

Incorporating Feedforward Action into Self-optimizing Control Policies

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Abstract

The available methods for selection of controlled variables (CVs) using the concept of self-optimizing control (SOC) focus on finding CVs, which are held at constant setpoints using a feedback controller. In this paper, it is shown that better self-optimizing properties can be achieved by incorporating feedforward action using measured disturbances in the SOC policies. The resulting operational policy allows the setpoints for CVs to be varied with measured disturbances allowing for near-optimal operation in presence of disturbances and uncertainties. The effectiveness of the proposed approach is demonstrated through its application to an exothermic reactor and a forced-circulation evaporator.

Keywords: Controlled variable; Control structure design; Feedforward control; Self-optimizing control.

1 Introduction

The selection of controlled variables (CVs) from available measurements is an important step during the design of control systems for industrial processes. A number of methods for CV selection have been proposed in the past few decades. Van de Wal and de Jager [2001] provide an overview of the CV selection approaches proposed in 1980s and 1990s. Recently, Skogestad [2000] introduced the concept of self-optimizing control (SOC) for systematic selection of CVs. In this approach, CVs are selected such that

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in presence of disturbances and uncertainties, the loss incurred in implementing the operational policy by holding the selected CVs at constant setpoints is minimal, as compared to the use of an online optimizer.

The choice of CVs based on the general non-linear formulation of SOC requires solving large-dimensional non-convex optimization problems [Skogestad, 2000]. To quickly pre-screen alternatives, local methods have been proposed including the minimum singular value (MSV) rule [Skogestad and Postlethwaite, 1996] and exact local methods with worst-case [Halvorsen et al., 2003] and average loss minimization [Kariwala et al., 2008]. In comparison with the traditional approach of using a subset of available measurements as CVs, it is possible to obtain lower losses using linear combinations of available measurements as CVs [Halvorsen et al., 2003]. Recently, explicit solutions to the problem of finding locally optimal measurement combinations have been proposed [Alstad et al., 2009; Heldt, 2010; Kariwala, 2007; Kariwala et al., 2008]. The usefulness of these methods has been demonstrated through a number of case studies; see *e.g.* Rangaiah and Kariwala [2012] for an overview. Note that although the available methods can be used to evaluate the loss for the specified nonlinear combinations of measurements (*e.g.* ratios of measurements), these methods cannot find the optimal nonlinear measurement combination that minimizes loss. Jaschke and Skogestad [2012] have provided a partial solution to overcome this problem, which allows using polynomials expressed in terms of measurements as CVs, but the effect of measurement noise is ignored.

The past development in SOC has focussed on the selection of CVs, which are held at constant setpoints using feedback controller to achieve near-optimal operation. In practice, measurements of some key disturbances are often available. These disturbances can include the physical disturbances, which affect the process outputs, as well as “virtual” disturbances, which do not affect the outputs, but have an effect on economics, *e.g.* utility cost. Clearly, the loss incurred in implementing the SOC policy can be reduced by adding feedforward action based on these measured disturbances to the feedback controller. This possibility has been earlier mentioned by Alstad [2005], but no analysis was presented. Cao and Yang [2004] considered the use of measured virtual disturbances to enhance the SOC policies under the restrictive assumption that these disturbances are measured perfectly.

In this paper, we present an exact local method for SOC, which allows incorporating feedforward action in SOC policies using noisy measurements of both physical and virtual disturbances. In particular, it is shown that loss can be reduced by including the measured disturbances in the available measurement set (typically consisting of outputs and inputs) and finding locally optimal measurement combinations of the extended measurement set. The resulting control system can be viewed as one, where the feedback controller holds the CVs at setpoints, which vary with the disturbances [Cao and Yang, 2004]. The effectiveness of the

proposed approach is demonstrated through its application to an exothermic reactor [Economou et al., 1986; Kariwala, 2007] and a forced-circulation evaporator [Kariwala et al., 2008; Newell and Lee, 1989].

The rest of the paper is organized as follows: the available local methods for SOC are briefly discussed in Section 2. The proposed approach of incorporating feedforward action into SOC policies is presented in Section 3. Case studies on the exothermic reactor and forced-circulation evaporator are given in Section 4 to illustrate the advantages of the proposed approach. Finally, Section 5 concludes the paper.

2 Local Methods for Self-Optimizing Control

Consider that the steady-state economics of the plant is characterized by the scalar objective function $J(u, d)$, where $u \in \mathbb{R}^{n_u}$ and $d \in \mathbb{R}^{n_d}$ are inputs and disturbances, respectively. Let the linearized model of the process, obtained around the nominally optimal operating point, be

$$y = G^y u + G_d^y W_d d + W_e e \quad (1)$$

where $y \in \mathbb{R}^{n_y}$ denotes the measurements of process variables (PVs) and $e \in \mathbb{R}^{n_y}$ denotes the implementation error, which results due to measurement and control errors. Here, the diagonal matrices W_d and W_e contain the expected magnitudes of disturbances and implementation error, respectively. The CVs $c \in \mathbb{R}^{n_u}$ are given as

$$c = H y = G u + G_d W_d d + H W_e e \quad (2)$$

where H is a selection or combination matrix and

$$G = H G^y, \quad G_d = H G_d^y \quad (3)$$

It is assumed that $G \in \mathbb{R}^{n_u \times n_u}$ is invertible. This assumption is necessary for integral control. When d and e are assumed to be uniformly distributed over the set

$$\left\| \begin{bmatrix} d' & e' \end{bmatrix} \right\|_2 \leq 1 \quad (4)$$

where “ $'$ ” represent the transpose of a matrix, the local worst-case and average losses are given as [Halvorsen et al., 2003; Kariwala et al., 2008]:

$$L_{\text{worst}}(H) = 0.5 \bar{\sigma}^2 \left(J_{uu}^{1/2} (H G^y)^{-1} H Y \right) \quad (5)$$

$$L_{\text{average}}(H) = \frac{1}{6(n_y + n_d)} \left\| J_{uu}^{1/2} (H G^y)^{-1} H Y \right\|_F^2 \quad (6)$$

where n_y and n_d represent the number of PVs and disturbances, respectively, $\bar{\sigma}$ and $\|\cdot\|_F$ denote the maximum singular value and Frobenius norm, respectively, and

$$Y = [(G^y J_{uu}^{-1} J_{ud} - G_d^y) W_d \quad W_e] \quad (7)$$

with $J_{uu} = \frac{\partial^2 J}{\partial u^2}$ and $J_{ud} = \frac{\partial^2 J}{\partial u \partial d}$, evaluated at the nominal operating point. In comparison with worst-case loss, the selection of CVs is preferred through minimization of average loss, as the worst-case may not occur frequently in practice [Kariwala et al., 2008].

When individual measurements are selected as CVs, H can be considered to be a selection matrix. The selection of n_u CVs from n_y measurements is a combinatorial optimization problem. Bidirectional branch and bound (BAB) methods have been proposed in [Kariwala and Cao, 2009, 2010] to solve this problem efficiently.

Instead of using individual measurements, it is possible to use combinations of measurements as CVs. For this case, Alstad et al. [2009] has recently proposed an explicit expression for H , which minimizes the L_{average} in (6) and is given as

$$H' = (YY')^{-1} G^y ((G^y)' (YY')^{-1} G^y)^{-1} J_{uu}^{1/2} \quad (8)$$

As shown by Kariwala et al. [2008], the H in (8) also minimizes L_{worst} in (5). The locally optimal combinations of all the available measurements, which can be used as CVs can be found using (8). It is, however, noted in [Alstad et al., 2009; Kariwala, 2007; Kariwala et al., 2008] that the use of combinations of a few measurements as CVs often provide similar loss as the case where combinations of all available measurements are used. Partially bidirectional BAB methods have been proposed for efficient selection of measurements, whose combinations can be used as CVs, in [Kariwala and Cao, 2009, 2010].

Remark 1: For the given locally optimal combination matrix H , any combination matrix obtained as QH , where Q is a non-singular matrix, is also locally optimal [Halvorsen et al., 2003]. Thus, by selecting $Q = ((G^y)' (YY')^{-1} G^y) J_{uu}^{-1/2}$, a simplified expression for locally optimal H can be derived as [Rangaiah and Kariwala, 2012]

$$H' = (YY')^{-1} G^y \quad (9)$$

To find Y in (7), one needs to evaluate $(G^y J_{uu}^{-1} J_{ud} - G_d^y)$, which represents the sensitivity of the optimal values of y with respect to d and can be obtained by repeatedly solving the non-linear optimization problem with perturbations in d [Alstad et al., 2009]. Then, (9) shows that to find locally optimal H , the knowledge of J_{uu} is not necessary, which can be difficult numerically, especially if the process is modelled using a

commercial simulator; see *e.g.* [Yelchuru and Skogestad, 2012]. However, J_{uu} is still required to evaluate loss, *e.g.* during the application of BAB methods for measurement subset selection.

3 Incorporation of disturbance measurements into SOC

To incorporate feedforward action into SOC policies, we partition d into d_m (measured disturbances) and d_u (unmeasured disturbances). The disturbance gain matrix is conformably partitioned as

$$G_d^y = \begin{bmatrix} G_{d_m}^y & G_{d_u}^y \end{bmatrix} \quad (10)$$

The measured value of d_m is denoted as \hat{d}_m . It is considered that the elements of the diagonal matrix W_{e_d} contain the error associated with measurement of d_m . Let us define the extended measurement set as

$$\tilde{y} = \begin{bmatrix} y' & \hat{d}_m' \end{bmatrix}' \quad (11)$$

It follows that

$$\tilde{y} = G^{\tilde{y}} u + G_d^{\tilde{y}} W_d d + W_{\tilde{e}} \tilde{e} \quad (12)$$

where

$$G^{\tilde{y}} = \begin{bmatrix} G^y \\ 0 \end{bmatrix} \quad (13)$$

$$G_d^{\tilde{y}} = \begin{bmatrix} G_{d_m}^y & G_{d_u}^y \\ I & 0 \end{bmatrix} \quad (14)$$

$$W_{\tilde{e}} = \begin{bmatrix} W_e & 0 \\ 0 & W_{e_d} \end{bmatrix} \quad (15)$$

$$\tilde{e} = \begin{bmatrix} e' & e_{e_d}' \end{bmatrix}' \quad (16)$$

with e_{e_d} satisfying $W_{e_d} e_{e_d} = \hat{d}_m - d_m$.

Based on the extended set of measurements, the CVs can be selected as

$$\tilde{c} = \tilde{H} \tilde{y} = H_y y + \textcolor{red}{H}_{d_m} \hat{d}_m \quad (17)$$

Similar to (8), the optimal H can be obtained using the following expression

$$\tilde{H}' = (\tilde{Y} \tilde{Y}')^{-1} G^{\tilde{y}} ((G^{\tilde{y}})' (\tilde{Y} \tilde{Y}')^{-1} G^{\tilde{y}})^{-1} J_{uu}^{1/2} \quad (18)$$

where

$$\tilde{Y} = \begin{bmatrix} (G^{\tilde{y}} J_{uu}^{-1} J_{ud} - G_d^{\tilde{y}}) W_d & W_{\tilde{e}} \end{bmatrix} \quad (19)$$

$$= \begin{bmatrix} (G^y J_{uu}^{-1} J_{ud} - G_d^y) W_d & W_e & 0 \\ -W_{d_m} & 0 & W_{e_d} \end{bmatrix} \quad (20)$$

Here, the diagonal matrix W_{d_m} contains the magnitude of d_m . In the proposed approach, u is manipulated such that $\tilde{c} = \tilde{H}\tilde{y} = H_y y + \textcolor{red}{H}_{d_m} \hat{d}_m = 0$ or

$$H_y y = -\textcolor{red}{H}_{d_m} \hat{d}_m \quad (21)$$

Interpreting $H_y y$ as the CV for feedback control and $-\textcolor{red}{H}_{d_m} \hat{d}_m$ as its setpoint, the proposed operational policy is viewed as traditional SOC approach with varying setpoint. Note that in comparison with feedback only, the loss seen using the feedforward action cannot be higher, as in the worst-case $\textcolor{red}{H}_{d_m}$ can always be selected to be zero and H_y as H in (8).

4 Results and Discussion

In this section, we demonstrate the advantages of incorporating feedforward action into SOC policies using benchmark examples.

4.1 Exothermic Reactor

We first consider the example of an exothermic reactor [Economou et al., 1986] to illustrate the benefit of incorporating measured physical disturbances into the measurement set. For this process, the inlet to the well-mixed reactor consists of reactant A and product B as contaminant at temperature T_i . The outlet stream has a temperature T with the concentrations of the product B and the unused reactant A being C_B and C_A , respectively. The schematic of the exothermic reactor is shown in Figure 1. The economic objective function to be minimized is

$$J = -2.009 C_B + (0.001657 T_i)^2 \quad (22)$$

This process has three outputs (C_A , C_B , and T), one input (T_i), and two disturbances (C_{Ai} and C_{Bi}). The nominal values of disturbances are $C_{Ai} = 1$ mol/L and $C_{Bi} = 0$. The measurement set is given as

$$y = [C_A \quad C_B \quad T \quad T_i]^\top \quad (23)$$

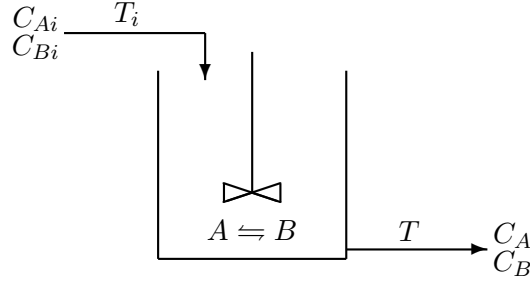


Figure 1: Schematic of Exothermic reactor

The allowable ranges for disturbances are $0.7 \leq C_{Ai} \leq 1.3$ and $0 \leq C_{Bi} \leq 0.3$, which implies that $W_d = \text{diag}(0.3, 0.3)$. The implementation errors are taken as 0.01 mol/L for concentration measurements and 0.5 K for temperature measurement. Thus, $W_e = \text{diag}(0.01, 0.01, 0.5, 0.5)$. The gain and Hessian matrices obtained around the nominally optimal operating point are available in [Kariwala, 2007]. Let us define the extended measurement as $\tilde{y} = [y' \ d_m']'$. We consider four different cases, where $d_m = \emptyset$, $d_m = C_{Ai}$, $d_m = C_{Bi}$, and $d_m = [C_{Ai} \ C_{Bi}]'$. Measurement errors for both disturbances C_{Ai} and C_{Bi} are taken as 0.01 mol/L.

The locally optimal measurement combination matrices for different measurement sets are computed using (18). The resulting losses for each CV candidate obtained using the local method and the nonlinear model are shown in Table 1. For nonlinear analysis, 100 scenarios are considered, where d and e are generated randomly to have zero mean and uniform distribution over the range -1 to 1. In general, the nonlinear analysis shows good agreement with the local analysis, except that the worst-case loss seen with $d_m = [C_{Ai} \ C_{Bi}]'$ is higher than the case with $d_m = C_{Bi}$ for nonlinear analysis. This is due to the fact that the combination matrix \tilde{H} obtained using (18) is only locally optimal. It can be noted that as compared to the use of feedback-based SOC policy, the inclusion of C_{Ai} and C_{Bi} individually reduces the average loss computed using nonlinear model by approximately 51%, while inclusion of both disturbances results in 55% reduction.

Table 1: Local and nonlinear losses for exothermic reactor

d_m	Local Analysis		Nonlinear Analysis	
	$L_{average}$ [\$/min]	L_{worst} [\$/min]	Average loss [\$/min]	Worst-case loss [\$/min]
\emptyset	1.465×10^{-5}	2.637×10^{-4}	2.567×10^{-4}	2.372×10^{-3}
C_{Ai}	2.809×10^{-6}	5.899×10^{-5}	1.256×10^{-4}	9.468×10^{-4}
C_{Bi}	1.856×10^{-6}	3.898×10^{-5}	1.254×10^{-4}	6.699×10^{-4}
C_{Ai}, C_{Bi}	1.182×10^{-6}	2.837×10^{-5}	1.166×10^{-4}	9.304×10^{-4}

Table 1 shows that the measurement set with $d_m = C_{Bi}$ provides similar loss as seen with both disturbances measured. As combining fewer measurements is desirable to obtain a simpler control structure, we recommend the use of C_{Bi} as measured disturbance to incorporate feedforward action for this exothermic reactor. The selected CV is given as

$$\tilde{c} = 0.295 C_A - 0.028 C_B - 0.007 T - 0.008 T_i - 0.642 C_{Bi} \quad (24)$$

for which the relative average loss evaluated based on the nonlinear model is approximately 0.02% showing that the selected CV achieves nearly perfect self-optimizing properties.

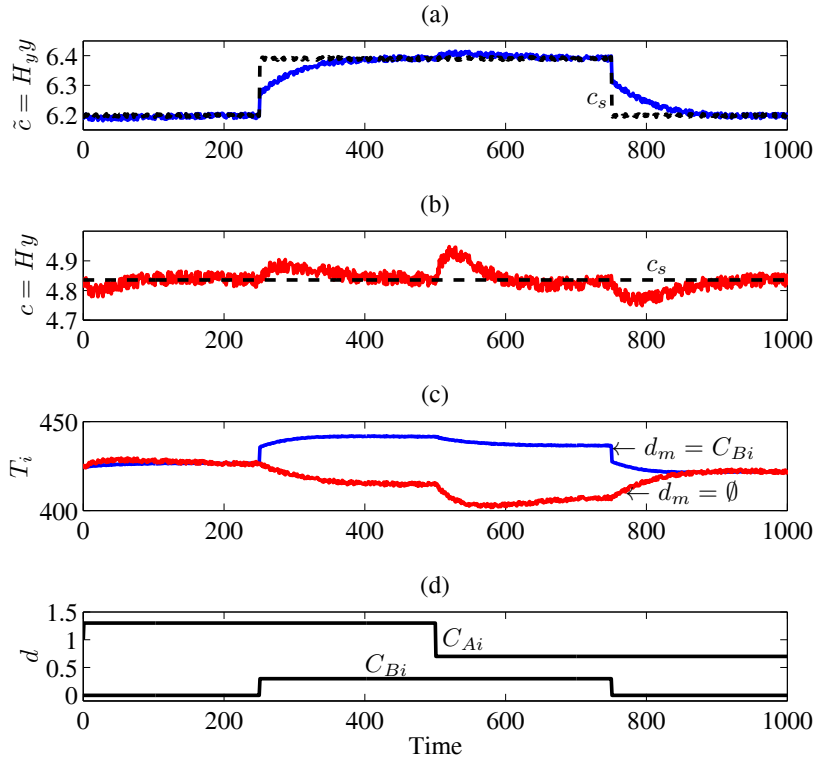


Figure 2: Comparison of dynamic responses for exothermic reactor: (a) CV ($\tilde{c} = H_y y$) for $d_m = C_{Bi}$; (b) CV ($c = H y$) for $d_m = \emptyset$; (c) input (T_i); and (d) disturbances (d)

We point out that the proposed approach of selecting CVs as combinations of measurements does not take dynamic performance into account and the selected CVs can have poor controllability in general. To verify the dynamic performance, the following linear model, obtained around nominal optimal point, is derived:

$$\frac{\tilde{c}(s)}{T_i(s)} = \frac{0.0159(30.964s + 1)(13.627s + 1)}{(60s + 1)(13.353s + 1)} \quad (25)$$

A first order approximation of the model is obtained using half-rule and the internal model control (IMC) method [Skogestad, 2003] with desired closed-loop time constant $\tau_c = 12$ min (one-fifth of dominant open-loop time constant) is used to design a proportional-integral (PI) controller with proportional gain $K_c = 77.517$ and integral time $\tau_I = 29.036$ min. For comparison purposes, this procedure is repeated for the case $d_m = \emptyset$. In this case, the linear model between T_i and CV $c = -1.675 C_A + 1.425 C_B + 0.0003 T + 0.011 T_i$, obtained around nominal optimal point, is:

$$\frac{c(s)}{T_i(s)} = \frac{0.0153(40.142s + 1)(14.492s + 1)}{(60s + 1)(13.353s + 1)} \quad (26)$$

As before, using half-rule and IMC method [Skogestad, 2003], a PI controller with proportional gain $K_c = 48.495$ and integral time $\tau_I = 19.858$ min is designed. The closed-loop responses for multiple step changes in disturbances C_{Ai} (from 1 to 1.3 mol/L at $t = 1$ min and from 1.3 to 0.7 mol/L at $t = 501$ min) and C_{Bi} (from 0 to 0.3 mol/L at $t = 251$ min and from 0.3 to 0 mol/L at $t = 751$ min) are shown in Figure 2. In these simulations, the measurement errors are considered to be uniformly distributed random sequences with magnitudes $\pm \sum_{i=1}^{n_y} |H_y W_e|$, $\pm \sum_{i=1}^{n_y} |H W_e|$ and $\pm \sum_{i=1}^{n_d} |H_{d_m} W_{e_d}|$ for \tilde{c} , c and \hat{d}_m , respectively. It can be seen that \tilde{c} follows its setpoint c_s , updated based on measurements of C_{Bi} , closely with smooth changes in T_i . The average cost (J) for $d_m = \emptyset$ is 0.414 [\$/min], which reduces to 0.395 [\$/min] for $d_m = C_{Bi}$.

Overall, this case study clearly demonstrates that the proposed method can provide considerably lower loss in comparison with traditional feedback-based SOC policy. We point out that the benefits of incorporating feedforward action in SOC policies strongly depends on the accuracy of disturbance measurement. For example, in comparison with feedback-based SOC policy ($d_m = \emptyset$), the use of \tilde{c} as CV reduces the average loss computed using nonlinear model by only 8 %, if the measurement error of C_{Bi} is 0.1 mol/L.

4.2 Forced-Circulation Evaporator

Next, we consider the case of forced-circulation evaporator [Cao, 2005; Kariwala et al., 2008; Newell and Lee, 1989]. The primary objective of this case study is to illustrate the use of price variation as measured disturbance in SOC. The schematic representation for this process is shown in Figure 3 and the variables are listed in Table 2. The operational objective of this process involves minimizing

$$J = \alpha F_{100} + 0.6 F_{200} + 1.009 (F_2 + F_3) + 0.2 F_1 - 4800 F_2 \quad (27)$$

which denotes negative profit. In (27), α denotes the price of steam (virtual disturbance). This process has a number of operational constraints on X_2 , P_2 , P_{100} , F_{200} , F_1 , and F_3 ; see Kariwala et al. [2008] for

details.

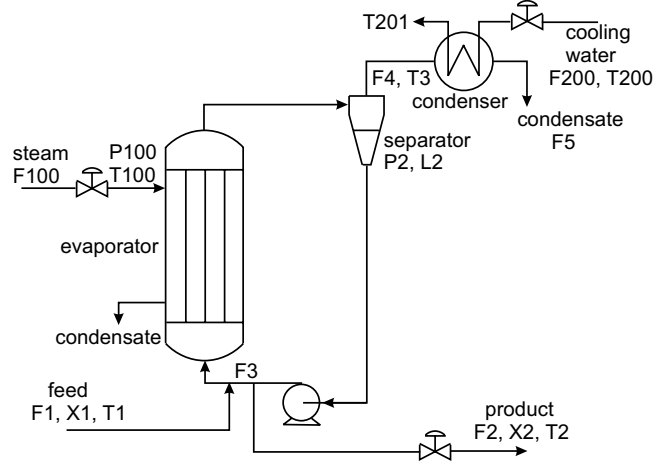


Figure 3: Schematic representation of the Forced Circulation Evaporator

Table 2: Variables of Forced Circulation Evaporator

Var.	Description	Var.	Description
F_1	Feed flowrate	T_3	Vapor temperature
F_2	Product flowrate	L_2	Separator level
F_3	Circulating flowrate	P_2	Operating pressure
F_4	Vapor flowrate	F_{100}	Steam flowrate
F_5	Condensate flowrate	T_{100}	Steam temperature
X_1	Feed composition	P_{100}	Steam pressure
X_2	Product composition	F_{200}	Cooling water flowrate
T_1	Feed temperature	T_{200}	Inlet temperature of cooling water
T_2	Product temperature	T_{201}	Outlet temperature of cooling water

This process has 5 manipulated inputs (F_1 , F_2 , P_{100} , F_3 , and F_{200}) and 3 disturbances (X_1 , T_1 and T_{200}). The case, where $X_1 = 5\%$, $T_1 = 40^\circ C$, $T_{200} = 25^\circ C$ and $\alpha = 600$, is taken as the nominal operating point. At these conditions, the optimum negative profit of the process is -582.233 [\$/h]. It is noted that the constraints on X_2 and P_{100} remain active over the entire set of allowable disturbances. In addition, the separator level (L_2) needs to be controlled, which has no steady-state effect. Amongst these 5 manipulated inputs, P_{100} is kept at its upper limit, F_2 is used to control X_2 at the lower bound and F_3 is adopted to maintain the level, L_2 at its setpoint. Thus, two inputs are available as unconstrained degrees of freedom, for which CVs need to be selected. Without loss of generality, they are taken as F_1 and F_{200} .

The measurement set is given as

$$y = [P_2 \ T_2 \ T_3 \ F_2 \ F_{100} \ T_{201} \ F_5 \ F_{200} \ F_1]' \quad (28)$$

Note that in comparison with earlier studies [Kariwala et al., 2008], F_3 is not included in y , as the linear model for this measurement results in large plant-model mismatch due to linearization [Kariwala et al., 2008]. The gain and Hessian matrices for this process are available in [Kariwala et al., 2008]. In addition, for α

$$J_{u\alpha} = \begin{bmatrix} -0.001 & 1.115 \end{bmatrix}' \quad (29)$$

The allowable disturbance set corresponds to $\pm 5\%$ variation in X_1 , $\pm 20\%$ variation in T_1 and T_{200} and $\pm 10\%$ in α around their nominal values. Based on these variations, we have $W_d = \text{diag}(0.25, 8, 5, 60)$. The implementation errors for the pressure and flow measurements are taken to be $\pm 2.5\%$ and $\pm 2\%$, respectively, of the nominal operating values. For temperature measurements, implementation error is considered to be $\pm 1^\circ\text{C}$. Therefore, we have $W_e = \text{diag}(1.285, 1, 1, 0.027, 0.189, 1, 0.163, 4.355, 0.189)$. It is considered that the price α is measured with an accuracy of 0.5% of its nominal value, which implies $W_{\tilde{e}} = \text{diag}(W_e, 3)$.

Analysis. Let us define c_9 and \tilde{c}_{10} as the CV candidates consisting of combination of all the measurements in y and the extended measurement set $\tilde{y}' = \begin{bmatrix} y' & \alpha \end{bmatrix}$, respectively. The local average losses incurred with the use of c_9 and \tilde{c}_{10} as CVs are 4.306 \$/h and 0.224 \$/h, respectively. Similarly, the **local worst-case loss**, when c_9 and \tilde{c}_{10} are used as CVs, are 167.866 \$/h and 9.325 \$/h, respectively. This analysis shows that varying the setpoints based on α can significantly reduce the loss.

To obtain simpler control structure, combinations of fewer measurements, which can be used as CVs, are identified using BAB method with local average loss minimization [Kariwala and Cao, 2010]. The BAB method is applied by considering y (**without including α in the measurement subset**) and \tilde{y} (**with inclusion of α in the measurement subset**) as the measurement set. For both cases, the variations of least local average losses with the measurement subset size, n_y are shown in Figure 4. As α itself, *i.e.* without other measurements, cannot be used as a CV, combinations of at least 3 measurements need to be selected as CVs, **when α is included in the measurement subset**. Figure 4 shows that including α in the measurement set reduces the loss by factors of 2-20 for different n_y .

It can be observed from Figure 4 that **when α is included in the measurement subset**, the use of combinations of 4 or 5 measurements as CVs yields similar local average loss (0.505 and 0.383 \$/h, respectively) as seen for \tilde{c}_{10} (0.224 \$/h). These CV candidates offer a good trade off between simpler control structure

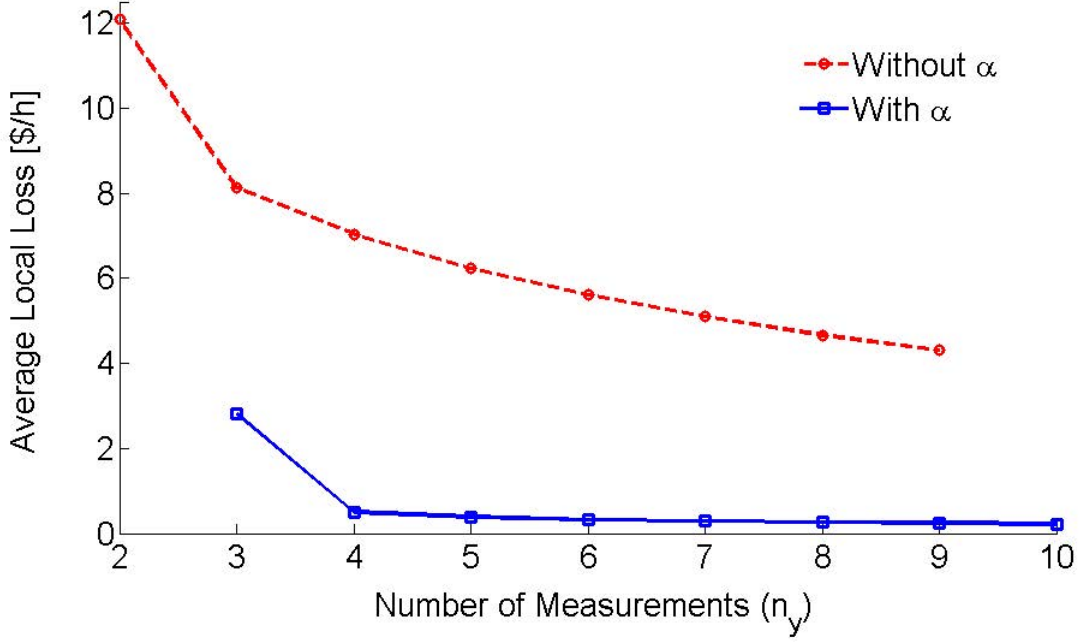


Figure 4: Local average loss for best measurement set with size n_y

and economic loss, and are given as:

$$\tilde{c}_4 = \begin{bmatrix} 0.99897 F_2 + 0.027167 F_{100} - 0.035538 F_{200} + 0.0071889 \alpha \\ 0.027401 F_2 - 0.9996 F_{100} + 0.0064695 F_{200} + 0.0018819 \alpha \end{bmatrix} \quad (30)$$

$$\tilde{c}_5 = \begin{bmatrix} 0.9991 F_2 - 0.022095 F_{100} + 0.000894 F_5 - 0.03539 F_{200} + 0.0073234 \alpha \\ -0.021832 F_2 - 0.99973 F_{100} + 0.00027481 F_5 + 0.0081462 F_{200} + 0.0015411 \alpha \end{bmatrix} \quad (31)$$

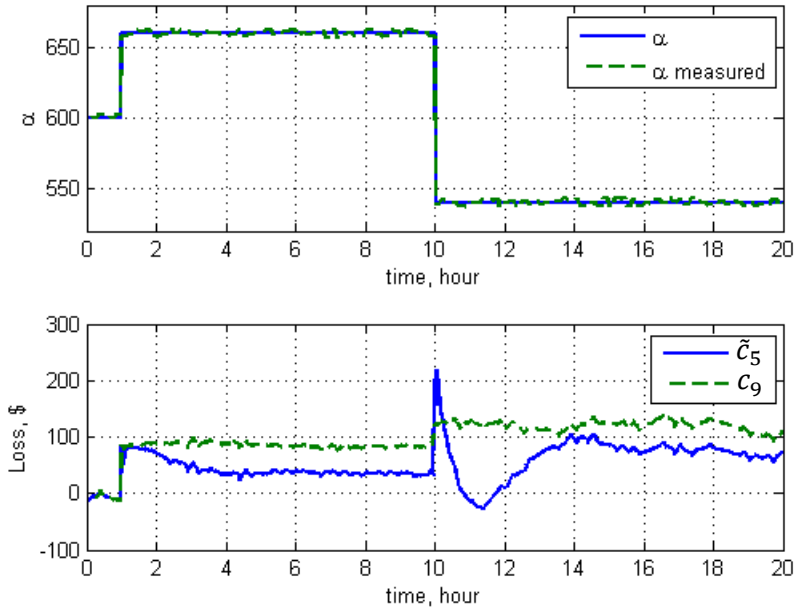
Similar to the CSTR case study, nonlinear analysis is conducted to verify the results of local analysis. The resulting average and worst-case losses for the promising candidates are presented in Table 3. We note that using \tilde{c}_4 and \tilde{c}_5 as CVs provides lower losses than the use of \tilde{c}_{10} as CVs. This observation highlights the local optimality of \tilde{H} and approaches to overcome this limitation will be pursued in future. In comparison with c_9 , the use of \tilde{c}_5 as CV reduces the average and worst-case losses obtained using nonlinear model by factors of 18 and 8, respectively. **Furthermore, the relative average loss evaluated based on the nonlinear model is approximately 0.3% with the use of \tilde{c}_5 as CV.**

The performance of the proposed method is further evaluated through dynamic simulations using c_9 and \tilde{c}_5 as CVs, respectively. For both cases, the first component of CVs (CV1) is cascaded with a pressure controller through F_{200} to maintain P_2 within its upper and lower constraints, as described in [Cao, 2005],

Table 3: Local and nonlinear analysis for promising CV alternatives for forced-circulation evaporator

CV	Measurements	Local Analysis		Nonlinear Analysis	
		$L_{average}$ [\$ /h]	L_{worst} [\$ /h]	Average loss [\$ /h]	Worst-case loss [\$ /h]
c_9	y	4.306	167.866	36.229	180.925
\tilde{c}_4	$F_2, F_{100}, F_{200}, \alpha$	0.505	12.032	2.267	27.349
\tilde{c}_5	$F_2, F_{100}, F_{200}, F_5, \alpha$	0.383	10.275	2.159	24.427
\tilde{c}_{10}	$\tilde{y} = \begin{bmatrix} y' & \alpha \end{bmatrix}'$	0.224	9.325	2.399	36.885

whilst the second component of CVs (CV2) is paired with the manipulated variable, F_1 . All controller parameters, except those used in the CV2- F_1 loop, are the same as those reported in [Cao, 2005]. For the CV2- F_1 loop, a simple PI controller is designed with a unit control gain and unit integral time (1 min). All measurements are assumed to have uniformly distributed measurement noises within the variation ranges specified by $W_{\tilde{e}}$. For simplicity, the process is considered to be operated at the nominally optimal point initially. The following step changes are introduced in α : \$600 to \$660 at $t = 1$ hours and \$660 to \$540 at $t = 10$ hours, which lasts until $t = 20$ hours, as shown in Figure 5 (a). The profit losses comparing to the true optimal operation resulted due to the use of \tilde{c}_5 or c_9 as CVs are shown in 5 (b). The corresponding transient responses of key process variables are shown in Figure 6.


 Figure 5: (a) Step changes of α (b) Hourly profit loss comparing to true optimal operation

It can be seen that for the first hour when steam price, α is at nominal value, both \tilde{c}_5 and c_9 result

in almost the same zero loss. However, when α increases or decreases from the nominal value, without feedforward action, c_9 does not change the operational conditions, as indicated by dashed lines in Figure 6, resulting in a higher profit loss compared to that obtained by using \tilde{c}_5 as CV, for which feedforward action is incorporated to adjust operation conditions accordingly, as indicated by the solid lines in Figure 6.

From Figure 6, it can be seen that when the steam price increases, the CV with feedforward action, \tilde{c}_5 reduces F_1 , F_2 , F_3 and P_2 , which requires F_{200} to increase, such that the plant operates at a low production mode to keep the operation profitable, whilst, when the steam price decreases, \tilde{c}_5 is able to adjust process variables so as the plant operates in a high production mode to take the advantage fully. In contrast, the CV without feedforward action, c_9 cannot detect the steam price changes. Hence, the plant operates continuously in the nominal condition independent from the steam price resulting in high losses.

The total profit for 20 hours of operation is \$13160.95 and \$12232.23, when \tilde{c}_5 and c_9 are used as CVs, respectively. Based on these results, the use of \tilde{c}_5 as CV is recommended for the forced-circulation evaporator.

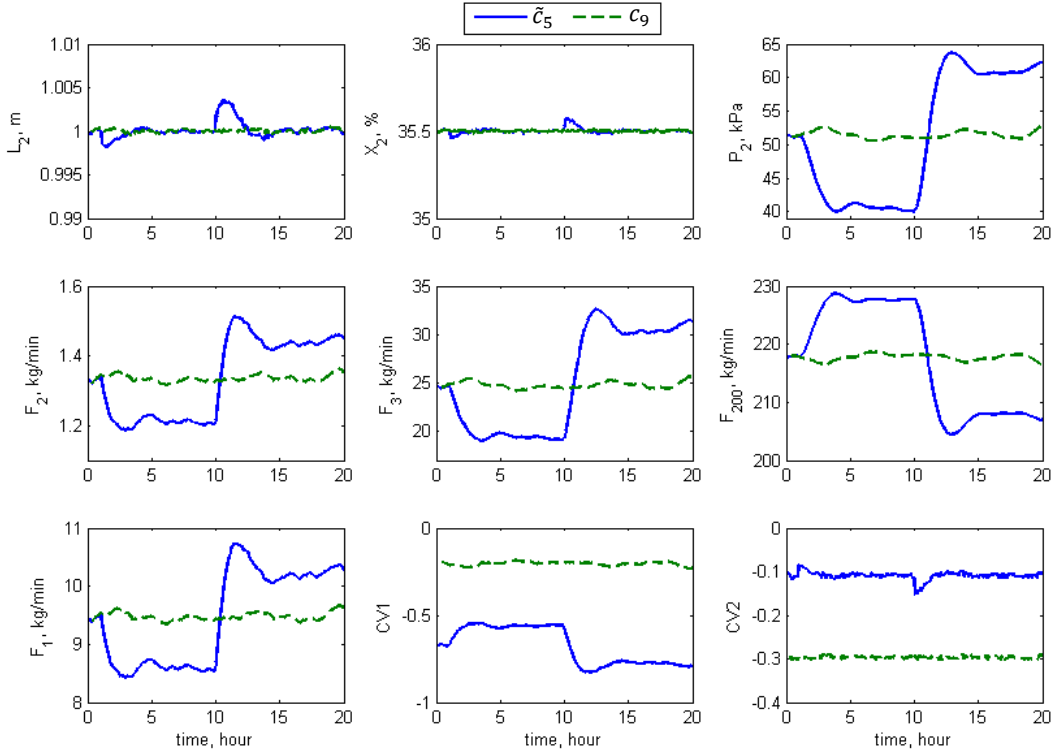


Figure 6: Transient response of major process variables using c_5 as CVs.

5 Conclusions

We proposed an approach to improve the feedback-based self optimizing control (SOC) by including information of key disturbances into measurement set, whose combinations are used as CVs. The incorporation of the feedforward action is useful to anticipate the effect of measured disturbances and thus lower economic loss is obtained in comparison with the use of CVs synthesized with the feedback-based SOC policies. This work provides broader scope in comparison with the work of Cao and Yang [2004] by extending the notion of measured disturbances to include the physical/process disturbances in addition to the “virtual” disturbances, which only affect the scalar objective function related to optimal operation of process. Case studies of CSTR and forced-circulation evaporator show that incorporation of key disturbance information in SOC policies results in significant reduction of loss. It is pointed out that this reduction in loss requires additional sensors for measuring disturbances and thus selection of dominant disturbances, as done for CSTR case study, is important to minimize the additional cost of instrumentation. Furthermore, unlike individual measurements, measurement combinations lack physical interpretation, which can sometimes limit their adoption as CVs. To overcome this issue, Heldt [2010] and Yelchuru and Skogestad [2012] have suggested imposing structure on H such that only physically similar measurements, *e.g.* temperature or flow measurements, are combined as CVs, which can be used for incorporating feedforward action in SOC policies as well. Lastly, the available methods for selection of self-optimizing CVs are based on steady-state economics and the selected CVs may suffer from poor dynamic controllability. A possible approach to overcome this drawback is to select CVs based on dynamic models. Some progress to handle process dynamics has been reported in [Dahl-Olsen et al., 2008; Hu et al., 2012], which can form the basis for future research.

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