

Neural Predictive Control of Broiler Chicken and Pig Growth

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Abstract

Active control of the growth of broiler chickens and pigs has potential benefits for farmers in terms of improved production efficiency, as well as for animal welfare in terms of improved leg health in broiler chickens. In this work, a differential recurrent neural network (DRNN) was identified from experimental data to represent animal growth using a nonlinear system identification algorithm. The DRNN model was then used as the internal model for nonlinear model predictive control (NMPC) to achieve a group of desired growth curves. The experimental results demonstrated that the DRNN model captured the underlying dynamics of the broiler and pig growth process reasonably well. The DRNN based NMPC was able to specify feed intakes in real time so that the broiler and pig weights accurately followed the desired growth curves ranging from -12% to $+12\%$ and -20% to $+20\%$ of the standard curve for broiler chickens and pigs, respectively. The overall mean relative error between the desired and achieved broiler or pig weight was 1.8% for the period from day 12 to day 51 and 10.5% for the period from week 5 to week 21, respectively.

Keywords: Predictive Control, Broiler, Pig, Growth, Optimal Control, System Identification, Neural Network Models

1. Introduction

This work forms part of a programme to determine, model and control the biological and physical responses and interactions of poultry and pigs to dynamic changes in their physical environment. In particular, it studies the growth and behaviour of broiler chickens and pigs reared for meat production and their ammonia emissions in response to dynamic changes in feed quantity, light intensity, temperature and relative humidity. This paper builds on early data for broilers growth published by Demmers et al. (2010) and focusses primarily on the growth of both broilers and pigs.

Growth of an animal integrates various physiological and environmental processes, so weight gain is not only a valuable measure of economic performance, but also a convenient measure of environmental response. Maximal growth rate as a function of feed intake is the most important parameter from the perspective of growers, because feed is the biggest cost in the production of housed livestock. Recently other physiological processes such as skeletal development of and activity of broiler chickens have also been considered. Slower growth in the early stages of broiler development reduces the incidence of lameness, the most important animal welfare issue in broiler production (Butterworth & Arnould, 2009), whilst liquid phase-feeding has the potential to improve pig health and growth (Scott et al., 2007).

Frost et al. (1997) argued that livestock production systems contain multiple interconnected processes that need to be managed to meet several performance criteria, including economic, animal welfare and environmental targets. Traditional management was, and still is, largely based on experience and is not good at integrating processes and performance criteria. An example is the use of climate (temperature) controllers. Development of the climate controller was through observing animal performance and behaviour (Charles & Walker, 2002). However, control was through temperature measurement alone, discarding any information from the animal. The stockman still had to intervene if the response of the animals indicated that the temperature control was imperfect. The proposed solution was to move towards integrated closed-loop, model-based control systems, by first developing controllers for the key processes, using sensor technology capable of measuring animal responses, that was becoming available.

The nutritional and environmental requirements of broilers and pigs are

36 well understood (Gous et al., 1999; Kyriazakis & Whittemore, 2006), which
37 has enabled the development of mechanistic models to predict broiler and pig
38 growth from feed inputs (Emmans, 1995; Black, 2014). These models and
39 the science underlying them have been used to create plans for nutrition and
40 weight gain (Aviagen, 2002; PIC, 2005). However, the dynamic responses
41 of animals to (sudden) changes in the environment are less well understood
42 and fewer models exist. Furthermore, Wathes et al. (2008) states that in
43 general mechanistic models are not suitable for control purposes, because
44 they are often overly complex, with too many parameters, although these
45 have biological meanings, and inaccurate, since parameter values may change
46 over time and space.

47 Recently, data-based models describing the response of the growing broiler
48 to changes in feed quantity have been explored as an alternative to mechanis-
49 tic models. Data-based modelling techniques estimate the unknown model
50 parameters of any abstract mathematical model structure from measure-
51 ments of process inputs and outputs. In principle, the parameters can be
52 estimated on-line resulting in an adaptive model that can cope with the char-
53 acteristics of most biological processes, *i.e.* complex, individual, time variant
54 and dynamic (Aerts et al., 2003b). This type of model has the advantage
55 that no *a priori* knowledge of the process is required, although the latter is
56 beneficial whilst developing the model. However, in contrast to mechanistic
57 models, the parameters have no biological meaning. The resulting model
58 will in general be more compact and therefore suitable for control purposes.
59 As a result data-based models are widely used for process control in other
60 industries. Various approaches to modelling broiler growth have been used,
61 including hyperbolic models (Ahmadi & Mottaghitalab, 2007), artificial
62 neural networks (Ahmadi & Mottaghitalab, 2008) and recursive linear mod-
63 els (Aerts et al., 2003b).

64 Frost et al. (2003) and Stacey et al. (2004) described the development of a
65 system based on a mechanistic model to control the feeding of broiler chickens
66 to achieve a given time-weight performance. The system was developed on
67 farm scale (over 30,000 birds/house) using a feeding system where the diet
68 composition was controlled by blending two different feeds and growth was
69 monitored by perch weighers. It aimed to optimise the feed blend to minimise
70 the errors from a planned growth curve from the current day to slaughter,
71 and was able to deliver birds of the correct weight, except when growth
72 was inhibited by disease. A pig growth monitoring system based on image
73 analysis (Doeschl-Wilson et al., 2004; Schofield et al., 1999), supported the

74 development of a mechanistic model and a real time controller for pig growth
75 (Parsons et al., 2007). The model was able to control mean pig weight in
76 trials to within 2 kg of the target weight, by varying crude protein content
77 of the diet. The use of a mechanistic simulation models for broilers and
78 pigs based on the nutritional and environmental requirements, required the
79 specification of several genotype-dependent parameters and feed analysis in
80 terms of several nutrients, rendering them less suitable for control purposes.

81 For the reasons discussed above, a data-based approach was followed on
82 laboratory scale by Aerts et al. (2003a) and at a larger scale by Cangar
83 et al. (2008), in which the quantity of feed presented was controlled using
84 model predictive control. They used a recursive linear models with time
85 varying parameters to predict weight 3–7 days ahead (Aerts et al., 2003b;
86 Cangar et al., 2008). Using online prediction of the feed quantity, control
87 of broiler growth along a target trajectory proved possible within certain
88 boundary conditions. Most notably, the period during which growth could
89 be restricted without affecting the ability of the broiler to reach the target
90 weight was limited to the early stages of growth (age 7–30 days). Growing
91 broilers to the required target weight using online control resulted in a mean
92 relative error of 6–10% in live weight.

93 The method described here shares some of the characteristics of the above
94 approaches and aims to overcome some of their limitations. The model is
95 empirical, so does not require genetic parameters or detailed feed analyses,
96 but simulates growth from hatching to slaughter. Based on this model, the
97 controller is designed to optimise feeding over the complete period of growth
98 instead of a fixed horizon. The control strategy aims to optimise the system
99 by reducing the feed intake to save cost, minimising the deviation of bird
100 weight from a predefined grow curve to ensure the final target is smoothly
101 achieved and at the same time restricting the daily change in the intake to
102 avoid potential stress on the birds. These objectives are combined into a
103 single cost function as a weighted sum of these criteria.

104 This paper is organised as follows. In section 2, after a brief description
105 of broiler and pig growth and the experimental data, the DRNN model is
106 introduced and developed to represent the growth dynamics. The growth
107 control problem is then defined in section 3 and solved using the DRNN
108 model and the NMPC framework. The performance of the DRNN model
109 and the NMPC algorithm are demonstrated through experiments in section
110 4. A discussion of the results and the conclusions are given in section 5.

111 2. Weight-Feed Model Identification

112 Growth of any organism is a complicated nonlinear dynamic process,
113 which is difficult to model from first principles. Most conventional system
114 identification approaches use linear model structures, such as the autoregres-
115 sive moving average with exogenous input model (ARMAX). The latter can
116 be adapted to account for variability in time and therefore non-linear systems
117 (RARMAX), but the time-varying nature is dependent on the actual state
118 trajectory, which the linearisation takes as a reference trajectory. This po-
119 tentially limits their use to specific applications where the trajectory of the
120 model developed is similar to that of future applications. Due to their abil-
121 ity to approximate any nonlinear function, recurrent neural networks (RNN)
122 are widely used for nonlinear system identification. However, most available
123 RNN models are in discrete time, which can only work for the specific sam-
124 pling rate with which the model is trained. In order to develop a dynamic
125 model to control the entire growth process with potentially variable sampling
126 rate, the differential RNN (DRNN) and the associated automatic differenti-
127 ation based training algorithm developed by Al-Seyab & Cao (2008b,a) were
128 adopted for this work. DRNN models are black box models and the internal
129 parameters are not transparent, unlike the external input and output vari-
130 ables, in this case feed intake and liveweight under various conditions, which
131 can be interpreted from a biological point of view.

132 A first order DRNN model with two hidden nodes represented as follows,
133 adopted to represent the broiler growth process.

$$\dot{x} = w_5\sigma(w_1x + w_3u) + w_6\sigma(w_2x + w_4u) \quad (1)$$

134 where x and u are the weight and feed intake, respectively, for a single
135 bird, $\sigma(x) = \frac{e^x - e^{-1}}{e^x + e^{-1}}$ and w_1, \dots, w_6 are model parameters to be determined.
136 The model structure is determined based on the intuitive assumption that
137 from any initial weight, x_0 , if the feed intake is zero, then the animal's weight
138 will gradually decay to a constant.

139 To represent the pig growth equally a first order model with one state
140 and 2 hidden nodes was adopted:

$$\dot{x} = W_2\sigma(W_x x + W_u u + b_1) \quad (2)$$

141 where x and u are the weight of a pig and the feed intake, respectively,
142 W_2, W_x, W_u and b_1 are model parameters to be determined and the current

143 temperature is a disturbance in the growth models as this is gradually re-
144 duced over the experimental period for broilers and an experimental factor
145 in the pig trials.

146 To generate data for training and validating the broiler models, broilers
147 were grown from 1 day old to 51 days. The broilers were exposed to dynamic
148 (sudden) changes in the inputs, feed amount, light intensity and relative
149 humidity (RH) from day 12 onwards. To ensure a measurable response in
150 output, the change in the input was set unrealistically large compared to nor-
151 mal broiler production practise. Feed amount was set at either 90% or 110%
152 of recommended feed requirements for broilers (Aviagen, 2002). Light inten-
153 sity was set at either 10 or 100 lux and RH at 56% or 70%. The frequency
154 of change was set according to the time required to reach a new steady state
155 in the output, *i.e.* hours for the light intensity and 3–7 days for feed amount
156 and RH. A two-level (change or no change) of three-factor (feed amount,
157 light intensity and RH) factorial design requiring $2^3 = 8$ identical rooms
158 was used and repeated in three trials. Each possible combination of inputs
159 was randomly allocated to a room in each of the three trials. This experi-
160 mental design potentially allowed identification of interactions between the
161 processes: growth, activity and ammonia emission, affected by feed amount,
162 light intensity and RH, respectively.

163 Each room housed 262 broilers (Ross 308) on a bed of woodshavings up
164 to a maximum stocking density of 33 kg m^{-2} at 50 days. The average bird
165 weight was estimated continuously using a weighing platform suspended from
166 a load cell (Fancom 747 series bird weight platform and computer). Specially
167 produced animal feeds were weighed and dosed automatically to each room
168 (Fancom 771 feed computer) four times a day. Feed quantity dosed and
169 broiler weight in each room were recorded automatically four times per day
170 from day 3-51. Other environmental variables, such as temperature, RH and
171 light intensity, were monitored and recorded at 1 minute intervals.

172 To generate data for training and validating the pig models, pigs (Large
173 white, Landrace and Pietran cross) were housed from 5 weeks of age to 22
174 weeks. Pigs were exposed to dynamic changes in feed amount and temper-
175 ature from week 6 onwards. The change in feed amount was set at either
176 80% or 120% of recommended feed requirements for pigs and to +7 C above
177 the recommended room temperature at 3 week intervals. A two-level of two-
178 factor (feed amount and temperature) factorial design with four identical
179 pens in two rooms was used and repeated in two trials, which potentially
180 allowed identification of interactions between the processes growth and am-

181 monia emission, affected by feed amount and temperature, respectively.

182 Each room was divided in 4 identical pens which housed 10 pigs on a
183 part slatted floor with straw on the solid floor. The average pig weight
184 was measured daily using the visual image analysis system (Osborn Ltd),
185 validated by weighing the pigs every 14 days using a weighing crate. Specially
186 produced animal feeds were weighed and dosed automatically to each pen
187 twice daily. Feed quantity dosed was recorded automatically and animal
188 weights averaged daily.

189 To determine the model parameters, experimental data from the trials
190 described above were used. Each batch contained the input and output data
191 for one room or pen from one trial. The training data set consisted of six
192 batches, two from each trial, and five batches, drawn from both trials, for
193 broilers and pigs respectively. Another six and three batches, for broilers and
194 pigs respectively, were selected for validation.

195 The training process started from a set of randomly generated parameters.
196 The growth of a batch was then calculated from the initial weight and the
197 feed intakes recorded in the data by solving the model equation (1) using the
198 automatic differentiation approach described by Cao (2005). Let the bird
199 weight recorded in experiments and estimated from (1) at each sampling time
200 be x_k and \hat{x}_k , $k = 1, \dots, N$, respectively. Then the training process aimed
201 to minimise the following cost function by adjusting the model parameters
202 w_1, \dots, w_6

$$\min_{w_1, \dots, w_6} \sum_{k=1}^N (x_k - \hat{x}_k)^2 + \sum_k^6 \alpha w_k^2 \quad (3)$$

203 where α is a weighting factor for the model parameters. The second term of
204 the cost function is for rigid regulation, which improves the model generality.

The optimization in (3) was converted into a standard nonlinear least squares problem and solved using the Levenberg-Marquardt (LM) algorithm (Marquardt, 1963), where the model parameters were iteratively updated to reduce the cost function until the algorithm converged or the validation cost started to increase. To avoid the training process being trapped in a local minimum, the optimization procedure was repeated with different sets of randomly generated initial parameters until a satisfactory model was obtained. The final model parameters obtained for the broiler growth model

were:

$$\begin{aligned} w_1 &= -2.8456 \times 10^{-4} & w_2 &= 1.0162 \times 10^{-4} \\ w_3 &= -2.5539 \times 10^{-3} & w_4 &= 4.2284 \times 10^{-3} \\ w_5 &= 756.5 & w_6 &= 1488.5 \end{aligned}$$

and for the pig growth model:

$$W_x = [-0.3649 \quad 0.2254]^T$$

$$W_u = \begin{bmatrix} 0.6443 & -0.0912 \\ 0.3980 & 0.0621 \end{bmatrix}$$

$$\begin{aligned} b1 &= [0.0903 \quad -0.0347]^T \\ W_2 &= [0.3870 \quad 0.5538] \end{aligned}$$

205 The broiler growth system is stable at the equilibrium point $x = 0$ and
 206 $u = 0$. This can be verified by the pole of the system at this point, $p =$
 207 $w_1 w_5 + w_2 w_6 = -0.064 < 0$. Equally, the pig system is stable as $x = 0$ as
 208 $W_2 W_x = -0.0164 < 0$. Therefore, the model indicates that for zero intake,
 209 the weight of a bird or pig will in theory eventually decay to 0, but in practice
 210 will decay to a constant e.g. the carcass.

211 The performance of the trained DRNN model is given in table Table ??
 212 Typical performance of the trained DRNN model is represented for one of the
 213 remaining 12 test batches in Figure 1, which shows that the trained DRNN
 214 was able to predict the bird weight satisfactorily even when the actual feed
 215 intake was modulated by regular step changes. As with the broiler growth
 216 model the pig growth DRNN model predicted the actual growth well, with an
 217 average validation index $\gamma^2 = 0.9889$, with $\gamma^2 = 1 - \frac{\sum(x - x_{model})^2}{\sum x -$
 218 $x_{mean})^2$.

219 3. Livestock Growth Control

220 In theory, using the identified DRNN model, many optimal control prob-
 221 lems can be investigated, such as minimum time control, where feed intakes
 222 are calculated such that animals can grow as fast as possible to reach the

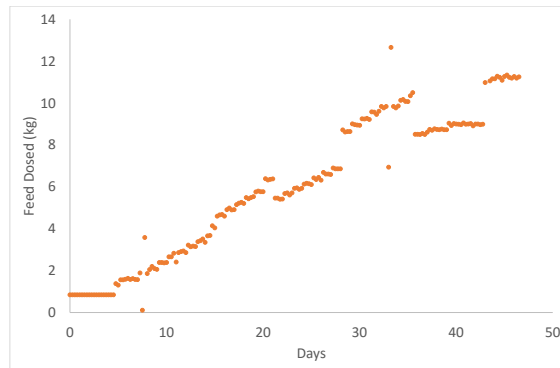
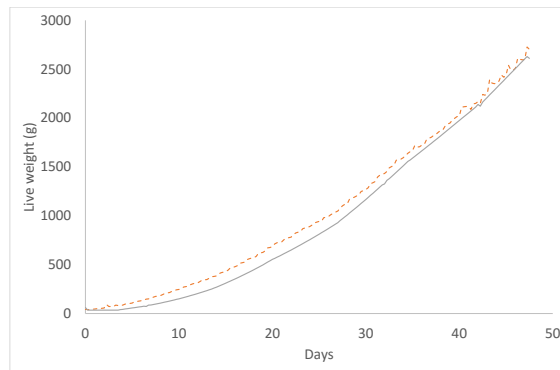


Figure 1: DRNN model testing. Top: the actual (solid-line) and predicted (dashed-line) broiler weight; Bottom: the actual feed dosed to the room holding 262 broilers (corrected for mortality).

Table 1: The performance of the Differential Recurrent Neural Network models for broiler or pig growth for each of the data sets. Factors used are changes in feed, light, humidity and temperature indicated by F,L, H or T for the active state and f, l, h and t for the corresponding control or normal state.

species	factor used	batch 1	batch 2	batch 3
broiler	f l h	0.9985	0.9976	0.9984
broiler	f L h	0.9989	0.9968	0.9943
broiler	f l H	0.9637	0.9976	0.9983
broiler	f L H	0.9862	0.9970	0.9965
broiler	F l h	0.9993	0.9981	0.9989
broiler	F L h	0.9886	0.9957	0.9965
broiler	F l H	0.9898	0.9984	0.9982
broiler	F L H	0.9954	0.9970	0.99887

species	factor used	batch 1	batch 1a	batch 2	batch 2a
pig	f t	0.9901	0.9882	0.9901	0.9910
pig	f T	0.9947	0.9889	0.9952	0.9924
pig	F t	0.9560	0.9856	0.9884	0.9904
pig	F T	0.9931	0.9944	0.9933	0.9920

223 target weight, and the minimum food problem, where optimal feed intake is
 224 designed such that the total food consumption is minimized to achieve the
 225 same target weight on the target day. However, due to the limited experi-
 226 mental data, upon which the model was based, it would not be applicable to
 227 some extreme situations, such as very low and high feed intakes. To ensure
 228 the model was working within a reliable range that would not compromise
 229 animal welfare, a regulation control problem was constructed to design op-
 230 timal feed intake such that the actual animal growth followed a predesigned
 231 curve smoothly with the minimum feed intake.

232 The above regulation problem was solved through a nonlinear model pre-
 233 dictive control (NMPC) scheme. In the NMPC, at each sampling point, t_0 ,
 234 the average weight of an animal predicted by the model, x_0 is compared with
 235 the measured weight, x_m . The difference, $n = x_m - x_0$ is treated as the dis-
 236 turbance. This disturbance is assumed to be constant within the prediction
 237 horizon, $t_0 \leq t \leq t_f$. Therefore, to correct the error caused by this distur-
 238 bance, the actual set-point at a time point, t , within the prediction horizon
 239 is biased as $\hat{x}(t) = x_r(t) + n$, where $x_r(t)$ is the target weight. Then, the
 240 optimal control problem to be solved at each sampling point, t_0 is stated as

241 follows.

$$\min_u \sum_{t=t_0}^{t_f} [\alpha_1^2(x(t) - \hat{x}(t))^2 + \alpha_2^2 v^2(t) + \alpha_3^2(\Delta v(t))^2] \quad (4)$$

$$\text{s.t.} \quad \dot{x} = w_5 \sigma(w_1 x + w_3 u) + w_6 \sigma(w_2 x + w_4 u) \quad (5)$$

$$x(t_0) = x_0 \quad (6)$$

$$x(t_f) = x_f \quad (7)$$

242 where, $v^2(t) = u(t)$ is the feed intake at day t , $\Delta v(t) = v(t) - v(t-1)$, t_0 and
 243 t_f are current and final days, respectively, x_0 and x_f are current and final
 244 weights, respectively, α_1 , α_2 and α_3 are weights of the optimization problem
 245 for weight accuracy, food consumption and smoothness respectively. Note
 246 that although the optimal control problem in (4) is open loop, the correction
 247 of modelling error, $\hat{x}(t) = x_r(t) + x_m(t_0) - x_0$ uses the real measured weight,
 248 $x_m(t_0)$, hence the actual control is feedback control.

249 The problem can be cast as a standard nonlinear least square problem,
 250 $\min_{\mathbf{u}} \mathbf{e}^T \mathbf{e}$, with residuals, \mathbf{e} defined as follows.

$$\mathbf{e} = \begin{bmatrix} \alpha_1(x(t_0 + 1) - \hat{x}(t_0 + 1)) \\ \vdots \\ \alpha_1(x(t_f) - \hat{x}(t_f)) \\ \alpha_2 v(t_0) \\ \vdots \\ \alpha_2 v(t_f - 1) \\ \alpha_3 \Delta v(t_0) \\ \vdots \\ \alpha_3 \Delta v(t_f - 1) \end{bmatrix} \quad (8)$$

251 The corresponding Jacobian, $\mathbf{J} = \partial \mathbf{e} / \partial \mathbf{u}$ can be derived through automatic
 252 differentiation as explained by Al-Seyab & Cao (2008b). The optimal values
 253 of $\mathbf{v} = [v(t_0), \dots, v(t_f - 1)]^T$ are then obtained iteratively using the LM
 254 algorithm (Marquardt, 1963):

$$\mathbf{v}_{k+1} = (\mathbf{J}_k^T \mathbf{J}_k + \mu \mathbf{I})^{-1} \mathbf{J}_k^T \mathbf{e}_k \quad (9)$$

255 where \mathbf{e}_k and \mathbf{J}_k are the residuals and the Jacobian corresponding to \mathbf{v}_k , μ
 256 is a parameter adjusted by the algorithm to maintain a fast convergence.

257 Once the iteration had converged, the first instance of the obtained opti-
258 mal solution, \mathbf{v} was converted into the feed intake, $u(t_0) = v^2(t_0)$ and applied
259 to the real system. The whole procedure will be repeated at next sampling
260 time when a new measured average animal weight, x_m is available.

261 4. Validation of the Growth Control Algorithm

262 To validate the control algorithm developed in the previous section, fresh
263 experiments were designed and carried out. In these experiments, new growth
264 curves were devised for the controller to attempt to follow as closely as possible
265 by predicting the required feed intake. These new growth curves were
266 derived from the recommended (standard) growth curve for broilers provided
267 by Aviagen (2002), e.g. reaching a weight of 2.85 kg at 50 days of age and
268 the recommended growth curve for pigs PIC (2005), e.g. reaching a weight
269 of 92 kg at 21 weeks of age and were used for the development of the controller.
270 The broilers were grown according to the standard curve up to day
271 12 and from day 12 to 50 followed the new growth curves. The pigs were
272 grown according to the standard curve till week 6 and then followed the new
273 growth curves. The new growth curves for broilers were specified as,

- 274 • standard curve
- 275 • +12% of standard curve
- 276 • -12% of standard curve
- 277 • -12% to day 30 followed by +12% of standard curve (slow growth
278 followed by recovery growth)

279 and for pigs as

- 280 • standard curve
- 281 • alternating each 3 weeks between -20% and +20% of the standard
282 curve

283 The broiler growth controller was tested using four of the eight available
284 rooms. Each growth curve was tested with one room. Each room was initially
285 stocked with 265 day-old chicks (Ross 308). The pig growth controller was
286 tested using 8 pens in two rooms with the growth curves tested in paired

287 pens, each holding 10 pigs. Environmental conditions were kept identical to
 288 the conditions used in the training and model validation trials, apart from the
 289 frequency of light intensity change and number of meals fed daily for broilers
 290 and room temperature for pigs. The total daily intake of each room or pen
 291 was set by the controller. The controller was used for on-line calculation
 292 of the feed intake, however with a 24-hour delay in implementation of the
 293 calculated feed intake through a manual adjustment of the feed dosed.

294 The production results for broilers from the 4 batches and pigs from the
 295 2 batches are summarised in Table 2 and Table 3, where the four controlled
 296 (actual) weights at the end of the growth curve are compared with their
 297 corresponding target values taken from the prescribed growth curves. The
 298 predicted total feed intake was calculated from the sum of the controller-
 299 predicted feed dosage rate. The actual total feed intake was calculated from
 300 the sum of the feed dosed, corrected for the actual number of birds present.
 301 The mean relative error and maximum deviation of the actual weights from
 302 day 12–50 for broilers or week 6 to 21 for pigs were calculated as percentages,
 303 where the mean relative error, $\bar{\varepsilon}$ and the maximum deviation, σ_{\max} are defined
 304 based on the actual weight, w_{act} and the corresponding target weight, w_{th} as
 305 follows.

$$\bar{\varepsilon} = \frac{1}{39} \sum_{d=12}^{50} \left| \frac{w_{\text{act}}(d) - w_{\text{th}}(d)}{w_{\text{th}}(d)} \right| \quad (10)$$

$$\sigma_{\max} = \max_{12 \leq d \leq 50} \left| \frac{w_{\text{act}}(d) - w_{\text{th}}(d)}{w_{\text{th}}(d)} \right| \quad (11)$$

306 Daily comparisons of controlled against modelled and standard growth
 307 curves for broilers are shown in Figures 2 to 5 for the standard growth curve
 308 and +12%, -12% and -12% followed by +12% of standard growth curves,
 309 respectively.

310 The results for broilers clearly indicate that the controller is capable of
 311 predicting the feed intake required to reach the end weight and follow the
 312 reference growth curves well with an mean relative error less than 2%, ex-
 313 cept for the -12% curve. The larger mean relative error in the -12% growth
 314 curve was caused by a malfunction in the feeding equipment from day 16–19
 315 (see Figure 6). Although the room recieved the correct feed amount for
 316 each feeding period, due to blockages the feed was delivered to the birds
 317 at very irregular intervals, potentially inhibiting growth (maximum devia-
 318 tion from curve was -16%). However, the controller was able to return the

Table 2: Target live weight and achieved live weight of the broilers at age 50 days and goodness of fit of the achieved live weight compared to the set growth curve from day 12–50. Predicted and actual total feed intake per bird and feed conversion ratio (FCR) for the period of day 12–49. The standard growth curve had been derived from the optimal growth curve provided by Aviagen (2002).

Growth curve	unit	Standard	+12% of standard	-12% of standard	-12% & +12% of standard
Bird weight at 50 days					
Target	kg	2.85	3.20	2.51	2.85
Actual	kg	2.73	3.10	2.44	2.72
Mean relative error	%	1.8	1.8	2.8	1.6
Maximum deviation	%	5.2	6.0	16.3	5.0
Total feed intake from day 12–49					
Predicted	kg.bird ⁻¹	4.66	4.99	4.30	4.62
Actual	kg.bird ⁻¹	4.59	5.04	4.31	4.62
Feed conversion Ratio	-	1.91	1.84	2.02	1.93

Table 3: Theoretical live weight and achieved live weight of the pigs at age 21 weeks and goodness of fit of the achieved live weight compared to the set growth curve from age 6 to 21 weeks. Predicted and actual total feed intake per bird and feed conversion ratio (FCR) for the period of week 6–21. The standard growth curve had been derived from the optimal growth curve provided by PIC (2005).

Growth curve	unit	Standard	-20%/ + 20%/ - 20% of standard
Pig weight at 21 weeks			
Target	kg	91.9	88.4
Actual	kg	98.4	90.5
Mean relative error	%	10.5	10.9
Maximum deviation	%	34.1	35.3
Total feed intake from age 6 – 21			
Predicted	kg.pig ⁻¹	170.9	158.7
Actual	kg.pig ⁻¹	187.9	179.0
Feed conversion Ratio		2.40	2.50
Feed conversion Ratio	(to 35kg)	1.54	1.73
Feed conversion Ratio	(35-100kg)	2.71	2.79

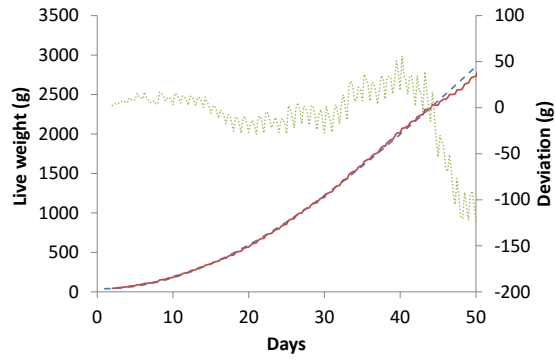


Figure 2: The target standard (dashed line) and actual achieved (solid line) growth curves of broilers and the deviation of the target curve (dotted line, secondary axis).

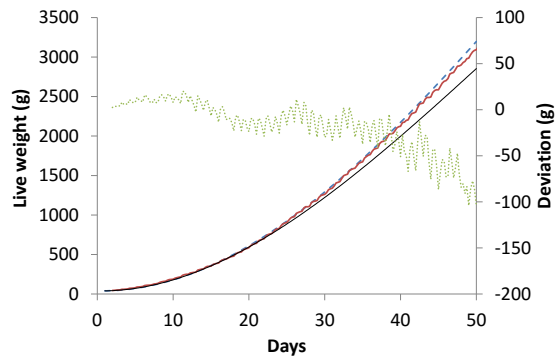


Figure 3: The target +12% above standard (dashed line) and actual achieved (solid line) growth curves of broilers and the deviation of the target curve (dotted line, secondary axis). The standard growth curve (Aviagen) is plotted for comparison.

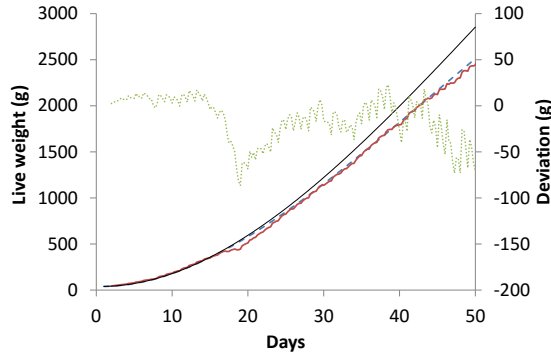


Figure 4: The target -12% below standard (dashed line) and actual achieved (solid line) growth curves of broilers and the deviation of the target curve (dotted line, secondary axis). The standard growth curve (Aviagen) is plotted for comparison.

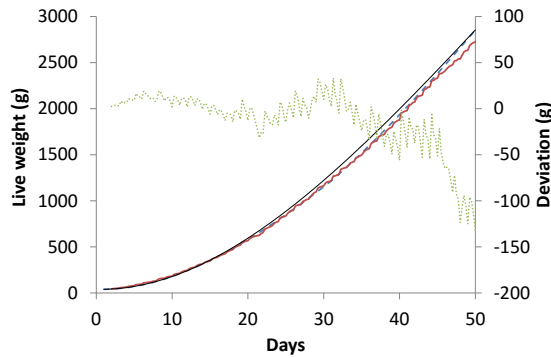


Figure 5: The target -12% followed by $+12\%$ of standard (dashed line) and actual achieved (solid line) growth curves of broilers and the deviation of the target curve (dotted line, secondary axis). The standard growth curve (Aviagen) is plotted for comparison.

319 growth to the set curve within 4 days, by feeding more than originally an-
 320 ticipated. Excluding this period reduced the mean relative error to 1.9%.
 321 Overall the mean relative error in this work is much lower than the 7–9%
 322 reported by Cangar et al. (2008). The authors suggested that this high error
 323 might be largely due to different conditions and systems for the weighing
 324 and feed delivery used for generating data for creating and validating their
 325 model (small scale, "ideal" conditions) and for the validation of the control
 326 algorithm (commercial conditions). In our work all steps were done on the
 327 same scale, same conditions and with the same equipment. further more the
 328 number of birds used in their trials was substantially higher, especially in the
 329 commercial validation trials.

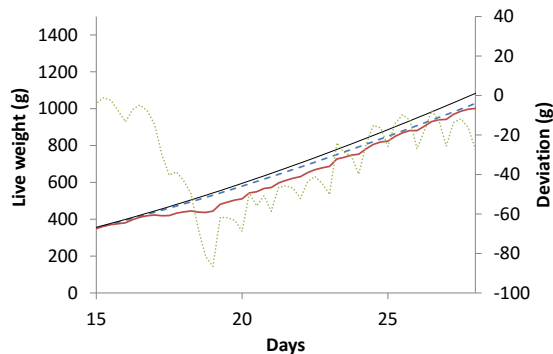


Figure 6: The target -12% below standard (dashed line) and actual achieved (solid line) growth curves of broilers and the deviation of the target curve (dotted line, secondary axis) for the period the feed system malfunctioned.

330 For all four broiler growth curves, the projected end weight was met
 331 within small tolerances. From day 42 onwards the actual bird weight started
 332 to deviate from the theoretical bird weight (slower growth). This could be
 333 a undesirable feature of the DRNN model used. However, it also coincided
 334 with the introduction of the withdrawal grower diet which in theory differs
 335 in composition from the normal grower diet in the absence of coccidiostats
 336 only. The absence of the coccidiostats should not affect the growth or feed
 337 conversion, but it is not evident from the feed analysis if other minor changes
 338 were made to the feed composition between the two deliveries that could have
 339 affected the growth. In contrast to findings by Cangar et al. (2008) in these

340 trials the Ross 308 bird appeared to be capable of recovery growth (see Figure
341 5), *i.e.* the broilers were capable of regaining weight in excess of equivalent
342 growth by the standard growth curve beyond 31 days. One reason for this
343 difference is the lower energy and protein content of the diets used in this
344 work compared with current industry standards (approximately 15% lower).
345 The standard growth curve used was also set below the maximum potential
346 growth curve given by Aviagen (2002). Hence, the broilers were capable of
347 utilising the additional protein and energy provided as the maximum growth
348 potential had not yet been reached.

349 The growth controller for pigs equally indicates that the controller is
350 capable of predicting the feed intake to meet the desired growth curve and
351 end weight (see Figure 7). However, the mean relative error was significantly
352 higher at 10.5% and 10.9%, for the standard and recovery growth curves,
353 respectively. The larger mean relative error is potentially due to the lower
354 number of data sets available for determining the DRNN model parameters,
355 compared to the broiler DRNN model, 5 v 6, respectively, and the lower
356 number of changes in feed amount. Equally, the slower rate of growth meant
357 the dynamic changes in weight due to the changed feed intake regime were
358 smaller compared to the broiler, potentially resulting in a less accurate model.
359 Creating even larger changes in the feed intake regime were however deemed
360 to be too detrimental for the pigs welfare. Another contributing factor is
361 the variation in temperature in the experimental conditions (standard versus
362 standard +7C). The effect of temperature on growth is well documented. Pigs
363 decrease their voluntary feed intake with increasing temperatures and hence
364 their average daily gain is lower (Hyun et al., 1998; Sutherland et al., 2006).
365 However, the FCR for the two temperature regimes was not significantly
366 different as was expected (Sutherland et al., 2006).

367 The DRNN model used in the controller controlled not only the daily
368 feed intake on line, but predicted accurately the required feed intake for the
369 whole of the growing period. This novel addition will be very useful to farm-
370 ers when deciding on a growth curve suitable for various scenarios. From the
371 four broiler growth curves used in this trial the +12% of standard growth
372 curve is better from an economic point of view, as it has by far the lowest feed
373 conversion ratio (FCR). The authors suggest this is largely due to making
374 better use of the genetic potential of the broilers. Using the slow growth with
375 recovery growth option, has potential advantages for animal welfare in terms
376 of leg health and proved to be no worse in achieving the final weight with
377 a similar FCR and total feed intake requirement, compared to the standard

378 growth curve. The FCR's achieved here are however significantly higher
379 than those commonly achieved on commercial farms, where the best pro-
380 ducers achieve 1.6 -1.7 FCR, approximately. The purposely lower protein
381 content of the feed used in these trials, approximately 15% less, appears to
382 be the root cause of the poorer FCR. The otherwise optimal environmen-
383 tal conditions had no negative effect on the FCR. Using optimal diets for
384 the genetic growth potential might reduce the effectiveness of the model to
385 recover lost growth over a number of days as shown in this work, as the
386 maximum daily weight gain had already been reached (Cangar et al., 2008).
387 The feed conversion ratio for pigs in these trials and especially the for the
388 standard growth curve which had the best performance in economic terms,
389 compares favourably to the industry average of 2.35 reported by BPEX
390 (2011, 2015) for rearer/finisher pigs combined (8-100 kg), as well as the indi-
391 vidual FCR's for rearer and finisher at 1.71 and 2.67, respectively, despite the
392 suboptimal lower protein content of the feed used in these trials. The optimal
393 environmental conditions in the new animal welfare facility and therefor the
394 significant reduction in disease burden on the pigs will have contributed to
395 the good growth performance.

396 5. Conclusions

397 An accurate differential recurrent neural network model of broiler and pig
398 growth has been identified, validated and tested successfully. The DRNN
399 model accurately described the dynamic time variable growth of housed live-
400 stock. Typically the mean square error and standard deviation between the
401 broiler growth model and data were of the order of 0.02 and 0.03, respectively
402 and the equivalent figures for the pig growth model were of the order of 0.02
403 and 0.05, respectively.

404 The nonlinear model predictive controller, incorporating the DRNN model,
405 was constructed to predict the feed quantity required for the broilers to grow
406 following predetermined growth curves. The NMPC accurately predicted the
407 feed quantity to achieve a range of predetermined growth curves. The mean
408 relative error for the period from day 12–50 was 1.8% for broilers and for pigs
409 10.5% for the period from 6 to 21 weeks. The NMPC was capable of accu-
410 rately predicting compensatory growth rates following two days of retarded
411 growth rates due to feeding equipment failure. In addition, the controller was
412 able to predict the total feed intake for the whole growth period accurately.

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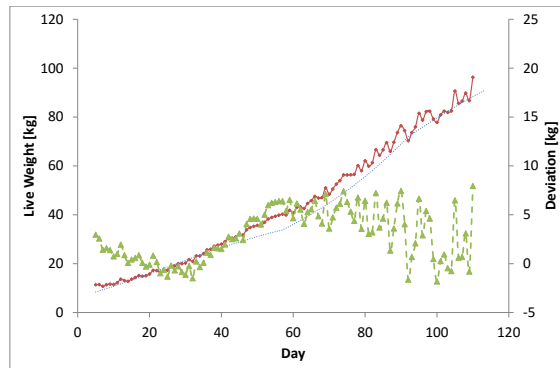
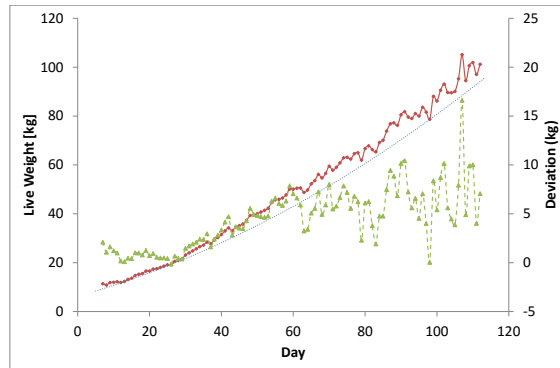


Figure 7: The target standard (top graph, dashed line) and variable (bottom graph, dashed line) and actual achieved (solid) growth curves for pigs and the deviation of the target curve (dotted line, secondary axis).