The Spatial Resolution Enhancement for a Thermogram Enabled by Controlled Sub-pixel Movements

Weixiang Du, Sri Addepalli, and Yifan Zhao

Abstract—The measurement accuracy and reliability of thermography is largely limited by a relatively low spatial resolution of the thermal imager. Using a high-end camera to achieve high spatial resolution can be costly or infeasible due to a high sample rate required. Furthermore, the system miniaturisation becomes an inevitable trend with the continuous development of Internet of Things and their suitability to in-situ inspection scenarios. However, a miniaturised sensor usually suffers a low spatial resolution. Addressing this challenge, the paper reports a novel Spatial Resolution Enhancement for a Thermogram (SRE4T) system to significantly improve the spatial resolution without upgrading the sensor. A high-resolution thermal image is reconstructed by fusing a sequence of low-resolution images with sub-pixel movements. To achieve the best image quality, instead of benefitting from natural movements of existing studies, this paper proposes to use a high-resolution xy translation stage to produce a sequence of controlled sub-pixel movements. The performance of the proposed system was tested on both high-end and low-end thermal imagers. Both visual and quantitative results successfully demonstrated the considerable improvement of the quality of thermal images (up to 30.5% improvement of peak signal to noise ratio). This technique allows improving the measurement accuracy of thermography inspection without upgrading sensors. It also has the potential to be applied on other imaging systems.

Index Terms—Resolution Enhancement, NDT, Motion Estimation, Image Reconstruction

I. INTRODUCTION

Infrared (IR) thermography is a non-contact Non-Destructive Testing (NDT) method and offers a robust and a rapid platform for inspection while covering a large area within a short time frame and thus potentially adaptable to in-service monitoring applications [1], [2] for electrical equipment [3], [4], mechanical equipment [5], welding [6], structural [7], [8] and aerospace composite materials [9]. However, in comparison with other NDT methods such as x-ray and ultrasound, thermography has a relatively low spatial resolution (typically 640 × 480 pixels). Although some latest thermal imaging technologies have been achieved [10], the spatial resolution is still the major limiting factor and bottleneck for industrial applications of thermography [11] mainly due to the refinement needed for the improved anomaly feature extraction. A high-end IR camera with a high spatial resolution is usually costly which is driven by the use of quantum detectors, e.g. mercury cadmium telluride, indium antimonide. Additionally, the maximum spatial resolution may be unachievable when a high sample rate has to be used for materials such as metals and alloys as they have a high thermal-conductivity. Furthermore, even with the same spatial resolution, the boundary of objects or discontinuity in thermal images is not as sharp as that of digital images. This is related to their imaging principles[12]–[14]: the digital imaging system normally acquire images using CCD/CMOS sensors, which is based on the difference in the intensity of light in the range of 0.4-0.7µm reflected by the surface of the observed target, with a high contrast and improved resolution. Infrared thermal imaging technology is based on receiving radiant energy with longer wavelengths in the range of 3-12µm. Due to the influence of atmospheric condition, the difference in minimum resolvable temperature difference between the object and the background together with the distance it is measured from, the target is easily submerged in the dark background, which leads to the blurring effect of the acquired thermal image. The existing low-cost IR cameras usually have disadvantages such as low contrast, edge blurring, large noise, low clarity, and poor ability, which make it difficult to define the boundary and accurately measure the shape of targets. There is a strong demand to improve the quality of thermal images without upgrading the hardware in the context of NDT and surveillance systems.

With the increase of the functionality integration, complexity of industrial products and increasing use of advanced materials into complex systems, the heavy weight and large size of equipment has become the bottleneck to deploy NDT devices in in-situ inspection. Developing lightweight and miniaturised NDT equipment to inspect various materials for degradation assessment of inaccessible area becomes more and more important [15]. Furthermore, the serviceability of the components or systems to be inspected has now become challenging, particularly in determining their maintenance requirements as disassembly and inspection is very expensive. The trend is now in the development of portable equipment that will improve the maintenance and performance of the system that is being monitored. The rapid development of the Internet of Things (IoT) technology has promoted the development of small sensors which contained the feature of small size and low power consumption [16]. However, it brings some problems

W. Du, S. N. P. Addepalli is with the Through-life Engineering Service Centre, SATM, Cranfield University, Y. Zhao (corresponding author) is with the Through-life Engineering Service Centre, SATM, Cranfield University, UK (e-mail: yifan.zhao@cranfield.ac.uk)
such as poor image quality, low resolution and sensitivity in addition to the ability to transfer large datasets wirelessly.

There are a few studies reported to improve the quality of thermal images, and are largely based on single image enhancement or super-resolution (SR). The key of SR is to capture multiple sub-pixel low-resolution (LR) images at pre-defined locations for the same scene, and rebuild the high-resolution (HR) images by integrating these images and restoring the missing signals in one pixel, which greatly improves the image quality. In the category of single image enhancement, Holland and Renshaw [17] proposed a physics-based method that used the basic principles of the physics of thermal diffusion to improve the spatial resolution of the thermogram. Another attempt was done by Ashiba et al. [18] who presented a new approach based on contrast limited adaptive histogram equalisation to improve the infrared images. In the category of SR, Alam et al. [19] proposed a gradient-based registration algorithm to estimate the shifts between the acquired thermal images and then used a weighted nearest-neighbour approach for placing the frames onto a uniform grid to form a final HR image. The quality of the produced HR image relies on how well the sub-pixel motions are uniformly distributed. However, the shifts were caused by the vibrations from the platform on which the camera was mounted, which is uncontrollable and random, such as commercial tool FLIR UltraMax™ [20] Sadi and Crastes [21] used an uncooled microbolometer array to produce a HR thermal imaging by taking advantages of the relative motion between the camera and the object to produce information redundancy. Kaczmarek and Borwanski [22] used recording time series of thermograms to reconstruct a thermal image with improved spatial resolution. Mwangi et al. [23] proposed a fusion of active thermography and visible imagery data, capable of producing higher-resolution thermograms based on the physical boundaries in the visible domain. The sharpness of the thermogram was improved based on the additional information obtained from the digital image. Collectively, SR-based approaches usually produce better results than the single image enhancement methods because they increase the entropy of the images through benefiting from the true measurements of multiple images. Single image enhancement methods either improve the

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**TABLE I**

<table>
<thead>
<tr>
<th>Specification</th>
<th>FLIR A655sc</th>
<th>FLIR one</th>
</tr>
</thead>
<tbody>
<tr>
<td>Spectral range</td>
<td>7.5 – 14.0 μm</td>
<td>8 – 14 μm</td>
</tr>
<tr>
<td>Resolution</td>
<td>640 x 480</td>
<td>160 x 120</td>
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<tr>
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<td>24.6 mm - Infinity</td>
<td>150 mm - Infinity</td>
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<tr>
<td>Pixel size</td>
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<td>12 μm</td>
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<tr>
<td>Frame rate</td>
<td>50 Hz</td>
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<tr>
<td>Accuracy</td>
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</tr>
<tr>
<td>Measurement temperature</td>
<td>-40°C to 150°C</td>
<td>-20°C - 120°C</td>
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<tr>
<td>Operating temperature</td>
<td>-15°C to 50°C</td>
<td>0°C – 35°C</td>
</tr>
<tr>
<td>Size</td>
<td>216 x 73 x 75 mm</td>
<td>65x29x18mm</td>
</tr>
<tr>
<td>Weight</td>
<td>900g</td>
<td>32g</td>
</tr>
</tbody>
</table>

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![Fig. 1. Experiment setup. (a) The experiment setup for FLIR A655sc; (b) the experiment set up for FLIR ONE; (c) the infrared blackbody calibrator (OMEGA BB702); (d) the FLIR A655sc and FLIR One cameras.](image)

**II. METHODS**

A. Experimental setup

To capture a sequence of raw thermal images with subpixel shifts in both x and y directions, an experiment setup is introduced and illustrated by Figs. 1(a) and (b). A thermal camera is mounted on a high accuracy x-y translation stage with a resolution of ±1 μm. An infrared blackbody calibrator (OMEGA BB702), as illustrated in Fig. 1(c), is used as the observed object. The 2.5-inch (63.5 mm) diameter target plate has an emissivity of 0.95 and can be set to a range of temperatures between ambient +32°C to 215°C. To ensure the observed object has the exact same temperature distribution during the data acquisition of multiple images, the temperature of the calibrator was fixed at 38°C with the room reflected temperature recorded at 22°C and a relative humidity value of 55%.
There are two potential motion modes: one is the object moves and the camera is fixed, and the other is the object is fixed while the camera moves. Both modes can introduce a global sub-pixel motion, which is key to increase the resolution of static objects. In this paper, the later mode is employed. The main reason for this setup was due to the heavy weight of the blackbody calibrator and the relatively low weight of the cameras (as seen in Fig. 1).

To create the sub-pixel movements required for the super-resolution technique, for each data capture, the translation stage moves a step of $1/a$ pixel either on $x$ or $y$ direction, where $a$ ($a > 1$) is the scale factor to achieve. Assuming the object position in the thermal image on the first data capture as the reference, denoted as $(x_0, y_0)$, the camera is moved to ensure that the following positions of the object on the thermal image are achieved:

$$
\begin{align*}
(x_0, y_0, \ldots, \left(x_0 + \frac{1}{a}y_0\right), \ldots, \left(x_0 + \frac{a-1}{a}y_0\right), & \\
\left(x_0, y_0 + \frac{1}{a}x_0, \ldots, \left(x_0 + \frac{a-1}{a}x_0\right), & \\
\ldots, \ldots, \ldots, & \\
\left(x_0, y_0 + \frac{a-1}{a}\right), & \\
\end{align*}
\tag{1}
$$

It can be inferred from Eq. (1) that the total number of images to be captured is $a^2$.

The movement step of the translation stage depends on the intrinsic parameters of the camera and the distance from the camera to the object surface. This paper uses a simple calibration process to achieve a parameter $\alpha$, which indicates the required millimetre movement of the stage in the $x$ or $y$ direction to achieve a representative shift of one-pixel in thermal image. In this study, one thermal image was captured along the $x$ direction of the stage which represents a shift of 1 mm. The shift of the calibrator on the thermal images is now measured and denoted as $m$ pixels. Then $\alpha$ is written as

$$
\alpha = 1/m.
\tag{2}
$$

This step can then be repeated for the $y$ direction. To simplify the process, this paper uses the same value of $\alpha$ for both the $x$ and $y$ directions.

In this study, two thermal cameras have been tested, as shown in Fig. 1(d). The FLIR A655sc, a high-end IR camera with a resolution of 640 $\times$ 480 pixels, was used to demonstrate the proof of concept. Quantitative evaluation of the performance is conducted by this camera as it can offer a high-resolution reference image. Resolution enhancement of this camera could lead to the improvement of detection accuracy and reliability. A low-end miniature IR camera, the FLIR ONE with a resolution of 160 $\times$ 120 pixels, was then used to validate the proposed technique for a miniaturised sensor where the imaging quality is compromised for portability. This case study aims to explore the potential of SRE4T in situ inspection scenarios. The key parameters of two cameras are shown in Table 1. Both cameras have similar spectral range, but have a huge difference on spatial resolution, size and weight.

The distance between the camera and the calibrator surface was adjusted to ensure a good field of view of the calibrator. For the FLIR A655sc, the distance was set as 300 mm and the estimated $\alpha$ is 20 $\mu$m. Considering the minimal step of the stage (1 $\mu$m), 20 movements should be conducted on each direction to achieve one-pixel movement in images. Therefore, theoretically, the maximal achievable scale factor of resolution for this setting is 20. For the FLIR ONE, the distance was set as 140 mm to ensure a similar field of view (the FLIR ONE has a wider angle of the lens) as the FLIR A655sc and the estimated $\alpha$ is 40 $\mu$m. The maximal achievable scale factor of resolution in the latter case is 40. It should be noted that the achievable maximal scale factor depends on the working distance, focus, stage step and camera specifications.

### B. Super-resolution algorithm

There are two main stages to fuse the captured low resolution raw images (LR) into a high resolution (HR) image: the image registration and the image construction. Image registration aims at the estimation of motion parameters between the LR images, while image reconstruction aims at combining the registered LR image to reconstruct a HR image by using the estimated motion parameters. It should be noted that the image registration step can be skipped if the motions are perfectly controlled. For this study, this step was still implemented since the motion was controlled manually and has limited accuracy.

#### 1) Image registration

Image registration methods can be operated either in the spatial-domain or the frequency-domain. Frequency-domain methods are usually limited to global motion models, whereas spatial-domain methods usually allow more general motion models. In this paper, the method developed by Keren et al. [24] was employed to estimate the shifts (both horizontal and vertical shifts) and rotations among the LR images due to its fine performance to tackle the global motion.

The relation between the horizontal shift $\alpha$, the vertical shift $b$, and the rotation angle $\theta$ between the LR images $f$ and $g$ can be written as

$$
g(x, y) = f(x \cos(\theta) - y \sin(\theta) + a, y \cos(\theta) + x \sin(\theta) + b). \tag{3}
$$

Expanding $\sin(\theta)$ and $\cos(\theta)$ to the first two terms in their Taylor series expansion gives the following equation

$$
g(x, y) \approx f(x + a - y\theta - x\theta^2/2, y + b + x\theta - y\theta^2/2). \tag{4}
$$

Expanding $f$ to the first term in its Taylor series gives the first-order equation

$$
g(x, y) = f(x, y) + (a - y\theta - x\theta^2/2) \frac{\partial f}{\partial x} + (b + x\theta - y\theta^2/2) \frac{\partial f}{\partial y}. \tag{5}
$$

The error between $g$ and $f$ after translation by $a$ and $b$ and rotation by $\theta$, expressed as $E$, can thus be approximated by

$$
E(a, b, \theta) = \sum \left[f(x, y) + (a - y\theta - x\theta^2/2) \frac{\partial f}{\partial x} + (b + x\theta - y\theta^2/2) \frac{\partial f}{\partial y} - g(x, y)\right]^2,
$$

where the summation is over the overlapping area of $f$ and $g$.

The minimum of $E(a, b, \theta)$ can be obtained by computing its derivatives with respect to $a$, $b$ and $\theta$ and setting them to zero.
The difference between $g$ and $f$ warped by $(a, b, \theta)$ will be minimised by solving the following equation for $a$, $b$, and $\theta$:

\[
\begin{align*}
\sum \left( \frac{\partial f}{\partial x} \right)^2 a + \sum \frac{\partial f}{\partial x} b + \sum R \frac{\partial f}{\partial x} \theta &= \sum \frac{\partial f}{\partial x} (f - g) \\
\sum \frac{\partial f}{\partial y} a + \sum \frac{\partial f}{\partial y} b + \sum R \frac{\partial f}{\partial y} \theta &= \sum \frac{\partial f}{\partial y} (f - g) \\
\sum R \frac{\partial f}{\partial x} a + \sum R \frac{\partial f}{\partial y} b + \sum R^2 \theta &= \sum R (f - g)
\end{align*}
\]

(7)

where

\[
R = x \frac{\partial y}{\partial y} - y \frac{\partial x}{\partial x}.
\]

By solving this set of linear equations, the motion parameters $a$, $b$, and $\theta$ can then be computed.

2) Image Reconstruction

Pham et al. [25] proposed the so-called structure-adaptive normalised convolution (SANC) reconstruction method for the fusion of irregularly sampled data obtained from the different LR images. The method is based on the normalised convolution (NC) method [26], which approximates the local signal from projections onto a set of polynomials basis functions. Employing the polynomials basis functions in the NC makes it equal to a local Taylor series expansion. Considering a local neighbourhood centred at $s_0 = \{x_0, y_0\}$, the intensity value at position $s = \{x, y\}$ in the HR image is estimated using a polynomial expansion written as

\[
\hat{f}(s, s_0) = P_0(s_0) + P_1(s_0)x + P_2(s_0)y + P_3(s_0)x^2 + P_4(s_0)xy + P_5(s_0)y^2 + \ldots
\]

(8)

where

\[
\begin{align*}
x &= \cos(\theta)(a + x_0) - \alpha \sin(\theta)(b + y_0) \\
y &= \sin(\theta)(a + x_0) + \alpha \cos(\theta)(b + y_0).
\end{align*}
\]

(9)\(P(s_0) = [P_0 P_1 \ldots P_m][s_0]\) are the projection coefficients onto their entire polynomial basis functions at $s_0$.

A structure-adaptive applicability function is used in NC to localise a polynomial approximation, which gives different weights to all data points in a neighbourhood in the image. In addition, the signal certainty is introduced in NC to ensure each input signal owing its certainty value and reduce the impact of outliers caused by missing samples or erroneous registration.

C. Performance Evaluation

This section presents the approach to quantify the resolution improvement of the proposed system. The peak signal to noise ratio (PSNR) between the super-resolved image and the original HR image is one of the most commonly used objective fidelity criteria for evaluating image quality. It can be calculated as

\[
PSNR = 10 \log_{10} \left( \frac{L^2}{MSE} \right),
\]

(11)

where $L$ is the maximum fluctuation in the image. The higher the PSNR, the better the improvement is. If the image is represented by 8-bit grayscale, the value of $L$ will be 255. $MSE$ represents the mean-square-error between the super-resolved image $\hat{X}(i,j)$ and the original HR image $X(i,j)$. It can be calculated as

\[
MSE = \frac{1}{WH} \sum_{i=1}^{W} \sum_{j=1}^{H} (\hat{X}(i,j) - X(i,j))^2,
\]

(12)

where $W$ and $H$ denote the width and height of the image.

Entropy is another quantitative measure used to assess image quality when the error images for different image resolution enhancement techniques are very close to each other and it is very difficult to make a firm assessment. The entropy of a negative error image, denoted by $ET$, can be calculated as

\[
ET = - \sum_{k=1}^{l} P(r_k) \log_{2} P(r_k),
\]

(13)

where $P(r_k)$ is the probability of an intensity value $r_k$. The lower the $ET$, the better the improvement is [27].

To complement the quantitative analysis, the structural similarity (SSIM) [28] image quality measure has also been applied. The SSIM index evaluates the visual effect of three characteristics of an image: luminance, contrast, and structure. It is based on the computation of these three components and is an inner product of them. It is defined as

\[
SSIM = \frac{2\mu_x \mu_y + C_1}{\mu_x^2 + \mu_y^2 + C_1} \frac{2\sigma_{xy} + C_2}{\sigma_x^2 + \sigma_y^2 + C_2}
\]

(14)

where $\mu_x, \mu_y$ are the local means for the images $\hat{X}$ and $X$, respectively; $\sigma_x, \sigma_y$ are corresponding standard deviations; and $C_1, C_2$ are two constants used to avoid the instability. The higher the SSIM, the better the improvement is.

D. Experiment Plan

To evaluate the performance of resolution improvement qualitatively and quantitatively, three experiments were conducted.

Experiment 1: The FLIR A655sc was used and $\alpha$ was chosen as 20 $\mu$m. Three groups of data were collected aiming to achieve the scale factor of 2, 3, and 4 respectively. The resolution of the produced HR images is now at 1280 $\times$ 960, 1920 $\times$ 1440, and 2560 $\times$ 1920 respectively. Visual comparison (qualitative evaluation) was conducted between the produced HR images and the raw images with a resolution of 640 $\times$ 480. No quantitative evaluation was conducted for this experiment due to the lack of the reference image.

Experiment 2: The FLIR ONE was used and $\alpha$ was chosen as 40 $\mu$m. Three groups of data were collected to achieve the scale factor of 2, 3, and 4 respectively. The resolution of the produced HR images is 320 $\times$ 240, 480 $\times$ 360, and 640 $\times$ 480 respectively. Visual comparison was conducted between the produced HR images and the raw images with a resolution of 160 $\times$ 120. No quantitative evaluation was conducted for this experiment due to the lack of the reference image.

Experiment 3: The FLIR A655sc was used and $\alpha$ was chosen as 20 $\mu$m, where $\alpha$ is the scale factor. The captured raw images $IMR_i (i = 1, 2, \ldots, a^2)$ with a resolution of 640 $\times$ 480 were downsized to 640/$\alpha$ by 480/$\alpha$, denoted by $IMR_i (i = 1, 2, \ldots, a^2)$. The SR technique was then applied on these LR images to reconstruct a HR image with a resolution of 640 $\times$ 480, denoted by $IMH$. $IMR_i$ now becomes the reference HR image, which allows a quantitative evaluation on the similarity between $IMH$ and $IMR_i$. Three criteria were calculated to represent the quality improvement and can be written as
m_{PSNR} = \max_i PSNR(IM_{Ri}, IM_{H}), \quad (15)

m_{SSIM} = \max_i SSIM(IM_{Ri}, IM_{H}), \quad (16)

and

m_{ET} = \min_i ET(IM_{Ri}, IM_{H}). \quad (17)

Three scale factors of 2, 3, and 4 were tested.

III. RESULTS

A. Experiment 1

Fig. 2 shows a snapshot of the captured thermal image using FLIR A655sc with a spatial resolution of 640 × 480 pixels. As seen in Fig. 1(c), the blackbody calibrator is an off-the-shelf unit with a ridged hot plate. The ridges are clearly seen in Fig. 2. In typical calibration measurements, having a flat hot plate may not be efficient as the data may be influenced by the angle of measurement and often needs to be compared with multiple sources. Having concentric ridges allows the global average of the temperature and provides a more accurate measure of the temperature.

A total number of 4, 9, and 16 images with this resolution were captured for the scale factor of 2, 3, and 4 respectively. To better demonstrate the details of improvement, six regions of interest with the size of 20 × 20 pixels, as highlighted in Fig. 2, are compared between the raw image and super-resolved images in Fig. 3. Zones 1-5 show the performance on high contrast areas while Zone 6 shows the performance on a relatively low contrast area. It can be clearly observed that the proposed SRE4T technique significantly improved the sharpness of both high and low contrast boundaries and is evidenced by reduced pixilation and improved sharpness of the image. With the increment of the scale factor, more and more details have been recovered in the HR images. The selected zones also include different directions of boundary, including 0º (Zone 2), 45º (Zone 1, 3 and 4), 90º (Zone 5 and 6). Results demonstrate that this system can improve the spatial resolution in all observed directions. In Zone 2, the ‘v’ shape feature is presented in a much clearer manner using the scale factor 4, in comparison with the raw captured image. Fig.4 shows a digital image of the Zone 2, where the small feature can be clearly observed. This level of improvement is unlikely to be achieved using the traditional interpolation based approach.

To explore more details of improvement, a vertical cross section in the middle of the image for Zone 2 and a horizontal cross section for Zone 5 are shown in Fig. 5 to compare the difference between the raw image (denoted by the blue curve) and the HR image (denoted by the red curve) with the scale factor 4. It can be clearly observed that the red curve has a higher slope than the blue curve between the region of 2-3 mm along the x axis. This observation suggests that the produced HR image is a better representation of the ground truth, where the black body has a sharp temperature change on that region.

It should be noted that the performance of the introduced technique highly depends on the accuracy of the motions. Fig. 6 plots the comparison between the estimated motions (blue dots) using the employed image registration method and the ideal motions (red dots) for the three scale factors. The absolute errors of both directions are shown in TABLE II. It suggests that a) the error is smaller than 0.03 pixels for both directions; b) the error in the y axis is higher than that in the x axis which may be due to the stage layout or the fact that α was calibrated in x direction only; and c) the error increases following the increment of the scale factor, which is potentially caused by human error due to the reduced movement step of the stage. The observation c) also indicates that the maximum scale factor may be not achievable due to the increased error of motion following the increment of the scale factor.

Fig. 2. A representative thermal image of the blackbody calibrator acquired using FLIR A655sc, where the temperature was set as 38°C and the room temperature is 22°C. The regions of interest for resolution improvement are highlighted by rectangles.

Fig. 3. Comparison of super-resolved high-resolution image for the passive thermography using FLIR A655sc. The selected regions are highlighted in Fig. 2 from Zone 1 to 6 respectively. It should be noted that the colormap could be different with Fig. 2 for better visualisation.
B. Experiment 2

Fig. 7 shows a snapshot of the captured thermal image using FLIR ONE with a spatial resolution of 160 × 120 pixels. In comparison to Fig. 2, the poor, degraded quality of the image can be clearly observed. In line with the lower pixel resolution, wider angle of the lens, miniature sensor size and a large stand-off distance clearly contributes to the image quality. Further, the image shows a great deal of pixilation even at the full field of view even before reviewing the highlighted zones of interest. Super-resolved results of the highlighted six regions of interest with the size of 5 × 5 pixels (to ensure the same spatial size as the Experiment 1) are as shown in Fig. 8. It can be observed that the image sharpness on boundaries has had a large improvement for each direction. The image quality becomes better and better following the increment of the scale factor. However, the level of improvement is not as significant as that of Experiment 1, even though the motions applied are very close to the ideal values, as shown in Fig. 9.

C. Experiment 3

This section aims to quantify the quality improvement using the proposed technique. The well-accepted nearest neighbour and bicubic interpolation method are selected as the baseline. Each $IML_i$ was applied by these interpolation methods and compared with $IMR_i$ to calculate the PNSR, SSIM and Entropy for each pair. The maximum of PNSR and SSIM, and minimum of Entropy were then calculated, based on Eqs. (15) - (17), to represent the improvement of the interpolation methods.

The comparison of calculated criteria for two interpolation methods and the proposed technique is as shown in TABLE III. Taking the $m_{PSNR}$ values for example, it can be calculated that the proposed method produced

$$\frac{(41.70 - 31.96)}{31.96} = 30.5\% \quad (18)$$

$$\frac{(40.65 - 31.32)}{31.32} = 29.8\% \quad (19)$$

$$\frac{(35.36 - 28.60)}{28.60} = 23.6\% \quad (20)$$

<table>
<thead>
<tr>
<th>Scale factor</th>
<th>X axis (pixel)</th>
<th>Y axis (pixel)</th>
</tr>
</thead>
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<tr>
<td>2</td>
<td>0.0099±0.0097</td>
<td>0.0215±0.0191</td>
</tr>
<tr>
<td>3</td>
<td>0.0127±0.0123</td>
<td>0.0220±0.0159</td>
</tr>
<tr>
<td>4</td>
<td>0.0240±0.0207</td>
<td>0.0294±0.0172</td>
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</table>

Fig. 4. A snapshot of the observed ‘v’ shape feature (red circled) shown in Zone 2.

Fig. 5. 1D plots comparison between the raw LR image and the 4x super resolution image using FLIR A655sc.

Fig. 6. Measured motion in x and y directions for the thermal image using FLIR A655sc when the IR camera moves (blue dots), where the ideal motion parameters are also plotted (red dots).
increment against the nearest neighbour interpolation for the scale factor 2, 3, and 4, respectively. In comparison with the most well-accepted bicubic interpolation, our method produced 21.7%, 11.9%, and 10.1% increment in percentage. Similar observations are applicable on $m_{SSIM}$ and $m_{ET}$. The proposed method consistently produced the best results with a significant margin.

Fig. 10 plots the visual comparison between the raw HR image (640 × 480), down-sampled LR image (160 × 120), the bicubic interpolated HR image (640 × 480) and the HR image (640 × 480) produced by the SRE4T system with the scale factor of 4. A region of 120 × 120 pixels of the HR image is shown to better visualise the difference. It can be clearly observed that the proposed method produced a much better recovery of the ground truth. Whilst, achieving the image close to the raw HR image would be an ideal case, the sensor currently does not come with that level of refinement in the real case, and is evidenced by the LR image. The boundary on the bicubic interpolated image through improved from the pixelated LR image, the image now includes a minor distortion combined with blurriness of the image boundary. The super-resolved image however shows significant improvement in comparison with the LR image. Further, the sharpness of the image seems to have also improved and shows a better image in comparison with the bicubic interpolated image. The only minor downside is that the outer edge which is close to the reflected temperature of the room adds edge artefacts (boundary between blue and yellow band), whereas the high temperature bands (represented by the various shades of red) shows a true similarity with the raw HR image indicating that the performance of the sensor above the reflected temperature could improve the overall quality of the object being investigated.

### IV. DISCUSSION

**Motion mode:** This paper introduces a representative method that allows for global motions to be incorporated during data capture, where the IR camera was mounted onto the xy translation stage. The choice of using an appropriate method needs to be evaluated to achieve controlled motion, which is critical to improve the image quality. For instance, the global motion should be achieved by considering if the camera can be mounted onto a suitable translation stage or the sample being tested. Additionally, an appropriate field of view must be
chosen to ensure only the targeted object is shown in the scene, through selecting the region of interest, changing the lens, or adjusting the working distance.

**Passive and Active mode:** It should be noted that this study only focuses on passive thermography where there is no excitation involved and the temperature distribution of object does not change. The proposed SRE4T technique also has the potential to be applied on the pulsed flash thermography where the temperature of object changes and the data is recorded as a function of time. One uncertainty introduced by the active mode, which could affect the performance, is the actual applied heat. The assumption of the SRE4T technique is that the thermal behaviour of the object does not change for tests with different motions. It is difficult to control the heat source to ensure the heat applied on the object surface is exactly same for multiple tests as the system is still analogous in nature. The second difficulty is that the images selected for registration and reconstruction must be extracted at the same timestamp. This can be challenging due to the limitation of the sample rate and the potential difference from the initial temperature.

**Maximal achievable scale factor:** Theoretically, this value depends on the working distance, stage step and camera specifications. The results in this paper have shown that the accuracy of motion control becomes more and more challenging following the increment of the scale factor. It could be caused by the human error when operating the stage, or the physical limitation of the stage. One potential solution is to automate this process by using a motorised xy translation stage. The stage movement, data capture and image reconstruction can be automatically implemented using an algorithm. The advantages are that 1) motion error caused by human can be reduced; 2) the operating speed of this system will be much faster.

### V. Conclusions

Aiming to advance thermography by improving its accuracy and reliability, and adaptability on in-service inspection, this paper proposes a robust SRE4T system to improve spatial resolution benefiting from accurately controlled sub-pixel movements. Both quantitative and qualitative results, for a high-end IR camera and a low-end IR camera, showed that this solution can significantly improve the spatial resolution of the acquired thermal images at the expense of consuming more time during data collection and the extra cost of the translation stage that is usually much cheaper than upgrading to a high-resolution IR camera.

It should be noted that the experiments of this paper focus on passive thermography, where it is assumed that the thermal diffusion during data acquisition is saturated and that no external pulse or excitation has been used to alter the diffusion. The speed to capture data is therefore not important theoretically. However, for real applications, it is always suggested to maximise the sample rate through an automated fast-moving x-y translation stage.

This technique will potentially be applied on active thermography to advance NDT, where the challenge is that, significant thermal diffusion takes place during data capture. Particularly, for high thermal-conductivity materials, such as metals and alloys, the thermal diffusion is quick and the sample rate must be fast enough to ensure there is no or very limited thermal diffusion in-between the captured low-resolution images. Such a problem could be mitigated through automatically controlling a high-speed camera and fast-moving stage, but the problem cannot be solved entirely. Therefore, this solution is more suitable to inspect low thermal-conductivity materials, such as CFRP. Another solution is conducting multiple-inspection process with identical inspection parameters except shifting the relative position between camera and sample, and then registering and reconstructing the low resolution images from the same time-stamp.

The proposed solution is also straightforward to extend to digital imaging. The ultimate aim is to advance the capability of the existing sensor through enhanced signal and image processing, thus achieving improved information on the features that will help discriminate the part with added confidence. Features which were once invisible, now become visible, the measurement accuracy is improved, which improves not just the overall performance but also our ability to make confident decisions based on the thermogram. Meanwhile, with the reduction of instrument cost, it is envisaged that this work will be adapted to both passive and active NDT.
active thermography and will encompass the multidisciplinary field of digital imaging.

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