Exploiting Impacts of Antenna Selection and Energy Harvesting for Massive Network Connectivity

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Abstract—As a new energy saving approach for green communications, energy harvesting (EH) could be suitable technique to facilitate massive connections for large number of devices in such networks. The spectrum shortage occurs in huge number of devices which access with small-cell and macro-cell networks. To tackle these challenges, we develop a tractable framework relying on prominent techniques such as non-orthogonal multiple access (NOMA), antenna selection and energy harvesting. In this paper, we aim at practical scenarios of small cell networks by jointly evaluating capable of interference management and EH. We benefit from transmission approaches including full duplex (FD) and bi-directional transmission to improve the main performance system metrics such as outage probability and throughput. Three useful schemes are explored by considering EH and inter-cell interference. We derive the closed-form and asymptotic expressions for system metrics. We then perform extensive simulations with different system configurations to confirm the effectiveness of the proposed small-cell NOMA systems.

Index Terms—Small-cell, transmit antenna selection, outage probability, non-orthogonal multiple access.

I. INTRODUCTION

Various kinds of orthogonal multiple access (OMA) schemes are usually employed in current wireless communication systems, and these techniques are classified following time division, frequency division, and code division for multiple access function. In such schemes, to avoid possible multi-user interference multiple users are served, in which one mobile user (MU) is entirely assigned by one resource block. In practice, although the cost of low spectral efficiency, the OMA schemes are relatively easy to deploy. Benefiting from the superior performance of spectrum utilization, NOMA has attracted attentions due to advantages of massive connectivity and low latency [1, 2, 3]. Different from the traditional OMA, power is high popularity in research compared with time-based or frequency domain-based NOMA schemes [4, 5]. To enabling domain-based NOMA scheme, different power levels are allocated for group of users in NOMA networks and such allocation strategy depends on their channels or requirements, and then their signals are superposed at transmit side over the same channel [6]. At receiver side, to eliminate the co-channel interference, successive interference cancellation (SIC) is implemented and the expected message can be extracted from the received signals [7, 8].

A. Related Work and Motivation

Small-cell networks in heterogeneous networks (HetNets) have been researched to achieve improvements in terms of the ubiquitous service and the system capacity. However, the deployment of massive terminals in numerous small-cell meets several intractable challenges in terms of the energy consumption. The dense implementation of small networks for 5G and beyond networks pose new further challenges regarding energy-efficient network management and spectrum efficiency.

By considering the applications of NOMA in HetNet, Liu et al. [9] proposed a hybrid HetNet, where macro cells need massive multiple-input-multiple-output (MIMO) transmission while small cells implement NOMA transmission. It could be interesting result as conducting NOMA in HetNet provides better performance in comparison with the traditional OMA-based HetNet. Liu et al. [10] proposed non-cooperative and cooperative schemes to evaluate coverage performance of the HetNet in downlink, and they indicated that coverage improvement of all NOMA users is resulted from design of cooperative NOMA in the situation each NOMA user needs proper power allocations. The spectrum-efficiency improvement in NOMA is also beneficial to small/macro cells since multiple MUs’ offloading operating the same channel [11]. The authors in [12] derived the average successful transmission probability by implementing analysis from stochastic geometry, and this model together with opportunistic NOMA transmissions are employed in small cell networks. The subchannel allocation and power allocation are performed to achieve maximal energy efficiency (EE) for the a NOMA HetNet system containing small cells and macro-cell [13]. They considered a mixed non-integer convex optimization problem by determining the cross-tier interference and co-channel interference, and then they studied the problem of energy efficient resource allocation [13]. Different channel gains to users in small-cell network using NOMA with SIC due to the difference location of base stations (BSs), and hence, pairing the right BS with a MU is important [14]. They concerned problem of controlling its transmit power in the uplink.

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Design of multiple antennas at the BS benefits to wireless network even if MUs fabricated with a single antenna. Both the BS and the MUs are equipped multiple-antenna to introduce more general architecture as in [15]. In particular, a signal alignment scheme was proposed to mitigate interference existing in both the intra-cluster and inter-cluster. Furthermore, multiple input multiple output system has been designed in new architecture as combining NOMA scheme herein, namely MIMO-NOMA, to benefit the spatial degrees of freedom [16, 17, 18, 19, 20]. For reduced cost of deployment of NOMA-based system, the antenna selection (AS) technique has been introduced as an effective scheme to avoid the high hardware costs, demanding power consumption and heavy computational while maintaining benefits from MIMO in terms of the diversity and throughput [21, 22, 23]. There are only a few papers that considered the AS problem for MIMO-NOMA systems in the open literature. Specifically, advantages of a transmit AS (TAS) algorithm reported in [24, 25] should be included in NOMA networks together with their analytical characterizations of the system performance.

Besides, EE in wireless networks containing energy limited devices has attracted increasing attention [26]. Two different directions of researches can be investigated with respect to improve energy-efficient. The first group of previous paper considered on finding optimal EE [27]. In [28], system performance in a NOMA system is optimized in term of an EE power allocation strategy and they introduced a low-complexity sub-optimal scheme including power allocation and subchannel assignment. The second direction lies in EH. Recently, to enhance of the wireless communication networks in term of the EE, RF signals have been evaluated as viable new sources to implement EH as recent works in [29, 30, 31, 32, 33, 34]. Motivated by these approaches, we design linear EH in the perspective of HetNet manner.

Spectrum efficiency, EE, and outage probability could be considered three important characteristics of each HetNet system where the trade-off among them should be investigated. Recently, it is predicted that future HetNets should be able to provide massive connectivity to adapt to the fast improvement of mobile internet and proliferation of mobile devices. It is worth pointing out that such networks require an extremely provocative task for the OMA schemes due to limited radio resources. On the other hand, cell-edge users need to replenish to retain their operations. To address these challenges, by considering the energy harvesting approach, we propose different problem formulations based on advances of NOMA strategy that maximize benefits as concerned. Although the higher number of antennas provides the higher system capacity and the higher amount of harvested energy, but these advantages require at higher cost of radio-frequency (RF) chains, computational complexity, and high power consumption such higher costs happen at both the transmitter and receivers in term of signal processing. Therefore, TAS is adopted to relax cost of hardware design. To the best of our knowledge, this is the first work which investigates the NOMA based HetNet with considering energy harvesting and TAS architecture.

B. Main Contributions

Although the authors in [35] indicated the benefits of NOMA incorporated in small-cell networks with hybrid automatic repeat request (HARQ), energy shortage needs be considered. Therefore, our study focus on EH to wireless charge for large number of small devices. The similar work considered in [36] regarding a downlink NOMA to implement HetNet. In their system model, the macro BS (MBS) enables wireless backhaul to co-work with multiple small cell BSs (SBSs). The NOMA users can be grouped associated with small cell and the corresponding SBS [36]. From the system explored in [36], we can observe that achieved EE depends on the number of SBSs per MBS. However, the system performance relies on the effect of severe interference when MBS co-works with too many small cells. This motivated us to address such impact of interference. Reference [37] proposed mmWave-NOMA transmission for a machine-to-machine (M2M) network under the context of HetNet. In such, the same resource block can be shared among small-cell users (SCUs) and machine type communication (MTC) devices. In the mentioned work [37], only NOMA user pairs communicate with the SBSs. Further capable of bi-directional transmission among two NOMA user pairs was not well studied. In contrast, our paper examines benefit of bi-directional transmission mode, linear EH in the downlink small-cell to serve better performance for user pairs.

The main contributions are summarized as follows:

1) We consider the NOMA to support bi-direction transmission in the context of a HetNet. The NOMA technique allows the multiple antenna-assisted BS to serve users at different power level allocated. To the authors’ best knowledge, this is the first work that considers performance of typical scenarios in small-cell NOMA.

2) Due to the dense unplanned deployments of small cells, loud neighbors, and the closed subscriber group access, HetNet often meets worse performance since inter-interference. Therefore, this paper examines three scenarios related ability of EH, interference between macro-cell users (MCUs) and SCUs. Under impact of interference, a general framework in this paper is necessary to evaluate performance metrics.

3) We derive the closed-form expressions of the outage probability. Under different designs of proposed schemes, we optimally allocate the power level to each user and percentage of harvested power such that the outage probabilities are minimized. In addition, comparing three schemes in this paper provides guidelines as joint deployments of linear EH, small-cell, NOMA schemes.

The rest of this paper is organized as follows. Section II describes the NOMA to support bi-directional transmission. In Section III, we consider the scenario of downlink NOMA in which only NOMA users communicate without impact of interference from normal cellular users and analyze the outage performance. In Section IV present Scheme 2 for case of degradation performance at NOMA users under interference impact from the normal cellular user. While EH is further
provided to remain operation of NOMA users in case of limited-power at such users and Scheme 3 describes in section V for such situation. We conduct extensive simulations in Section VI, and Section VII concludes the paper.

II. SYSTEM MODEL

Consider cellular downlink communications in small-cell network in which SBS transmits superimposed signals to two full-duplex NOMA users simultaneously, shown in Fig. 2(a), Fig. 2(b) and Fig. 2(c). In this scenario, two users can communicate to each other in Scheme 1. To look on impact of interference from the MCU on both end user 1 and user 2, we introduce a framework as Scheme 2. In addition, EH approach benefits to the links between the MBS and two NOMA users, which case is presented in Scheme 3. The SBS is equipped antennas while MCU and two SCUs are with single antenna. We need two phases to proceed a signal frame, each phase is T/2. The main parameters and functions can be found in the Table II.

Initially, the two users’ superposed information is proceeded to serve users, i.e. User 1 and User 2 are denoted by D1 and D2, respectively. Which are in degraded performance with and without interference from macro cells. In the second phase related to bi-directional connection, D1 transmits information to D2 and vice versa. Two users D1, (i = 1, 2) are capable of EH or not.

III. SCHEME 1: SEPARATE SMALL-CELL

The signal received by user D1, (i = 1, 2) is given by

\[ y_{D1}^{s1} = g_{i,k} \left( \sqrt{a_1 P_S} x_1 + \sqrt{a_2 P_S} x_2 \right) + w_i, \]  \hspace{1cm} \text{ (1)}

where satisfying \( a_1 + a_2 = 1 \). We assume that user D1 is located at far distance compared with another, and hence higher potion of power needs be assigned to user D1, i.e. condition \( a_1 > a_2 \) must be guaranteed. Further, those factors are determined by the quality of the channel coefficients. It is further assumed a normalized unit power at the SBS, \( E \{ |x_i|^2 \} = 1 \). In this scenario, users D1 and D2 are the non-SIC user and SIC user, respectively.

Then, the received signal to interference plus noise ratio (SINRs) at user D1 can be formulated as

\[ \gamma_{1,k} = \frac{a_1 \rho |g_{1,k}|^2}{a_2 \rho |g_{2,k}|^2 + 1}. \]  \hspace{1cm} \text{ (2)}

\footnote{We study similar scenario of the downlink transmission in a two-tier network as reported in [36]. Such system model in [36] contains one MBS in the macro-cell tier and some SBSs. However, performance of several SBSs are similar, and thus we focus on performance analysis for a SBS.}

\[ \text{In term of SIC user, the SINR to detect } x_1 \text{ and the received SNR at user } D_2 \text{ is given by } \]

\[ \gamma_{1+2,k} = \frac{a_1 \rho |g_{2,k}|^2}{a_2 \rho |g_{2,k}|^2 + 1}, \quad \gamma_{2,k} = a_2 \rho |g_{2,k}|^2. \]  \hspace{1cm} \text{ (3)}

In this phase, the user with a stronger channel gain and the user with a weaker gain need cooperate. Designing bidirectional link can assist user D1 to decode its data, or user D2 to operate SIC better. In such situation, received signal obtained by user D1 is expressed as

\[ z_{D1}^{s1} = \sqrt{P_{D1}} h_{i} x_i + \sqrt{\bar{\alpha}} P_{D1} f X_{FDI} + w_i, \]  \hspace{1cm} \text{ (4)}

where \( \bar{\alpha} = 1 \) denotes user D1 working in FD.

Regarding condition to exist such received signal, when \( |g_{1,k}|^2 > |g_{2,k}|^2 \), only \( z_{D1}^{s1} \) happens, and when \( |g_{1,k}|^2 < |g_{2,k}|^2 \), only \( z_{D2}^{s1} \) is transmitted from user D2. Then, the received SINR at user D1 is given by

\[ \chi_{1}^{s1} = \frac{\rho |h_{i}|^2}{\bar{\alpha} |f|^{2} + 1}. \]  \hspace{1cm} \text{ (5)}

TABLE I: Comparison of the proposed scheme with similar ideas.

<table>
<thead>
<tr>
<th>Scheme</th>
<th>Our Scheme</th>
<th>[3]</th>
<th>[7]</th>
<th>[8]</th>
<th>[37]</th>
<th>[39]</th>
<th>[40]</th>
<th>[43]</th>
</tr>
</thead>
<tbody>
<tr>
<td>Best AS at SBS</td>
<td>x</td>
<td>x</td>
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<td>Full-Duplex</td>
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<tr>
<td>Bi-Directional signal</td>
<td>x</td>
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<tr>
<td>Impact of interference</td>
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<td>x</td>
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<tr>
<td>EH-assisted users</td>
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<tr>
<td>Outage probability</td>
<td>x</td>
<td>x</td>
<td>x</td>
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TABLE II: Definitions of Notations.

<table>
<thead>
<tr>
<th>Notations</th>
<th>Meaning</th>
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<tbody>
<tr>
<td>( f(x) ), ( F_X(.) )</td>
<td>The probability distribution function (PDF), Cumulative distribution function (CDF)</td>
</tr>
<tr>
<td>( C \sim (a, b) )</td>
<td>Complex normal distribution with mean ( a ) and variance ( b )</td>
</tr>
<tr>
<td>( a_i, d_i, \alpha )</td>
<td>The power allocation factors to ( i )-th user, normalized distances from SBS to ( D_i ), path loss exponent</td>
</tr>
<tr>
<td>( \eta, \beta )</td>
<td>The energy conversion coefficient with ( 0 &lt; \eta &lt; 1 ), the power splitting ratio ( 0 &lt; \beta &lt; 1 )</td>
</tr>
<tr>
<td>( T, K, \omega )</td>
<td>The whole signal frame, number of transmission antennas, conversion operation between FD/half-duplex(HD) each other</td>
</tr>
<tr>
<td>( P_{S1}, P_{D1}, P_{R} )</td>
<td>The normalized transmission powers at the SBS, at the ( D_i ), (i = 1, 2), transmit power from MCU to ( D_i )</td>
</tr>
<tr>
<td>( w_i )</td>
<td>Noise for user ( D_i ), i.e. ( w_i \sim C N (0, N_0) ) with ( N_0 ) is the normalized noise variance</td>
</tr>
<tr>
<td>( \rho )</td>
<td>The transmit signal-to-noise ratio (SNR) with ( P_{D} / N_0 )</td>
</tr>
<tr>
<td>( x_{i}, X_{FDI}, X_{R} )</td>
<td>Transmit symbols for user ( D_i ), loop interference signal at the ( D_i ), signal transmitting from MCU to ( D_i )</td>
</tr>
<tr>
<td>( R_i )</td>
<td>The target data rate of ( D_i )</td>
</tr>
<tr>
<td>( g_{i,k}, (i = 1, 2) )</td>
<td>The Rayleigh fading channel coefficients of corresponding links SBS-Di with average power of ( \lambda_i = d_i )</td>
</tr>
<tr>
<td>( l_i, (i = 1, 2) )</td>
<td>The Rayleigh fading channel coefficients of corresponding links MCU-D1 with average power of ( \lambda_1 )</td>
</tr>
<tr>
<td>( h_i )</td>
<td>The Rayleigh fading channel coefficients of corresponding links D2-D1 with average power of ( \lambda_{h1} )</td>
</tr>
<tr>
<td>( h_{2} )</td>
<td>The Rayleigh fading channel coefficients of corresponding links D1-D2 with average power of ( \lambda_{h2} )</td>
</tr>
<tr>
<td>( f_1 )</td>
<td>The Rayleigh fading channel coefficients of corresponding links D1-D2 with average power of ( \lambda_{f1} )</td>
</tr>
<tr>
<td>( f_{2} )</td>
<td>The Rayleigh fading channel coefficients of corresponding links D2-D2 with average power of ( \lambda_{f2} )</td>
</tr>
</tbody>
</table>
Here, if a certain user receives the cooperation signal, the direct transmission and bi-directional transmission joint provide the better of the signals received. The SINR for decoding $x_1$ given by

$$\rho_{s1D1} = \begin{cases} \min \{ \max \{ \gamma_{s1}^{1,k}, \chi_{s1}^{1,k} \}, \gamma_{s2}^{1,k} \} & \text{if } |g_{1,k}|^2 < |g_{2,k}|^2 \\ \min \{ \gamma_{s1}^{1,k}, \max \{ \gamma_{s2}^{1,k}, \chi_{s2}^{1,k} \} \} & \text{otherwise.} \end{cases} \quad (6)$$

Since only $x_1$ is shared for cooperation, the SINR for decoding $x_2$ is $\rho_{s1D2} = \gamma_{s2,k}^{1}$ and the data rate of $x_1$ in bi-directional cooperative NOMA becomes $R_{s1D_2} = \log_2 (1 + \rho_{s1D2})$.

The antenna element can be selected to strengthen the link between the SBS and user $D_i$ as follow $k^* = \arg \max_{k=1,...,K} (|g_{i,k}|^2), (i = 1, 2)$ [38].

The selected channel has CDF, and PDF of $|g_{i,k^*}|^2$ respectively as [39]

$$F_{|g_{i,k^*}|^2} (x) = 1 - \sum_{k=1}^{K} \binom{K}{k} (-1)^{k-1} \exp \left( -\frac{kx}{\lambda_i} \right), \quad (7)$$

$$f_{|g_{i,k^*}|^2} (x) = \sum_{k=1}^{K} \binom{K}{k} (-1)^{k-1} \frac{k}{\lambda_i} \exp \left( -\frac{kx}{\lambda_i} \right). \quad (8)$$

### A. Outage probability of user 1 in Scheme 1 using FD mode

We evaluate system performance under condition of the predefined data rates $R_{s1D_1}$ and $R_{s1D_2}$, and they are determined by the users’ QoS requirements. More importantly, the outage probability is considered as an important performance criterion. Depending ability of decode processing, condition of outage behavior happens based on capability of $\gamma_{1+2,k^*}$ compared with condition of required rates. It is noted that outage event occurs at the non-SIC user or the SIC user regarding using the cooperation signal from bidirectional link.

The outage probability at the non-SIC user 1 in this scheme...
given by [40]

\[ OP_{D_1}^{f-s} = \Pr \left( \gamma_{1,k^*}^s < \varepsilon_f^s \cap \gamma_{1-2,k^*}^s < \varepsilon_f^s \right) \]

\[ + \Pr \left( \max \left\{ \gamma_{1,k^*}^s, \gamma_{1-2,k^*}^s \right\} > \varepsilon_f^s \right). \]

**Proposition 1:** The outage probability at user 1 in closed-form \( OP_{D_1}^{f-s} \) is computed by

\[ OP_{D_1}^{f-s} = \left( 1 - \xi_f^s \right) \left( 1 - \xi_h^s \right) + \left( 1 - \xi_f^s \right) \times \left[ 1 - \exp \left( - \frac{\epsilon_f}{\lambda_{h_1}} \right) \right] \xi_h^s, \]

where \( \xi_f^s = 2^{R_1} - 1, \xi_h^s = 2^{R_2} - 1 \), \( \psi^q = \frac{\epsilon_f^q}{\rho} \), \( \xi^q = \sum_{k=1}^{K} \left( -1 \right)^{k-1} \left( 1 - \xi_f^s \right) \left( 1 - \xi_h^s \right) \).

**Proof:** Please refer to Appendix A.

**B. Outage probability of user 1 in Scheme 1 using HD mode**

Based on results from (9) and (10) outage probability of user 1 in Scheme 1 can be computed as

\[ OP_{D_1}^{h-s} = \left( 1 - \xi_h^s \right) \left( 1 - \xi_f^s \right) + \left( 1 - \xi_f^s \right) \times \left[ 1 - \exp \left( - \frac{\epsilon_f}{\lambda_{h_1}} \right) \right] \xi_h^s. \]

**C. Outage probability of user 2 in Scheme 1 using FD mode**

Consider the outage probability of \( D_2 \) in small-cell network employing NOMA. If the outage event does not happen at \( D_1 \), then \( D_2 \) can more opportunity to receive cooperation signal transmitted from \( D_1 \). It is noted that \( D_2 \) requires SIC process. In worse case, transmission from \( D_1 \) to \( D_2 \) in bidirectional link cannot be performed if the \( D_1 \)’s data rate is less than \( R_{D_1}^s \). As a result [40], outage probability of \( D_2 \) is expressed as

\[ OP_{D_2}^{f-s} = \Pr \left. \left( \gamma_{1,k^*}^s < \varepsilon_f^s \cup \gamma_{1-2,k^*}^s < \varepsilon_f^s \right) \right|_{B_1} \]

\[ + \Pr \left. \left( \gamma_{1,k^*}^s < \varepsilon_f^s \cup \max \left\{ \gamma_{1,k^*}^s, \gamma_{1-2,k^*}^s \right\} > \varepsilon_f^s \right) \right|_{B_2}. \]

**Proposition 2:** The closed-form formula to show the outage probability \( OP_{D_2}^{f-s} \) at \( D_2 \) is

\[ OP_{D_2}^{f-s} = \left[ 1 - \sum_{k=1}^{K} \left( 1 - \xi_f^s \right) \left( 1 - \xi_h^s \right) \right. \]

\[ \times \left[ 1 - \exp \left( - \frac{\epsilon_f}{\lambda_{h_1}} \right) \right] \xi_h^s, \]

where \( \theta^q = \max \left( \frac{\epsilon_f^q}{\alpha}, \frac{\epsilon_f^q}{\beta} \right), \delta^q = \frac{\epsilon_f^q}{\rho} \).

**D. Outage probability of user \( D_2 \) in Scheme 1 using HD mode**

In similar way, it can be obtained outage probability \( D_2 \) in scheme 1 at HD mode as

\[ OP_{D_2}^{h-s} = \left[ 1 - \sum_{k=1}^{K} \left( 1 - \xi_f^s \right) \left( 1 - \xi_h^s \right) \right. \]

\[ \times \left[ 1 - \exp \left( - \frac{\epsilon_f}{\lambda_{h_1}} \right) \right] \xi_h^s, \]

\[ \left. + \left( 1 - \mu_f^s \right) \left( 1 - \xi_h^s \right) \left( 1 - \eta_f^s \right) \right) \right) \xi_h^s. \]

**IV. SCHEME 2: IMPACT OF INTERFERENCE FROM MCU ON BIDIRECTIONAL USERS**

In case of existence of interference from the MCU to two NOMA users, the received signal can be obtained at \( D_1, (i = 1, 2) \)

\[ y_{D_1}^{s} = g_{i,k} \left( \sqrt{a_1 \rho_{S|x_1}} + \sqrt{a_2 \rho_{S|x_2}} \right) + \sqrt{P_R} l_i x_R + w_i. \]

Then, the received SINDs at user \( D_1 \) is computed as

\[ \gamma_{i,k}^{s2} = \frac{a_1 \rho |g_{i,k}|^2}{a_2 \rho |g_{i,k}|^2 + \rho |l_i|^2 + 1}. \]

The SINR for SIC user to detect \( x_1 \) and the received SINDs at user \( D_2 \) is given by

\[ \gamma_{i,k}^{s2} = \frac{a_2 \rho |g_{i,k}|^2}{a_1 \rho |g_{i,k}|^2 + \rho |l_i|^2 + 1}. \]

In this phase, the user with a stronger channel gain and the user with a weaker gain need cooperate. Designing bidirectional link can assist user \( D_1 \) to decode its data, or user \( D_2 \) to operate SIC better. In such situation, received signal obtained by user \( D_i \) is expressed as

\[ y_{D_1}^{s2} = \sqrt{P_{D_1} h_i x_i} + \sqrt{\rho \rho_{S|x_F}} + \sqrt{P_{D_1} l_i x_R} + w_i. \]

Then, the received SINR at user \( D_i \) is given by

\[ \gamma_{i,k}^{s2} = \frac{\rho |h_i|^2}{\rho |f_i|^2 + \rho |l_i|^2 + 1}. \]

**A. Outage probability of user 1 in Scheme 2 using FD mode**

In Scheme 2, the outage probability of user 1 in FD mode is given as

\[ OP_{D_1}^{f-s} = \Pr \left( \gamma_{i,k}^{s2} < \varepsilon_f^s, \gamma_{i-2,k}^{s2} < \varepsilon_f^s \right) \]

\[ + \Pr \left( \max \left\{ \gamma_{i,k}^{s2}, \gamma_{i-2,k}^{s2} \right\} < \varepsilon_f^s \right). \]
Proposition 3: The outage probability $OP_{D1}^{f-s_2}$ at user $D_1$ can be formulated by

$$OP_{D1}^{f-s_2} = \left(1 - \vartheta_1^{\prime}\right) \left(1 - \vartheta_2^{\prime}\right) + \left(1 - \vartheta_1^{\prime}\right) \vartheta_2^{\prime} \times \left[1 - \frac{\lambda_1}{\epsilon_1^{\prime} + \lambda_1 + \lambda_2} \exp \left(-\frac{\epsilon_1^{\prime}}{\rho \lambda_1}\right)\right],$$

(21)

where $\vartheta_i^{\prime} = \frac{K}{k} (-1)^{k-1} \frac{(a_i - \epsilon_i^{\prime} a_2)_{\lambda_1}}{k \epsilon_i^{\prime} a_1 + (a_i - \epsilon_i^{\prime} a_2)_{\lambda_1}} \exp \left(-\frac{\epsilon_i^{\prime}}{\rho \lambda_1}\right)$, $i \in \{1, 2\}$.

Proof: Please refer to Appendix C.

B. Outage probability of user 1 in Scheme 2 using HD mode

Lack of self-interference channel due to FD mode, the considered system in HD mode results in other form of outage probability and then relying on results in (20) and (21), outage probability $D_1$ in Scheme 2 at HD mode is formulated as

$$OP_{D1}^{h-s_2} = \left(1 - \vartheta_1^{h}\right) \left(1 - \vartheta_2^{h}\right) + \left(1 - \vartheta_1^{h}\right) \vartheta_2^{h} \times \left[1 - \frac{\lambda_1}{\epsilon_1^{h} + \lambda_1 + \lambda_2} \exp \left(-\frac{\epsilon_1^{h}}{\rho \lambda_1}\right)\right].$$

(22)

C. Outage probability of user 2 in Scheme 2 using FD mode

The outage probability of user 2 in Scheme 2 at FD mode can be computed and final result is presented in the following proposition.

$$OP_{D2}^{f-s_2} = \Pr \left[\{\gamma_2^{f,k} < \epsilon_2^{f} \cup \gamma_2^{f,1-2,k^*} < \epsilon_1^{f}\} , \gamma_1^{f,k} < \epsilon_1^{f}\right] + \Pr \left[\gamma_2^{f,k} < \epsilon_2^{f} \cup \max \{\gamma_2^{f,1-2,k^*}, \gamma_2^{f,1-2,k^*}\} < \epsilon_1^{f}\right].$$

(23)

Proposition 4: The closed-form expression of the outage probability $OP_{D2}^{f-s_2}$ is formulated as

$$OP_{D2}^{f-s_2} = \left(1 - \Omega_1^{q}\right) \left(1 - \Omega_2^{q}\right) + \left(1 - \psi_1^{q}\right) \left(1 - \psi_2^{q}\right) \vartheta_1^{q},$$

(24)

where

$$\Omega_1^{q} = \sum_{k=1}^{K} \left(\frac{K}{k}\right) (-1)^{k-1} \frac{a_k^{\prime}}{k \epsilon_k^{\prime} + \lambda_2^{\prime}} \exp \left(-\frac{\epsilon_k^{\prime}}{\rho \lambda_2^{\prime}}\right),$$

$$\Omega_2^{q} = \sum_{k=1}^{K} \left(\frac{K}{k}\right) (-1)^{k-1} \frac{(a_1 - \epsilon_1^{\prime} a_2)_{\lambda_1}}{k \epsilon_1^{\prime} a_1 + (a_1 - \epsilon_1^{\prime} a_2)_{\lambda_1}} \exp \left(-\frac{\epsilon_1^{\prime}}{\rho \lambda_1}\right),$$

$$\psi_1^{q} = \sum_{k=1}^{K} \left(\frac{K}{k}\right) (-1)^{k-1} \frac{a_k^{\prime} \lambda_2^{\prime}}{a_2^{\prime} + \epsilon_k^{\prime} \lambda_2^{\prime}} \exp \left(-\frac{\epsilon_k^{\prime}}{\rho \lambda_2^{\prime}}\right),$$

$$\psi_2^{q} = \frac{\lambda_2^{\prime}}{\epsilon_1^{\prime} a_1^{\prime} + \lambda_2^{\prime}} \exp \left(-\frac{\epsilon_1^{\prime}}{\rho \lambda_2^{\prime}}\right).$$

Proof: Please refer to Appendix D.

D. Outage probability of user 2 in Scheme 2 with HD mode

Considering HD mode, such outage probability can be achieved straightforward. Using results in (23) and (24), outage probability $D_2$ in scheme 2 at HD mode is formulated as

$$OP_{D2}^{h-s_2} = \left(1 - \Omega_1^{h}\right) \left(1 - \Omega_2^{h}\right) + \left(1 - \psi_1^{h}\right) \left(1 - \psi_2^{h}\right) \vartheta_1^{h},$$

(25)

in which $\psi_2^{h} = \frac{\lambda_2^{h}}{\epsilon_1^{h} + \lambda_2^{h}} \exp \left(-\frac{\epsilon_1^{h}}{\rho \lambda_2^{h}}\right)$.

V. SCHEME 3: EH-ASSISTED USERS

In this scheme, once MCU is wireless power enabler, $D_i$ can harvest energy from the MCU in the first phase and uses such energy to transmit the signal to $D_i$ in the second phase. It is assumed that the energy harvested from the noise can be ignored. Therefore, according to the power splitting protocol (PS) [41, 42] for EH, the received signal at $D_i$ in the first phase is expressed as

$$y_{D_i}^{3} = g_i \left(\sqrt{a_1} P_{x_1} + \sqrt{a_2} P_{x_2}\right) + \sqrt{(1 - \beta)} P_{nl} l_{x_R} + w_i.$$

(26)

Then the received SINRs at user $D_1$ is computed as

$$\gamma_1^{s_3} = \frac{a_1 \rho |g_1|^{2}}{a_2 \rho |g_2|^{2} + (1 - \beta) |l_1|^{2} + 1}.$$ 

(27)

The SINR for SIC user to detect $x_1$ and the received SINRs at user $D_2$ is given by

$$\gamma_2^{s_3} = \frac{a_2 \rho |g_2|^{2}}{a_2 \rho |g_2|^{2} + (1 - \beta) |l_2|^{2} + 1}.$$ 

(28)

It is assumed that the energy harvested from the noise can be ignored [42, 43] and the harvest energy measured at bidirectional users are expressed by $E = \frac{T}{\eta} \beta \left(P_{nl} l_{x_R} + P_{fl_{x_R}}\right)$.

As a result, the transmit power $E_{fl_{x_R}}$ at user $D_1$ can be expressed as $P_{fl_{x_R}} = \frac{E_{fl_{x_R}}}{\eta \beta |f_2|^{2}}$ [42, 43],

In this phase, $D_i$ uses such energy from MCU to transmit the signal, the user with a stronger channel gain and the user with a weaker gain need cooperate. In such situation, received signal obtained by user $D_i$ is expressed as [41, 42]

$$z_{D_i}^{s_3} = \sqrt{P_{fl_{x_R}}} l_{x_R} + \sqrt{E_{fl_{x_R}}} f_{x_R} + \sqrt{(1 - \beta)} P_{nl} l_{x_R} + w_i.$$ 

(29)

The received SINR at $D_i$ in this circumstance is expressed by

$$\lambda_2^{s_3} = \frac{\eta \beta |l_i|^{2} |h_i|^{2}}{\eta \beta |l_i|^{2} |f_i|^{2} + (1 - \beta) (1 - \eta \beta |f_i|^{2}) |l_i|^{2} + (1 - \eta \beta |f_i|^{2})}.$$ 

(30)

A. Outage probability of user 1 in Scheme 3 using FD mode

In this situation, the outage probability user 1 in Scheme 3 is defined by

$$OP_{D1}^{f-s_3} = \Pr \left[\gamma_1^{s_3} < \epsilon_1^{f}, \gamma_1^{s_3} < \epsilon_1^{f}, \gamma_1^{s_3} < \epsilon_1^{f}\right] E_i$$

$$+ \Pr \left[\max \{\gamma_1^{s_3}, \lambda_1^{s_3}\} < \epsilon_1^{f}, \gamma_1^{s_3} < \epsilon_1^{f}\right] E_i.$$ 

(31)

Proposition 5: The exact expression is derived to indicate the outage probability $OP_{D1}^{f-s_3}$ as

$$OP_{D1}^{f-s_3} = \left(1 - \Phi_1^{f}\right) \left(1 - \Phi_2^{f}\right) + \left(1 - \Phi_1^{f}\right) \Phi_2^{f} \left(1 - \gamma_1^{s_3}\right),$$

(32)
where $\Phi_i = \sum_{k=1}^{K} f_K^{(k)} \exp\left(-\frac{\gamma_i}{\eta_i} \frac{1}{y_i} \right)$. 

Expanding the above expression, we have

$$\int_0^\infty \exp\left(-\frac{\gamma_i}{\eta_i} \frac{1}{y_i} \right) dy = \frac{\eta_i}{\gamma_i}.$$

**Proof:** Please refer to Appendix E.

### B. Outage probability of user 1 in Scheme 3 using HD mode

It is assumed that the energy harvested from the noise can be ignored [42, 43] and the harvest energy measured at bidirectional users for HD are expressed by $E_h = \frac{T}{2} \eta_i^{k} P_R|l_i|^2$. Then, the transmitted power $P_D = \frac{\eta_i}{T/1+2}$ at $D_1$ for HD can be expressed as $P_D = \eta_i^{k} P_R|l_i|^2$.

In this phase, $D_1$ uses such energy from MCU to transmit the signal, the user with a stronger channel gain and the user with a weaker gain need cooperate. In such situation, received signal obtained by $D_1^n$ for HD is expressed as

$$z_{D_1}^{h,s-3} = \sqrt{P_D^n h_{i} x_i + (1-\beta)^T P_R x_i} + w_i [41, 42].$$

Then, the transmitted power $P_D$ in this circumstance is expressed by

$$\chi_i^h = \frac{\eta_i}{\gamma_i} \frac{1}{y_i} \frac{1}{y_i}.$$

In this situation, the outage probability $\gamma_i$ in Scheme 3 for HD is defined by

$$OP_{D_1}^{h,s-3} = \Pr\left(\gamma_i < \epsilon_i^h, \gamma_i^k < \epsilon_i^h \right)$$

$$+ \Pr\left(\max\left\{\gamma_i^k, \gamma_i^s \right\} < \epsilon_i^h \right).$$

From (33), $F_1$ is computed similarly as $E_1$, $F_1$ is given by $F_1 = (1 - \Phi_i^h) (1 - \Phi_i^s)$. By using this way, $F_2$ can be calculated by

$$F_2 = \Pr\left(\gamma_i^s < \epsilon_i^h \right) \Pr\left(\gamma_i^k < \epsilon_i^h \right) \Pr\left(\gamma_i^s < \epsilon_i^h \right) = \Pr\left(\gamma_i^s < \epsilon_i^h \right) \Pr\left(\gamma_i^k < \epsilon_i^h \right).$$

where $F_2$ in (34) can be expressed as $F_1$. Furthermore, $F_2$ can be calculated as

$$F_2 = \Pr\left(\gamma_i^s < \epsilon_i^h \right) \Pr\left(\gamma_i^s < \epsilon_i^h \right) \Pr\left(\gamma_i^s < \epsilon_i^h \right) = \Pr\left(\gamma_i^s < \epsilon_i^h \right) \Pr\left(\gamma_i^s < \epsilon_i^h \right).$$

For $F_2$, the outage probability performance of $D_1$ in Scheme 3 at HD mode can be formulated by

$$OP_{D_1}^{h,s-3} = (1 - \Phi_i^h) (1 - \Phi_i^s) + (1 - \Phi_i^k) \Phi_i^k (1 - \gamma_i^s).$$

### C. Outage probability of user 2 in Scheme 3 using FD

#### Proposition 6: The outage probability user $D_2$ in scheme 3 at FD mode can be addressed as

$$OP_{D_2}^{h,s-3} = (1 - \Theta_i^f) \left(1 - \Theta_i^f \right)$$

$$+ \left(1 - \Xi_i \right) \left(1 - \Phi_i^f \right) (1 - \gamma_i^s).$$

**Proof:** Please see Appendix F.

### D. Outage probability user 2 in Scheme 3 using HD

Based on (35), (37) it can be achieved outage probability

$$OP_{D_2}^{h,s-3} = (1 - \Theta_i^h) \left(1 - \Theta_i^h \right) + \left(1 - \Xi_i \right) \left(1 - \Phi_i^h \right) (1 - \gamma_i^s).$$

### E. Asymptotic Analysis

In order to obtain more insights, we analyze the asymptotic outage probability performance at high SNR by using $\rho \to \infty$. The asymptotic outage probability of $D_1$ and $D_2$ for FD/HD are given by

$$OP_{D_1}^{h,s-3} = (1 - \Theta_1^h) \left(1 - \Theta_1^h \right) + \left(1 - \Xi_1 \right) \left(1 - \Phi_1^h \right) \Phi_2^h (1 - \gamma_1^s).$$

**Proof:** Please see Appendix F.

### F. The overall outage probability of the system for 3 Schemes

The overall outage probability of the system can be given by

$$OP_{SYSTEM}^{h,s-3} = 1 - \left(1 - OP_{D_1}^{h,s-3} \right) \left(1 - OP_{D_2}^{h,s-3} \right),$$

where $s = s_1, s_2, s_3$.
TABLE III: Main parameters for our simulations.

<table>
<thead>
<tr>
<th>Parameters</th>
<th>Notation</th>
<th>Values</th>
</tr>
</thead>
<tbody>
<tr>
<td>Power coefficients</td>
<td>({a_1, a_2})</td>
<td>([0.8, 0.2])</td>
</tr>
<tr>
<td>Target rates SNR to decode (x_1) and (x_2)</td>
<td>(R_1 = R_2)</td>
<td>1 (BPCU)</td>
</tr>
<tr>
<td>Energy conversion coefficient ([41, 42])</td>
<td>(\eta)</td>
<td>0.6</td>
</tr>
<tr>
<td>The power splitting ratio ([41, 42])</td>
<td>(\beta)</td>
<td>0.6</td>
</tr>
<tr>
<td>Path loss exponent</td>
<td>(\alpha)</td>
<td>2</td>
</tr>
<tr>
<td>Normalized distances from SBS to (D_1) and SBS to (D_2)</td>
<td>({d_1, d_2})</td>
<td>([0.4, 0.2])</td>
</tr>
<tr>
<td>Average powers</td>
<td>({\lambda_1 = d_1^\alpha, \lambda_2 = d_2^\alpha, \lambda_{f_1} = \lambda_{f_2}, \lambda_{h_1} = \lambda_{h_2}})</td>
<td>([0.4^2, 0.2^2, 0.01, 1])</td>
</tr>
<tr>
<td>Conversion operation between FD/HD</td>
<td>(\omega)</td>
<td>1</td>
</tr>
<tr>
<td>Number of transmission antennas</td>
<td>(K)</td>
<td>5</td>
</tr>
</tbody>
</table>

VI. NUMERICAL RESULTS AND DISCUSSIONS

In this section, we evaluate performance of communication between the SBS and two users \(D_1, D_2\). The main parameters can be considered in Table III except for specific cases. We will verify results achieved from mathematical analysis, then they exhibit several necessary comparisons.

First, in Fig. 3(a), we present the outage probability of a two user in a group in small-cell network with respect to transmit SNR at SBS. It can be seen tight matching curves as comparing Monte Carlo simulation with analytic results. It can be concluded that performance gap among two users is resulted from different power level allocated to users. It is intuitively seen that higher \(a_1\) provides better performance for user \(D_1\). At each user, FD mode exhibits better outage performance compared with that in HD mode. As a result, it is important as selecting different operation mode for user in such small-cell network according to the different SNR levels in practical systems. In Fig. 3(b), it can be seen that the required rate at \(D_2\) make impact on its performance. In this case, increasing transmit SNR provides outage improvement, especially at high SNR outage probability is very small. Other trends of curves can be observed in similar manner as in Fig. 3(a). Fig. 3(c) plots outage probability versus transmit SNR at the SBS \(\rho\) at two cases related to the number of transmit antennas, \(K = 1, 5\). It can be explained that improved outage performance achieved since more antennas are equipped at the SBS. Through this simulation, it can be seen how the number of antennas at the SBS affects the outage performance significantly. It can be confirmed that the best outage performance occurs at the case \(K = 5\) for user \(D_1\) in FD mode.

Fig. 4(a) plots the outage probability of FD/HD NOMA with interference link from MCUs as varying \(a_1\) from 0.5 to 1. It is concluded that optimal outage performance of user \(D_2\) can be achieved at several values of \(a_1\) for FD and HD cases. Fig. 4(b) indicates that outage performance decrease significantly at high requirement of \(R_1\). The reason is that outage behavior is limited by target rates. These curves for outage performance for HD case become saturation as \(R_1\) is greater than 1.15. In contrast, outage performance will worse at higher value of target rate \(R_1\). This situation can be further explained that degraded performance is resulted by interference originated from MCUs in Scheme 2.
Fig. 4: Scheme 2: Outage probability comparison between FD and HD for user $D_1$, $D_2$.

Fig. 5(a) and Fig. 5(b) demonstrate outage performance of two users in Scheme 3 for FD and HD cases. The better outage performance is recognized for user $D_1$ at the point $\lambda_{h1} = \lambda_{h2} = 0.01$. It is also confirmed strong channels exhibit better outage performance, as shown in Fig. 5(b). Similarly, Fig. 5(c) shows how amount of harvested power leads to performance improvement achieved for both users.

Fig. 6(a) depicts that the outage performance of Scheme 1 and Scheme 2 exhibit large gap among two schemes. This situation is related impact of interference from macro-cell network. It is confirmed that challenge happens as important problem for HetNet in term of inter-cell interference. Therefore, limiting the impact of interference in Scheme 2 help to remain outage performance at acceptable level for small-cell network. Fig. 6(b) also reports that the outage performance with $R_1 = R_2 = 0.1$ (bps/Hz) in Scheme 3 worse than that in Scheme 1 significantly. While Fig. 6(b) confirms that outage probability of user $D_1$ in Scheme 1 outperforms than that in Scheme 3. In contrast, user $D_2$ in Scheme 3 is better than that in Scheme 2 in term of outage probability. In addition, small-cell NOMA exhibits its advances compared with the counterpart (OMA scheme). Finally, Fig. 6(c) depicts the most improvement of outage performance as observed for user $D_1$ Scheme 3. It can be explained that EH along higher power coefficient certainly are crucial impacts on performance improvement for cell-edge user.
confirmed that system performance related to three proposed schemes are still retained. In particular, Scheme 1 exhibits its superiority at high SNR compared with remaining schemes. As most important result. The closed-form expressions of outage probability were derived for the two destinations to evaluate the system performance of the proposed scheme, and several comparisons regarding power allocation factor, number of transmit antenna at the BS were provided as well. Simulation results were presented to indicate that the analytical results of outage behavior under impact of interference from MCU’s (Scheme 2 and Scheme 3) will become worse compared with ideal scenario in Scheme 1. More importantly, the proposed HetNet NOMA schemes can significantly improve the outage performance by enabling more antennas at the BS and capable of EH.

APPENDIX A

PROOF OF PROPOSITION 1

From (9), $A_1$ can be computed by

$$A_1 = \Pr \left( \gamma_{1,k}^1 < \epsilon_1^1 \right) \Pr \left( \gamma_{1,-2,k}^1 < \epsilon_1^1 \right) = \Pr \left( |g_{1,k}|^2 < \frac{\epsilon_1^2}{\rho(a_1 - \epsilon_1^2 a_2)} \right) \Pr \left( |g_{2,k}|^2 < \rho \left( a_1 - \epsilon_1^2 a_2 \right) \right)$$

where $\psi_f = \frac{\epsilon_1^2}{\rho(a_1 - \epsilon_1^2 a_2)}$. Based on (7), $A_1$ is given by $A_1 = \left( 1 - \xi_f^1 \right) \left( 1 - \xi_2^1 \right)$, where

$$\xi_2^f = \frac{K}{k \choose k} \left( -1 \right)^{k-1} \exp \left( - \frac{\psi_f}{\lambda_f} \right)$$

From (9) and based on $A_1$, $A_2$ can be expressed as

$$A_2 = \Pr \left( \gamma_1^1 < \epsilon_1^1 \right) \Pr \left( \gamma_1^1 < \epsilon_1^1 \right) \Pr \left( \gamma_{1,-2,k}^1 > \epsilon_1^1 \right) = \left( 1 - \xi_2^1 \right) \Pr \left( \gamma_1^1 < \epsilon_1^1 \right) \xi_2^2$$

(A.2)

Furthermore, $A_{2a}$ can be calculated as

$$A_{2a} = 1 - \Pr \left( |h_1|^2 \geq \frac{\epsilon_1^2 \rho|f_{11}|^2 + \epsilon_1^2}{\rho} \right) = 1 - \int_0^{\infty} \left( 1 - F_{|h_1|^2} \left( \frac{\epsilon_1^2 \rho|f_{11}|^2 + \epsilon_1^2}{\rho} \right) \right) f_{|f_{11}|^2} (x) \, dx.$$  

(A.3)

The CDF and PDF of channel $|g_{1,k}|^2$ are based on (7) and (8), respectively. It is noted that the other channels, i.e., $|h_1|^2$, $|l_2|^2$ and all loop feedback channels follow the Rayleigh distribution with CDF and PDF are $F_{|X|^2} (x) = 1 - \exp \left( - \frac{x}{\lambda_X} \right)$, $f_{|X|^2} (x) = \frac{1}{\lambda_X} \exp \left( - \frac{x}{\lambda_X} \right)$, respectively. It is straightforward to obtain

$$A_{2a} = 1 - \int_0^{\infty} \exp \left( - \frac{\epsilon_1^2 \rho|f_{11}|^2 + \epsilon_1^2}{\rho} \right) \frac{1}{\lambda_{f_{11}}} \exp \left( - \frac{x}{\lambda_{f_{11}}} \right) dx = 1 - \frac{\lambda_{h_1}}{\lambda_{h_1} + \epsilon_1^2 \rho \lambda_{f_{11}}} \exp \left( - \frac{\epsilon_1^2}{\rho \lambda_{h_1}} \right).$$

(A.4)

Substituting (A.4) into (A.2), $A_2$ is written as

$$A_2 = \left( 1 - \xi_1^f \right) \left( 1 - \frac{\lambda_{h_1}}{\lambda_{h_1} + \epsilon_1^2 \rho \lambda_{f_{11}}} \exp \left( - \frac{\epsilon_1^2}{\rho \lambda_{h_1}} \right) \right) \xi_2^f.$$
Combining $A_1$ and $A_2$ into (9), we can obtain (10). It completes the proof.

**APPENDIX B**

**PROOF OF PROPOSITION 2**

From (12), $B_1$ is computed by

$$ B_1 = \left[ 1 - \Pr \left( \gamma_{2,k^*}^s = \varepsilon_2^f, \gamma_{1-2,k^*}^s = \varepsilon_1^f \right) \right] \Pr \left( \gamma_{1,k^*}^s < \varepsilon_2^f \right). $$

\[ \text{(B.1)} \]

By using (B.1), $B_{1a}$ can be evaluated as

$$ B_{1a} = \Pr \left( |g_{2,k^*}|^2 \geq \frac{\varepsilon_2^f}{a_{2p}}, |g_{2,k^*}|^2 \geq \psi_f \right) $$

$$ = \Pr \left( |g_{2,k^*}|^2 \geq \max \left( \frac{\varepsilon_2^f}{a_{2p}}, \psi_f \right) \right) $$

$$ = \Pr \left( |g_{2,k^*}|^2 \geq \theta_f \right) = 1 - F_{|g_{2,k^*}|^2} (\theta_f) $$

\[ \text{(B.2)} \]

$$ = \sum_{k=1}^{K} \binom{K}{k} (-1)^{k-1} \exp \left( -\frac{\theta_f k}{\lambda_2} \right), $$

where $\theta_f = \max \left( \frac{\varepsilon_2^f}{a_{2p}}, \psi_f \right)$ and note that (B.2) is obtained by using the CDF in (7).

Similarly, $B_{1b}$ can be rewritten as

$$ B_{1b} = \Pr \left( |g_{1,k^*}|^2 < \frac{\varepsilon_1^f}{a_{1} - \varepsilon_1^f} \right) = F_{|g_{1,k^*}|^2} (\delta_f) $$

$$ = 1 - \sum_{k=1}^{K} \binom{K}{k} (-1)^{k-1} \exp \left( -\frac{\delta_f k}{\lambda_2} \right), $$

\[ \text{(B.3)} \]

where $\delta_f = \frac{\varepsilon_1^f}{a_{1} - \varepsilon_1^f} a_{2\lambda_2}.$

Substituting (B.2) and (B.3) into (B.1), $B_1$ is written as

$$ B_1 = \left( 1 - \sum_{k=1}^{K} \binom{K}{k} (-1)^{k-1} \exp \left( -\frac{\theta_f k}{\lambda_2} \right) \right) \times \left( 1 - \sum_{k=1}^{K} \binom{K}{k} (-1)^{k-1} \exp \left( -\frac{\delta_f k}{\lambda_2} \right) \right). $$

\[ \text{(B.4)} \]

Based on (12) and $A_1$, we can rewrite $B_2$ as

$$ B_2 = \left[ \Pr \left( \gamma_{2,k^*}^s < \varepsilon_2^f \right) + \Pr \left( \max \left\{ \gamma_{1-2,k^*}^s, \gamma_{2,k^*}^s \right\} < \varepsilon_1^f \right) \right] \Pr \left( \gamma_{1,k^*}^s < \varepsilon_2^f \right). $$

\[ \text{(B.5)} \]

\[ B_{21} \]

From (B.5), $B_{21}$ is given as

$$ B_{21} = \Pr \left( \gamma_{2,k^*}^s < \varepsilon_2^f \right) = 1 - \Pr \left( |g_{2,k^*}|^2 \geq \frac{\varepsilon_2^f}{a_{2p}} \right) $$

$$ = 1 - \sum_{k=1}^{K} \binom{K}{k} (-1)^{k-1} \exp \left( -\frac{\varepsilon_2^f k}{a_{2p} \lambda_2} \right) = 1 - \mu_1^f, $$

where $\mu_1^f = \sum_{k=1}^{K} \binom{K}{k} (-1)^{k-1} \exp \left( -\frac{\varepsilon_2^f k}{a_{2p} \lambda_2} \right).$

From (B.5) and based on (A.1), we can achieve $B_{22}$ as

$$ B_{22} = \Pr \left( \gamma_{1-2,k^*}^s < \varepsilon_1^f, \gamma_{1,k^*}^s < \varepsilon_1^f \right) $$

$$ = \Pr \left( \gamma_{1-2,k^*}^s < \varepsilon_1^f \right) \Pr \left( \gamma_{1,k^*}^s < \varepsilon_1^f \right) $$

$$ = \left( 1 - \varepsilon_2^f \right) \Pr \left( \gamma_{1,k^*}^s < \varepsilon_1^f \right). $$

\[ \text{(B.7)} \]

Then, $B_{22a}$ can be simplified as

$$ B_{22a} = 1 - \Pr \left( \gamma_{1,k^*}^s \geq \varepsilon_1^f \right) $$

$$ = 1 - \Pr \left( |h_{2}|^2 \geq \varepsilon_1^f \right) \exp \left( -\frac{\psi_2}{\rho \lambda_2} \right) $$

$$ = 1 - \int_{0}^{\infty} \left( 1 - F_{|h_{2}|^2} \left( \frac{\varepsilon_1^f}{\rho \lambda_2} \right) \right) f_{|h_{2}|^2} (y) dy $$

$$ = 1 - \int_{0}^{\infty} \exp \left( -\frac{\psi_2}{\rho \lambda_2} \right) \frac{1}{\lambda_{2}} \exp \left( -\frac{y}{\lambda_{2}} \right) dy = 1 - \eta_1^f, $$

\[ \text{where} \quad \eta_1^f = \frac{\lambda_{2}}{\lambda_{2} + \varepsilon_1^f}, \quad \frac{\psi_2}{\rho \lambda_2}. \]

Substituting (B.8) into (B.7), $B_{22}$ is written as $B_{22} = \left( 1 - \xi_2^f \right) \left( 1 - \eta_1^f \right).$

Based on $B_{21}$ and $B_{22}, B_{23}$ can be expressed as

$$ B_{23} = \Pr \left( \gamma_{1-2,k^*}^s < \varepsilon_2^f \right) \Pr \left( \gamma_{1-2,k^*}^s < \varepsilon_1^f \right) \Pr \left( \gamma_{2,k^*}^s < \varepsilon_1^f \right) $$

$$ = \left( 1 - \mu_1^f \right) \left( 1 - \xi_2^f \right) \left( 1 - \eta_1^f \right). $$

\[ \text{(B.9)} \]

By replacing $B_{21}, B_{22}$ and $B_{23}$ into (B.5). It can be further obtained $B_2$ as

$$ B_2 = \left[ \left( 1 - \mu_1^f \right) + \left( 1 - \xi_2^f \right) \left( 1 - \eta_1^f \right) \right] \xi_1^f. $$

\[ \text{(B.10)} \]

Combining (B.4), (B.10) into (12), we can obtain (13). It completes the proof.

**APPENDIX C**

**PROOF OF PROPOSITION 3**

From (20), $C_1$ is further computed as

$$ C_1 = \Pr \left( \gamma_{1,k^*}^s < \varepsilon_1^f \right) \Pr \left( \gamma_{1-2,k^*}^s < \varepsilon_1^f \right) \Pr \left( \gamma_{2,k^*}^s < \varepsilon_1^f \right). $$

\[ \text{(C.1)} \]

Then, $C_{1a}$ can be obtained as

$$ C_{1a} = 1 - \Pr \left( \gamma_{1,k^*}^s \geq \varepsilon_1^f \right) $$

$$ = 1 - \Pr \left( |g_{1,k^*}|^2 \geq \frac{\varepsilon_1^f}{a_{1} - \varepsilon_1^f} \right) \exp \left( -\frac{\psi_1}{a_{1} - \varepsilon_1^f a_{2\lambda_2}} \right) $$

$$ = 1 - \int_{0}^{\infty} \left( 1 - F_{|g_{1,k^*}|^2} \left( \frac{\varepsilon_1^f}{a_{1} - \varepsilon_1^f a_{2\lambda_2}} \right) \right) f_{|h_{1}|^2} (x) dx $$

$$ = 1 - \sum_{k=1}^{K} \binom{K}{k} (-1)^{k-1} \exp \left( -\frac{\varepsilon_1^f k}{a_{1} - \varepsilon_1^f a_{2\lambda_2}} \right) \frac{1}{\lambda_{1}} \exp \left( -\frac{x}{\lambda_{1}} \right) dx = 1 - \theta_1^f, $$

\[ \text{(C.1)} \]
Similarly, $C_{1b}$ is given by

\[
C_{1b} = 1 - \Pr \left( \gamma_{1+2,k^*}^2 \geq \varepsilon_1 \right)
\]

\[
= 1 - \Pr \left( |g_{2,k^*}|^2 \geq \frac{\varepsilon_1 \rho|g_1|^2 + \varepsilon_1}{(a_1 - \varepsilon_1 a_2) \rho} \right)
\]

\[
= 1 - \int_0^\infty \left( 1 - F_{|g_{2,k^*}|^2} \left( \frac{\varepsilon_1 \rho + \varepsilon_1}{(a_1 - \varepsilon_1 a_2) \rho} \right) \right) f_{|f_2|^2}(y) dy
\]

\[
= 1 - \sum_{k=1}^K (k)(-1)^{k-1} \int_0^\infty \exp \left( - \frac{(\varepsilon_1 \rho + \varepsilon_1) k}{(a_1 - \varepsilon_1 a_2) \rho \lambda_2} \right) \times \frac{1}{\lambda_2} \exp \left( - \frac{y}{\lambda_2} \right) dy = 1 - \theta_{12}^f.
\]  

(C.2)

Base on (C.1) and (C.2), $C_1$ is written as

\[
C_1 = \left( 1 - \theta_1^f \right) \left( 1 - \theta_2^f \right).
\]

From (20), $C_2$ is further expressed as

\[
C_2 = \Pr \left( \frac{\gamma_{1,k^*}^2 - \varepsilon_1^2}{\chi_1^2} \right) \Pr \left( \frac{\chi_2^2 - \varepsilon_1^2}{\chi_2^2} \right) \Pr \left( \gamma_{1+2,k^*}^2 > \varepsilon_1^2 \right).
\]

(C.3)

Furthermore, $C_{2a}$ and $C_{2c}$ in (C.3) can be expressed as (C.1) and (C.2), respectively.

According to (C.3), $C_{2b}$ can be calculated as follows

\[
C_{2b} = 1 - \Pr \left( \chi_1^2 \geq \varepsilon_1^2 \right)
\]

\[
= 1 - \Pr \left( \left| |h_1| \right|^2 \geq \frac{\varepsilon_1^2 (|\rho f_1|^2 + |\rho f_2|^2 + 1)}{\rho} \right)
\]

\[
= 1 - \int_0^\infty \int_0^\infty \left( 1 - F_{|h_1|^2} \left( \frac{\varepsilon_1^2 (|\rho f_1|^2 + |\rho f_2|^2 + 1)}{\rho} \right) \right) f_{|f_1|^2}(x) f_{|f_2|^2}(y) dxdy
\]

\[
= 1 - \frac{1}{\lambda_1} \exp \left( - \frac{\varepsilon_1^2}{\rho \lambda_1} \right) \int_0^\infty \exp \left( - \frac{\varepsilon_1^2}{\lambda_1} + \frac{1}{\lambda_1} x \right) dx
\]

\[
\times \int_0^\infty \exp \left( - \frac{\varepsilon_1^2}{\lambda_1} + \frac{1}{\lambda_1} y \right) dy
\]

\[
= 1 - \frac{\lambda_1}{\varepsilon_1^2 \lambda_1 + \lambda_1} \exp \left( - \frac{\varepsilon_1^2}{\rho \lambda_1} \right).
\]  

(C.4)

By replacing (C.1), (C.2), (C.4) into (C.3) it can be obtained $C_2$ as

\[
C_2 = \left( 1 - \theta_1^f \right) \frac{\lambda_1}{\varepsilon_1^2 \lambda_1 + \lambda_1} \exp \left( - \frac{\varepsilon_1^2}{\rho \lambda_1} \right).
\]

(C.5)

Combining $C_1$, (C.5) into (20), we can obtain (21). It completes the proof.

APPENDIX D

PROOF OF PROPOSITION 4

From (23), \( OP_{D_{22}} \) can be given as

\[
OP_{D_{22}}^{f-s_2} = \left[ 1 - \Pr \left( \frac{\gamma_{2,k^*}^2 \geq \varepsilon_1^2, \gamma_{1+2,k^*}^2 \geq \varepsilon_1^2}{Q_{12}} \right) \right]
\]

\[
\times \Pr \left( \frac{\gamma_{1,k^*}^2 < \varepsilon_1^2}{Q_{21}} \right) + \Pr \left( \frac{\gamma_{2,k^*}^2 < \varepsilon_1^2}{Q_{22}} \right)
\]

\[
+ \Pr \left( \max \{ \frac{\gamma_{1+2,k^*}^2, \gamma_{2,k^*}^2}{} \} < \varepsilon_1^2 \right) \quad \left( D.1 \right)
\]

\[
\times \Pr \left( \frac{\gamma_{1,k^*}^2 > \varepsilon_1^2}{Q_{32}} \right).
\]

It is noted that $Q_1$ is further computed as

\[
Q_1 = \Pr \left( \frac{\gamma_{1+2,k^*}^2 \geq \varepsilon_1^2, \gamma_{1+2,k^*}^2 \geq \varepsilon_1^2}{Q_1} \right)
\]

\[
= \Pr \left( |g_{2,k^*}|^2 \geq \frac{\varepsilon_1^2 (|\rho| f_1|^2 + |\rho| f_2|^2 + 1)}{\rho} \right)
\]

\[
= \Pr \left( |g_{2,k^*}|^2 \geq \left( \frac{|\rho| f_1|^2 + |\rho| f_2|^2 + 1}{\rho} \right) \theta^f \right)
\]

\[
= \int_0^\infty \left( 1 - F_{|g_{2,k^*}|^2} \left( \left( |\rho| f_1|^2 + |\rho| f_2|^2 + 1 \right) \theta^f \right) \right) f_{|f_2|^2}(y) dy
\]

\[
= \sum_{k=1}^K (k)(-1)^{k-1} \int_0^\infty \exp \left( - \left( \frac{|\rho| f_1|^2 + |\rho| f_2|^2 + 1}{\rho} \right) \theta^f \right) \frac{1}{\lambda_2} \exp \left( - \frac{y}{\lambda_2} \right) dy
\]

\[
= \Omega_1^f.
\]  

(D.2)

where $\Omega_1^f = \sum_{k=1}^K (k)(-1)^{k-1} \frac{\lambda_2}{\rho \lambda_1} \exp \left( - \frac{\theta^f k}{\lambda_1} \right)$. Similarly as $C_{1a}$, $Q_2$ can be formulated as $Q_2 = 1 - \Omega_1^f$, where

\[
\Omega_2^f = \sum_{k=1}^K (k)(-1)^{k-1} \frac{\lambda_2}{\rho \lambda_1} \exp \left( - \frac{\theta^f k}{\lambda_1} \right)
\]

where $\Omega_2^f = \sum_{k=1}^K (k)(-1)^{k-1} \frac{\lambda_2}{\rho \lambda_1} \exp \left( - \frac{\theta^f k}{\lambda_1} \right)$. Similarly as $C_{1b}$ and $C_{2b}$, it can be achieved $Q_4$ as

\[
Q_4 = \left[ 1 - \Pr \left( \frac{\gamma_{2,k^*}^2 \geq \varepsilon_1^2}{Q_{12}} \right) \right] \left[ 1 - \Pr \left( \frac{\gamma_{1+2,k^*}^2 \geq \varepsilon_1^2}{Q_{11}} \right) \right]
\]

\[
= \left( 1 - \theta_1^f \right) \left( 1 - \theta_2^f \right)
\]

(D.4)

where $\theta_2^f = \frac{\lambda_2}{\varepsilon_1^2 \lambda_2 + \lambda_2} \exp \left( - \frac{\varepsilon_1^2}{\rho \lambda_2} \right)$. 

Similarly as (23), The outage probability user $D_2$ in scheme 3 at FD mode can be expressed as

$$OP_{D2}^{f-s3} = \left[ 1 - \Pr \left( \gamma_{1, k^*}^{s3} < \varepsilon_2, \gamma_{1, k^*}^{s3} \geq \varepsilon_1' \right) \right]$$

$$\times \Pr \left( \gamma_{1, k^*}^{s3} < \varepsilon_2' \right) + \left[ \Pr \left( \gamma_{1, k^*}^{s3} < \varepsilon_2' \right) \right]$$

$$\times \Pr \left( \max \left\{ \gamma_{1, k^*}^{s3}, \chi_{23}^{s3} \right\} < \varepsilon_1' \right)$$

$$\times \Pr \left( \gamma_{1, k^*}^{s3} > \varepsilon_1' \right).$$

(F.1)

By exploiting $Q_1$, $F_1$ can be written as

$$F_1 = \Pr \left( \left| g_{2, k} \right|^2 \geq \frac{\varepsilon_1^3 (1-\beta) |l_2|^2 + 1}{\rho \lambda_1^2} \right)$$

$$= \Pr \left( \left| g_{2, k} \right|^2 \geq \left( (1-\beta) |l_2|^2 + 1 \right) \theta_f \right)$$

$$= \int_0^\infty \left( 1 - \Pr \left( \left| g_{2, k} \right|^2 \geq \left( (1-\beta) |l_2|^2 + 1 \right) \theta_f \right) \right) f_{|l_2|^2} (y) dy$$

$$= \sum_{k=1}^K \left( k \right) \left( 1 - \int_0^\infty \exp \left( - \left( (1-\beta) |l_2|^2 + 1 \right) \frac{\theta_f}{\lambda_2} \right) \right)$$

where $\Theta_f = \sum_{k=1}^K \left( k \right) \left( 1 - \frac{1}{\lambda_2} \right) \exp \left( \frac{\theta_f}{\lambda_2} \right)$.

Similarly as in $C_{1a}$ and $Q_2$, $F_2$ can be written as $F_2 = 1 - \Theta_2$, where $\Theta_2 = \sum_{k=1}^K \left( k \right) \left( 1 - \frac{1}{\lambda_2} \right) \exp \left( \frac{\theta_f}{\lambda_2} \right)$.

Furthermore, by using $Q_3$, $F_3$ can be expressed by $F_3 = 1 - \Xi_f$, where $\Xi_f = \sum_{k=1}^K \left( k \right) \left( 1 - \frac{1}{\lambda_2} \right) \exp \left( \frac{\theta_f}{\lambda_2} \right)$.

Similarly, as in $E_{2b}$ and $E_1$, $F_4$ can be written by

$$F_4 = \left[ 1 - \Pr \left( \chi_{23}^{s3} \geq \varepsilon_1' \right) \right] \left[ 1 - \Pr \left( \gamma_{1, k^*}^{s3} \geq \varepsilon_1' \right) \right]$$

$$= \left[ 1 - \Xi_f \right] \left[ 1 - \Phi_f^1 \right].$$

(F.3)

where $\Xi_f = \sum_{k=1}^K \left( k \right) \left( 1 - \frac{1}{\lambda_2} \right) \exp \left( \frac{\theta_f}{\lambda_2} \right)$.

Using $F_3$ and $F_4$, we obtain $F_5$ as

$$F_5 = \Pr \left( \gamma_{1, k^*}^{s3} < \varepsilon_2' \right) \left[ 1 - \max \left\{ \gamma_{1, k^*}^{s3}, \chi_{23}^{s3} \right\} \leq \varepsilon_1' \right]$$

$$= \left[ 1 - \Pr \left( \gamma_{1, k^*}^{s3} \geq \varepsilon_2' \right) \right] \left[ 1 - \Pr \left( \gamma_{1, k^*}^{s3} \geq \varepsilon_1' \right) \right]$$

$$= \left[ 1 - \Xi_f \right] \left[ 1 - \Phi_f^2 \right] \left( 1 - \Phi_f^1 \right).$$

(F.4)
Based on $E_1$, $F_0$ can be formulated as $F_0 = \Phi^f_1$. From (F.2)-(F.4), $F_2$, $F_3$ and $F_0$ into (F.1), we can obtain (37), the proof is completed.

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