shift of 377 diagnostic results is possible to raise a false alarm. If the diagnostic system dispatches frequent false alarms, the fault 378 diagnostic program's confidence will be significantly compromised from an operation and maintenance perspective.





Fig. 11 Average relative error of health parameters during a transient maneuver.



This case study employs the proposed method for fault diagnosis during a transient maneuver while considering heat soakage in the transient engine measurements. Fig. 12 illustrates the relative error of the ten degradation indices during a dynamic maneuver.





Fig. 12 Relative error of degradation indices during a dynamic maneuver.

387 Comparing the results in three cases (Fig. 13) reveals that the proposed method could estimate the health 388 parameters with greater precision than the benchmark method. Table 4 summarises the diagnostic results for all three 389 case studies. The computation time of Case 3 is 0.1567 s which is slightly better than that of Case 2. This is because 390 the maximum allowed iteration steps terminate the diagnostic process; rather than the convergence threshold when 391 affected by surplus power, heat soakage, and lag response during a transient maneuver. The average diagnostic error 392 by the proposed method is 0.0007 % which is superior to the benchmark method (1.5239 % in Case 2). Moreover, the 393 maximum error during the entire transient maneuver is 13.3647 % and 0.0058 % in Cases 2 and 3, respectively. It 394 follows that the proposed time-series fault diagnosis method is superior to the benchmark method in both 395 computational time and prediction accuracy aspects.





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Table 4 Summary of three diagnosis cases.

Parameter	Symbol	Unit	Case 1	Case 2	Case 3
Average Run Time	RT	Second	0.2024	0.1997	0.1567
Average Error	AE	%	0.4224	1.5239	0.0007
Maximum Error	ME	%	6.3396	13.3647	0.0058

401 **3.4** Case 4: Proposed Method - Sudden Failure during Transient Manoeuvre

The aero-engine may be faced with foreign object damage like bird strikes during flight. In such a condition, sudden degradation may happen during the flight. Moreover, the bird strike is more likely to occur during the take-off and landing processes when the engine runs under a transient or quasi-steady-state condition. Hence, it is necessary to verify the capability of the proposed method under sudden failure during dynamic conditions in real-time.

The sudden failure is assumed to happen at the 3.0 s mark during the transient maneuver in Fig. 6 (top). The health state is suddenly changed from 'Health State 1' to 'Health State 2' represented in Table 3. Fig. 14 presents the relative error of diagnostic results obtained from the proposed method during dynamic conditions with sudden failure. It can be seen from Fig. 14 that the proposed method could capture the sudden failure with high prediction accuracy. Fig. 15 compares the results of ten health parameters among all four Cases. The maximum relative error of all ten degradation indices is less than 0.0059 % in Case 4. It is evident that the relative error of all health parameters with sudden failure in Case 4 is similar to that of Case 3.

413 Table 5 presents the diagnostic results of all four Cases. The average computation time of Case 4 is only 0.1582 s 414 which amplifies the suitability of the proposed method for real-time implementation. It is worth noting that the computation time of Case 4 is similar to Case 3. The sudden failure does not affect the computational efficiency of 415 the proposed method. From the perspective of diagnostic accuracy, the average and maximum errors for all ten health 416 417 parameters during the dynamic maneuver are 0.0009 % and 0.0059 %, respectively. The maximum error is observed 418 at 3.6 s for $X_{FAN,E}$ and the sudden failure is taking place at 3.0 s, which means that the proposed algorithm is not 419 compromised when dealing with sudden failures. The average and maximum errors of Case 4 are similar to those of 420 Case 3. The sudden failure during the dynamic condition also does not affect diagnostic accuracy.

In summary, the results demonstrate and illustrate that the proposed method is capable of diagnosing the engine health state with time-series data at both steady-state and dynamic conditions in real-time, even when there are sudden faults during transient conditions.



Fig. 14 Relative error of degradation indices during dynamic maneuver.



Parameter	Symbol	Unit	Case 1	Case 2	Case 3	Case 4
Average Run Time	RT	Second	0.2024	0.1997	0.1567	0.1582
Average Error	AE	%	0.4224	1.5239	0.0007	0.0009
Maximum Error	ME	%	6.3396	13.3647	0.0058	0.0059

Despite the dynamic effect of rotor inertia, heat soakage and lag response during transient maneuver, the volume dynamic does not engage with the proposed method which may affect the diagnostic precision when very small-time step is selected. The volume dynamic is suggested to be considered in future work. However, it is worth noting that the effect of volume dynamics is less important when compared with the three dynamic effects mentioned in this study unless a limited time step is employed in the diagnostic system. Moreover, Further studies are suggested to integrate the proposed method with the aircraft and gas turbine starting models to track the engine health state from engine start until engine shut down during the whole aircraft mission. The health monitoring system could provide a real fault diagnosis in real-time on-wing, improving aircraft engine reliability, availability, and safety in such a condition.

4. Conclusions

This study is designed to provide the first systematic account of aero-engine transient characteristics during fault diagnosis in time-series data to fill the research gap in engine fault diagnosis under dynamic conditions. The findings clearly indicate that the proposed method could accurately diagnose the engine fault level under dynamic conditions. The most prominent finding to emerge from this study is that the sudden failure during transient conditions could be quantified correctly in real-time. In general, this study strengthens the idea that the proposed method could address the fault diagnosis of aero-engine in real-time under both stable and dynamic conditions.

The conclusions extracted from this study are below:

- When the heat soakage phenomenon during a dynamic condition is not considered, the diagnosis results 447 predicted by the benchmark method come with a maximum error of 6.3396 %. Moreover, the predicted 448 degradation indices fluctuate during a transient maneuver.
- The maximum diagnostic error has increased to 13.3647 during the entire transient maneuver when
 considering the heat soakage phenomenon in engine gas path measurements. It is clear to see that the
 benchmark method cannot provide correct results for the test cases.
- The proposed method could take both surplus power, heat soakage, and lag response into consideration. The
 maximum error of the health parameter is only 0.0058 % under a constant health state during transient
 conditions with a computation time of 0.1567 s.
- More importantly, the proposed method could also diagnose the sudden failure during transient maneuvers
 with a maximum error of 0.0059 % in 0.1582 s.

Before this study, the challenging real-time determination of the aero-engine fault level in dynamic conditions had not been investigated in detail. The present study extends our knowledge of turbofan engine fault diagnosis under dynamic conditions. A key strength of the present study is the fault diagnosis of sudden failure under transient maneuvers.

461 Overall, the findings of this investigation complement those of earlier studies of engine fault diagnosis under 462 dynamic maneuvers in real-time. These findings contribute in several ways to our understanding of aero-engine fault 463 diagnosis and benefit engine safety, availability, and reliability.

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Highlights

- A novel real-time successive fault diagnosis method is proposed.
- Time-series data consider the transient effect in gas path measurements.
- Constant engine degradation could be monitored with high accuracy in real-time.
- Sudden failure during dynamic conditions could be captured with great precision.
- The proposed method is far better than the benchmark method.

(maximum 85 characters, including spaces, per bullet point, 3-5 bullet points)

Declaration of interests

 \square The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

□ The authors declare the following financial interests/personal relationships which may be considered as potential competing interests:

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