

# Power Control Optimization for Large-Scale Multi-Antenna Systems

Haijun Yu<sup>†</sup>, Zhenyu Zhou<sup>†</sup>, Shahid Mumtaz<sup>‡</sup>, Saba Al-Rubaye\*, Antonios Tsourdos\*,  
and Rose Qingyang Hu<sup>§</sup>

<sup>†</sup>*North China Electric Power University, China*

<sup>‡</sup>*Instituto de Telecomunicações, Portugal*

<sup>\*</sup>*School of Aerospace, Transport and Manufacturing, Cranfield University, UK*

<sup>§</sup>*Electrical and Computer Engineering, Utah State University, USA*

## Abstract

Large-scale multi-antenna systems can effectively improve data transmission reliability and throughput for smart grid. However, the massive number of antennas and radio frequency (RF) chains also result in high complexity and energy cost. In this paper, we develop a new performance benchmark named energy economic efficiency for measuring the time-average throughput per energy cost. Then, we investigate how to maximize long-term energy economic efficiency via the joint optimization of communication and energy resource allocation. The formulated joint optimization problem is NP-hard because it not only involves long-term nonlinear optimization objective and constraints, but also involves both integer and continuous optimization variables. Next, we propose an online joint antenna selection and power control algorithm by combining nonlinear fractional programming, Lyapunov optimization, and bisection method. The proposed algorithm can achieve bounded performance deviation from the optimum performance without requiring the prior knowledge of future channel state information (CSI), energy arrival, and electricity price. Finally, a comprehensive theoretical analysis is provided, and the proposed algorithm is verified through simulations under various system configurations.

## Index Terms

Large-scale multi-antenna systems, Lyapunov optimization, smart grid, energy economic efficiency, bisection method, nonlinear fractional programming.

## I. INTRODUCTION

Smart grid relies on advanced communication technologies for improving efficiency, reliability, and economics of traditional power grid. To achieve intelligent management of energy generation,

transmission, transformation, delivery, and storage, huge volume of data have to be transmitted on a real-time basis. With the development of 5G cellular technologies, large-scale multi-antenna systems with hundreds of antennas have appeared as a promising solution. It can effectively improve data transmission reliability and throughput for smart grid via the exploitation of antenna gain [1]–[3]. The basic principles of large-scale multi-antenna systems were investigated [4], and real-world testbeds were developed [5], [6]. Despite its huge benefits, the massive number of antennas and RF chains also raises new challenges such as high complexity and power consumption. For each antenna, a separate radio frequency (RF) chain is required for signal processing, which is generally more expensive and energy consuming than the antenna itself [7], [8]. The overall energy costs can no longer be neglected as in existing cellular systems.

The costs of energy consumption can be reduced from both the energy and communication domains [9]. In the energy domain, a possible solution is to exploit external renewable energy sources such as wind and solar energy. Smart grid enables seamless integration of renewable energy sources into the demand side, thereby reducing the amount of grid power consumption. In the communication domain, the active number of antennas and respective RF chains can also be reduced through antenna selection. Previous experiment results have demonstrated that the contributions of different antennas are not equal in real-world communication channels [5]. Therefore, instead of using all antennas, it is beneficial to only select those antennas which contribute the most while turning off the rest.

However, the research on large-scale multi-antenna systems for smart grid is still in its infancy. There exist several key challenges that remain unsolved. First of all, energy resource allocation and communication resource allocation are intertwined with each other and should be jointly optimized. The formulated joint resource allocation problem is NP-hard due to the coupling between energy and communication domains. Second, renewable energy sources with intermittent and fluctuating characteristics and capacity-constrained energy storage devices cannot provide reliable quality of service (QoS) guarantees. A more feasible approach is to utilize both unreliable renewable energy sources and reliable grid power in a complementary manner [10]. The coexistence of various energy sources further complicates the resource allocation problem. Last but not least, the long-term system performance depends on the precise knowledge of future electricity price, energy arrival and channel state information (CSI), which is generally unavailable. In real-world implementation, even the accurate statistical information is difficult to be identified.

To address these challenges, we propose an online joint resource allocation algorithm by combining nonlinear fractional programming, bisection method, and Lyapunov optimization. Its main goal is to maximize the long-term energy economic efficiency via the joint optimization of communication resource allocation, i.e., antenna selection, and energy resource allocation, i.e., power control. First, we formulate the energy economic efficiency maximization problem as a joint antenna selection and power control problem over an infinite horizon, which cannot be solved in polynomial time. Both long-term and short-term constraints are taken into account. Second, the formulated problem in fractional form is transformed into an equivalent subtractive-form problem based on nonlinear fractional programming. Then, the long-term stochastic optimization problem is further converted to a short-term deterministic optimization problem by leveraging Lyapunov optimization. Third, by opportunistically minimizing the upper bound of drift-minus-reward, the antenna selection and power control subproblems are separated and solved sequentially. The main contributions of this work are summarized as follows:

- *Energy economic efficiency maximization:* We consider a new performance metric named energy economic efficiency, which provides a benchmark for measuring the time-average throughput per unit energy cost. Compared to other metrics such as energy efficiency, it is more suitable for the smart grid environment with various energy sources and electricity prices. Particularly, energy efficiency can be abstracted as a special case of this new metric.
- *Long-term online optimization with bounded performance deviation:* The proposed algorithm is aware of long-term optimization objective and constraints. It can guarantee bounded deviation from the optimum performance without requiring any prior knowledge of future CSI, energy arrival, and electricity prices.
- *Comprehensive theoretical analysis and performance validation:* We provide a comprehensive theoretical analysis for the proposed algorithm in terms of reliability, optimality, and complexity. Intensive simulation results are conducted under different scenarios to demonstrate its performance gains.

The rest of the paper is outlined as follows. A survey of related works is presented in Section II. Section III introduces the system model in details. The problem formulation is provided in Section IV. Section V elaborates the proposed online resource allocation algorithm. A comprehensive property analysis is provided in Section VI. Numerical results and analysis are introduced in Section VII. Finally, the conclusion is summarized in Section VIII.

## II. RELATED WORK

When implementing large-scale multi-antenna system for the smart grid, both the communication resource allocation and energy resource allocation should be jointly optimized according to dynamic CSI, energy arrival, and electricity prices. The key research challenge is that these uncertain factors may cause a high level of volatility and increase potential performance disturbances.

For the optimization of communication resources, antenna selection techniques for conventional multi-antenna systems are summarized in [7], and were then extended to co-located large-scale multi-antenna systems [5], [11], [12], as well as distributed antenna systems (DAS) [13], [14]. In [11], Li *et al.* proposed a bisection-based antenna selection algorithm to maximize the energy efficiency for the large-scale multi-antenna systems. In [5], Gao *et al.* evaluated antenna selection performance for large-scale multi-antenna systems with 128 elements and proposed a close-to-optimal antenna selection algorithm based on measurements of the received power. Amadori *et al.* developed an antenna selection algorithm to maximize the received power by identifying antennas with higher constructive interference [12]. Nevertheless, these attempts are only valid for scenarios with constant energy supply, and have not considered the smart grid scenarios with dynamic energy arrival and electricity prices.

For the optimization of energy resources, power control in renewable energy based communication systems was originally developed for nonfading channels [15], and was then extended to broadcasting channels [16], multiple-hop relay channels [17], [18], fading channels [19], and multiple input multiple output (MIMO) channels [20]. However, most of these attempts only target the power control problem in systems with a limited number of antennas. The specific characteristics of large-scale multi-antenna systems are largely neglected, and antenna selection is not jointly optimized with power control.

Markov decision process (MDP) provides an effective approach to handle uncertainties, in which the uncertain parameters are assumed to follow a well-known probability distribution [21]–[24]. In [21], Stephen *et al.* modeled the joint optimization problem of pilot allocation and antenna selection as a partially observed MDP, and developed a joint resource allocation algorithm to maximize the expected throughput. The drawback is that the performance degrades dramatically if the practical probability distributions of uncertain factors are different from the presumed statistical models. In addition, the computation complexity of MDP is enormously high because

of the well-known “curse of dimensionality” [25]. Although the algorithmic structures of low-complexity sub-optimal solutions were developed [15]–[17], [20], the knowledge of statistical information is required as a priori.

An alternative low-complexity sub-optimal solution for addressing long-term stochastic optimization problems is Lyapunov optimization [26]. It allows a distribution-free model of uncertain factors and provides bounded performance guarantees under all possible realizations of uncertainties. Some researchers have already applied it for resource allocation optimization in large-scale multi-antenna systems. In [27], Jiang *et al.* studied the joint user scheduling and beam selection problem in large-scale multi-antenna systems, and proposed an online sum-rate maximization algorithm based on Lyapunov optimization. The same authors extended their work to the scenario where statistical CSI is available [26]. Nevertheless, these works are not suitable for the smart grid environment with dynamic energy arrival and electricity prices. In [28], Mao *et al.* considered the intermittent characteristics of renewable energy sources and proposed a Lyapunov optimization-based base station (BS) assignment and power control (BAPC) algorithm to minimize the network service cost. Nevertheless, it is not suitable for large-scale multi-antenna systems considered in this paper.

Renewable energy sources based large-scale multi-antenna systems have attracted intensive studies from both academia and industry [29]–[34]. In [29], Demir *et al.* proposed a joint antenna and hybrid beamforming algorithm for multi-user relay systems based on simultaneous wireless information and power transfer (SWIPT). The relationship between SWIPT-based power transfer and throughput was studied in [30]. In [34], Men *et al.* proposed a joint relay and antenna selection algorithm based on the power splitting-based relaying (PSR) protocol to minimize the system outage probability. However, the SWIPT-based large-scale multi-antenna systems are quite different from our work since the main focus is on how to effectively transfer energy from the BS to terminals. In [31], Lei *et al.* studied the user association and power control problem in renewable energy-based heterogeneous networks, and proposed a low-complexity precoding scheme for co-channel interference cancellation. A geometric water-filling resource allocation algorithm with group upper bounded power constraints and recursion machinery was proposed to maximize the system throughput in [32]. However, most of these previous works assume that energy harvesting follows some well-known statistical models, and require the precise statistical information of energy arrival. In our previous work [33], we proposed an offline joint antenna selection and power allocation algorithm to maximize the energy efficiency of renewable energy

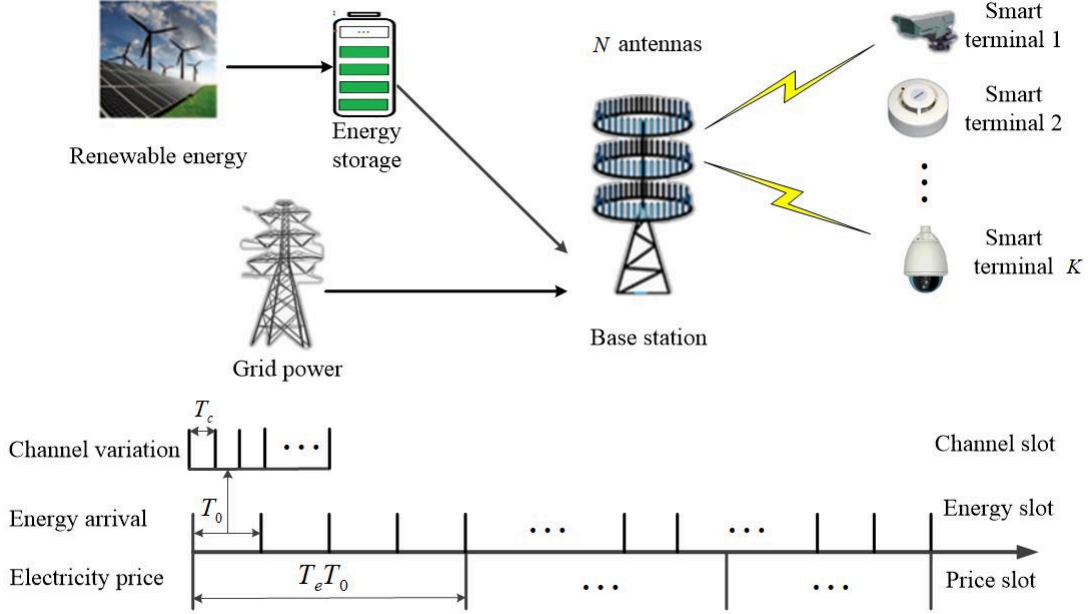


Fig. 1. System model

sources based large-scale multi-antenna systems. It requires perfect knowledge of future energy arrival and CSI, which is infeasible for practical implementation.

Different from above research attempts, we investigate how to jointly optimize antenna selection and power control in large-scale multi-antenna systems according to dynamic energy arrival, CSI, and electricity prices, which has not been considered before. Compared with [29]–[34], we consider a more practical scenario where even the statistical knowledge of uncertainties is unknown. Furthermore, we emphasize on a new performance metric named energy economic efficiency, which provides an effective benchmark for measuring the time-average throughput per unit energy cost. This new objective involves long-term optimization of a nonlinear fractional programming problem with both integer and continuous variables, which is not considered in [29]–[34].

### III. SYSTEM MODEL

We consider a typical downlink large-scale multi-antenna systems for smart grid, which is illustrated in Fig. 1. There are one BS and  $K$  smart terminals (STs). The BS is powered by two complementary energy sources including the fluctuating renewable energy sources and the reliable power grid. The renewable energy harvested from the external environment is stored in a capacity-constrained battery before usage, while the energy supply variability is compensated by the grid power. In the following, the models of energy arrival, electricity price, data transmission, and power consumption are introduced in details.

#### A. Dynamic Energy Arrival and Electricity Price Models

The dynamic process of renewable energy arrival and real-time electricity price over the continuous timeline is illustrated in Fig. 1. The time slot model proposed in [35], [36] is adopted. Specifically, we partition the time dimension into successive identical energy slots with slot duration  $T_0$  seconds, which are indexed by  $t_e = 1, 2, \dots, \infty$ . The time-scale difference among energy arrival, CSI variation, and electricity price variation has also been taken into consideration. Generally, it is assumed that CSI varies much faster than that of energy arrival, while electricity price varies much slower than that of energy arrival, i.e., electricity prices can be assumed as a deterministic value during a large number of energy slots. Therefore, each energy slot consists of  $T_0/T_c$  channel slots, where  $T_c$  is channel slot duration, and multiple energy slots, e.g.,  $T_e$  slots, are grouped as a price slot with duration of  $T_e T_0$  seconds, which is indexed by  $t_w = 1, 2, \dots, \infty$ . It is noted that in real-world implementations,  $\frac{T_0}{T_c}$  may not be an integer. The proposed algorithm can still be applicable since antenna selection and power control are jointly optimized at each energy slot instead of each channel slot.

In the smart grid, both energy arrival and electricity prices are varying temporally and spatially. Let  $E_{in}(t_e) \in [0, E_{max}]$  denote the amount of energy arrives to the battery at the  $t_e$ -th slot, which is i.i.d. over energy slots. Let  $\omega^E(t_w) \in [0, \omega_{max}^E]$  and  $\omega^G(t_w) \in [0, \omega_{max}^G]$  denote the prices of renewable energy and grid power at the  $t_w$ -th slot, which are i.i.d. over price slots, respectively. We can set  $0 < \omega^E < \omega^G$  to encourage the consumption of renewable energy.

Let  $B(t_e)$  denote the battery state and let  $P_{total}^E(t_e)$  denote the renewable power consumption at the  $t_e$ -th slot, respectively. Since the energy consumed at each slot cannot exceed the energy

stored in the battery, we have the energy causality constraint:

$$P_{total}^E(t_e)T_0 \leq B(t_e). \quad (1)$$

Then, the battery state can be modeled as a dynamic energy queue, where energy arrival and energy consumption represent the input and output of the queue, respectively. The energy queue is updated as

$$B(t_e + 1) = \min \{ B(t_e) - P_{total}^E(t_e)T_0 + E_{in}(t_e), B_{max} \}, \quad (2)$$

where  $B_{max}$  denotes the battery capacity.

*Remark 1:* Compared with previous works [33], [35], [37], we have not put any restriction on the statistical distributions of uncertain factors such as energy arrival and electricity price. In other words, the proposed joint resource allocation algorithm can be applicable even when the knowledge of statistical distributions is unknown.

### B. Data Transmission Model

The BS is assumed to be equipped with a total of  $N$  antennas ( $N \gg 1$ ), while each ST is based on a single antenna due to space and cost limitations. The downlink signal received at the terminal side is written as

$$y = \mathbf{H}^H \mathbf{W} \mathbf{x} + n_0, \quad (3)$$

where  $\mathbf{x}$  is the  $K \times 1$  transmission symbol vector, and  $\mathbf{W}$  is the  $N \times K$  precoding matrix. In this paper, we adopt the zero forcing (ZF) precoding scheme, i.e.,  $\mathbf{W} = \mathbf{H}(\mathbf{H}^H \mathbf{H})^{-1}$ , due to its superior performance and low complexity when  $N \gg K$  [38].  $\mathbf{H} = [\mathbf{h}_1, \mathbf{h}_2, \dots, \mathbf{h}_K]$  is the  $N \times K$  matrix of channel gain, and each element  $\mathbf{h}_k = [h_{k,1}, h_{k,2}, \dots, h_{k,N}]^T$  denotes the  $N$ -dimensional vector of channel gain between the BS and the  $k$ -th ST.  $n_0$  is additive white Gaussian noise (AWGN) which follows a normal distribution  $\mathcal{N}(0, \sigma^2 \mathbf{I}_K)$ , where  $\mathbf{I}_K$  is the  $N \times K$  identity matrix. Following the channel model assumptions used in [11], [39]–[41], we mainly consider resource allocation optimization based on the small-scale channel fading, and the elements in  $\mathbf{H}$  are independent identically distributed (i.i.d.) complex Gaussian random variables with the mean of zero and the variance of 0.5 per real dimension [11], [39], [40]. The assumption of small-scale Rayleigh flat fading is justified in [11], [39]–[41], i.e., adequate antenna spacing ensures channel decorrelation in a rich-scattering nonline-of-sight radio environment.



At the  $t_e$ -th energy slot, with antenna selection, the BS selects  $M(t_e) \in \{1, 2, \dots, N\}$  antennas with the largest channel gains, i.e.,  $\sum_{k=1}^K |h_{k,1}|^2 > \sum_{k=1}^K |h_{k,2}|^2 > \dots > \sum_{k=1}^K |h_{k,M(t_e)}|^2$ , from  $N$  antennas for data transmission. The rationale behind is that since the contributions of different antennas are not equal, the antennas with largest channel gains should be selected in priority. A similar assumption is also adopted in other previous works [11], [42]. The downlink spectral efficiency (bits/s/Hz) at the  $t_e$ -th energy slot is calculated as [42]

$$I_{sel}(t_e) = K \log_2 \left( 1 + \frac{P_{Tx}(t_e)}{K^2 \sigma^2} \sum_{j=1}^{M(t_e)} \sum_{k=1}^K |h_{k,j}|^2 \right), \quad (4)$$

where  $P_{Tx}(t_e)$  represents the transmission power at the  $t_e$ -th energy slot.

Based on the channel hardening phenomenon [42], we have the following theorem:

**Theorem 1.**  $I_{sel}$  defined in (4) follows a folded normal distribution, which is expressed as

$$I_{sel}(t_e) \sim \mathcal{FN} \left( K \log_2 \left[ 1 + \left( 1 + \ln \frac{N}{M(t_e)} \right) \frac{P_{Tx}(t_e) M(t_e)}{K \sigma^2} \right], \frac{(\log_2 e P_{Tx}(t_e))^2 M(t_e) \left( 2 - \frac{M(t_e)}{N} \right)}{K \sigma^4 \left[ 1 + \left( 1 + \ln \frac{N}{M(t_e)} \right) \frac{P_{Tx} M(t_e)}{K \sigma^2} \right]^2} \right). \quad (5)$$

*Proof:* Please see Appendix A. ■

*Remark 2:*  $M(t_e)$  represents the number of selected antennas at the  $t_e$ -th energy slot, which is an integer and is less than or equal to  $N$ . The value of  $M(t_e)$  is time-varying and should be dynamically determined by the proposed algorithm. It is noted that  $M(t_e)$  only indicates that how many antennas should be selected, while the CSI at each channel slot is used to determine which specific antennas are selected. We assume that the CSI is available for the BS. How to perform CSI estimation is out of the scope of this work and will be studied in the future.

### C. Power Consumption Model

Let  $P_{total}(t_e)$  denote the total power consumption of the BS at the  $t_e$ -th slot. According to [43],  $P_{total}(t_e)$  is expressed as

$$P_{total}(t_e) = P_C(t_e) + P_{Tx}(t_e) + P_{RF}(t_e) M(t_e), \quad (6)$$

where  $P_C(t_e)$ ,  $P_{Tx}(t_e)$ , and  $P_{RF}(t_e)$  represent the instantaneous circuit power, transmission power, and single RF chain circuit power at the  $t_e$ -th slot, respectively. Each part of the power

consumption comes from both the renewable energy stored in the battery and the power grid.

Thus,  $P_C$ ,  $P_{Tx}$  and  $P_{RF}$  are defined as

$$\begin{aligned} P_C(t_e) &= P_C^E(t_e) + P_C^G(t_e), \\ P_{Tx}(t_e) &= P_{Tx}^E(t_e) + P_{Tx}^G(t_e), \\ P_{RF}(t_e) &= P_{RF}^E(t_e) + P_{RF}^G(t_e), \end{aligned} \quad (7)$$

where  $P_C^E(t_e)$ ,  $P_{Tx}^E(t_e)$ , and  $P_{RF}^E(t_e)$  represent the instantaneous circuit power, transmission power, and single RF chain circuit power supplied by the battery at the  $t_e$ -th slot, respectively.  $P_C^G(t_e)$ ,  $P_{Tx}^G(t_e)$ , and  $P_{RF}^G(t_e)$  represent the instantaneous circuit power, transmission power, and single RF circuit chain power supplied by the power grid at the  $t_e$ -th slot, respectively.

The total power consumption of grid power and the total power consumption of renewable energy at the  $t_e$ -th slot are given by

$$P_{total}^G(t_e) = P_C^G(t_e) + P_{Tx}^G(t_e) + P_{RF}^G(t_e)M(t_e), \quad (8)$$

$$P_{total}^E(t_e) = P_C^E(t_e) + P_{Tx}^E(t_e) + P_{RF}^E(t_e)M(t_e). \quad (9)$$

#### IV. PROBLEM FORMULATION

In this section, we consider the optimization over  $T_\omega$  price slots, i.e., a total of  $T_e T_\omega$  energy slots. We define the antenna selection and power control policies as  $\mathcal{S} = \{\mathcal{S}_1, \dots, \mathcal{S}_{t_e}, \dots, \mathcal{S}_{T_e T_\omega}\}$  and  $\mathcal{P} = \{\mathcal{P}_1, \dots, \mathcal{P}_{t_e}, \dots, \mathcal{P}_{T_e T_\omega}\}$ , respectively, where  $\mathcal{S}_{t_e} = \{M(t_e)\}$  and  $\mathcal{P}_{t_e} = \{P_C^E(t_e), P_C^G(t_e), P_{Tx}^E(t_e), P_{Tx}^G(t_e), P_{RF}^E(t_e), P_{RF}^G(t_e)\}$ .

The expected throughput per unit bandwidth (bits/Hz) at the  $t_e$ -th slot is given by

$$U_{sel}(\mathcal{S}_{t_e}, \mathcal{P}_{t_e}) = \mathbb{E}\{I_{sel}(t_e)\}T_0 = K \log_2 \left[ 1 + \left( 1 + \ln \frac{N}{M(t_e)} \right) \frac{P_{Tx}(t_e)M(t_e)}{K\sigma^2} \right] T_0, \quad (10)$$

where  $\mathbb{E}\{\cdot\}$  denotes the expectation operator.

The energy cost (cents) at the  $t_e$ -th slot is given by

$$C_{total}(\mathcal{S}_{t_e}, \mathcal{P}_{t_e}) = \omega^E(t_e)P_{total}^E(t_e)T_0 + \omega^G(t_e)P_{total}^G(t_e)T_0. \quad (11)$$

Let  $\overline{U_{sel}}(\mathcal{S}, \mathcal{P})$  and  $\overline{C_{total}}(\mathcal{S}, \mathcal{P})$  denote the time-average throughput per unit bandwidth and the time-average energy cost over  $T_e T_\omega$  slots, respectively, which are given by

$$\overline{U_{sel}}(\mathcal{S}, \mathcal{P}) = \lim_{T_\omega \rightarrow \infty} \frac{1}{T_e T_\omega} \sum_{t_e=1}^{T_e T_\omega} \mathbb{E}\{U_{sel}(\mathcal{S}_{t_e}, \mathcal{P}_{t_e})\}, \quad (12)$$

$$\overline{C_{total}}(\mathcal{S}, \mathcal{P}) = \lim_{T_\omega \rightarrow \infty} \frac{1}{T_e T_\omega} \sum_{t_e=1}^{T_e T_\omega} \mathbb{E}\{C_{total}(\mathcal{S}_{t_e}, \mathcal{P}_{t_e})\}. \quad (13)$$

Let  $U_{E^3}$  denote the energy economic efficiency (bits/Hz/cent) which is defined as the ratio of the time-average throughput per unit bandwidth to the time-average energy cost.  $U_{E^3}$  can be written as

$$U_{E^3} = \frac{\overline{U_{sel}(\mathcal{S}, \mathcal{P})}}{\overline{C_{total}(\mathcal{S}, \mathcal{P})}}. \quad (14)$$

The energy-economic-efficient joint antenna selection and power control problem is formulated as

$$\begin{aligned} \mathbf{P1} : & \max_{(\mathcal{S}, \mathcal{P})} U_{E^3} \\ \text{s.t.} \quad & C_1 \sim C_9 \\ C_1 : & P_{total}^E(t_e)T_0 \leq B(t_e), \forall t_e, \\ C_2 : & P_C^E(t_e) + P_C^G(t_e) = P_C(t_e), \forall t_e, \\ C_3 : & P_{RF}^E(t_e) + P_{RF}^G(t_e) = P_{RF}(t_e), \forall t_e. \\ C_4 : & P_{Tx}(t_e) \leq P_{Tx,max}, \forall t_e, \\ C_5 : & P_{total}^G(t_e) \leq P_{max}^G, \forall t_e, \\ C_6 : & U_{sel}(\mathcal{S}_{t_e}, \mathcal{P}_{t_e}) \geq KR_{min}, \forall t_e, \\ C_7 : & \lim_{T_\omega \rightarrow +\infty} \frac{1}{T_e T_\omega} \sum_{t_e=1}^{T_e T_\omega} \mathbb{E} \{P_{Tx}(t_e)\} \leq P_{Tx,mean}, \\ C_8 : & M(t_e) \in [1, \dots, N], \forall t_e, \\ C_9 : & P_C^E(t_e), P_C^G(t_e), P_{Tx}^E(t_e), P_{Tx}^G(t_e), P_{RF}^E(t_e), P_{RF}^G(t_e) \geq 0, \forall t_e, \end{aligned} \quad (15)$$

where  $C_1$  is the energy causality constraint.  $C_2$  and  $C_3$  specify that the power required for reliable operations of BS and single RF chain should be guaranteed.  $C_4$  and  $C_5$  are instantaneous maximum transmission power and grid power constraints.  $C_6$  is the QoS requirement.  $C_7$  is the long-term constraint of transmission power.  $C_8$  and  $C_9$  specify the boundary constraints of optimization variables.

## V. ENERGY-ECONOMIC-EFFICIENT ONLINE JOINT RESOURCE ALLOCATION

In this section, the proposed joint resource allocation algorithm is presented. First, we introduce how to transform problem **P1** into a sequence of parameterized problems in subtractive form. Then, we introduce the formulation of Lyapunov optimization, in which the long-term stochastic

optimization problem is converted to a series of short-term deterministic optimization problems. Next, we propose an iterative online joint optimization algorithm based on bisection method and Lagrange dual decomposition.

#### A. Problem Transformation

Denote the optimum objective value of **P1** as  $q^*$ , which is given by

$$q^* = \max_{(\mathcal{S}, \mathcal{P})} U_{E^3} = \frac{\overline{U_{sel}}(\mathcal{S}^*, \mathcal{P}^*)}{\overline{C_{total}}(\mathcal{S}^*, \mathcal{P}^*)}, \quad (16)$$

where  $\mathcal{S}^*$  and  $\mathcal{P}^*$  represent the optimum antenna selection and power control policies, respectively. Based on nonlinear fractional programming [44], we have

**Theorem 2.** *The optimum objective value  $q^*$  is achievable if and only if*

$$\max_{(\mathcal{S}, \mathcal{P})} \overline{U_{sel}}(\mathcal{S}, \mathcal{P}) - q^* \overline{C_{total}}(\mathcal{S}, \mathcal{P}) = \overline{U_{sel}}(\mathcal{S}^*, \mathcal{P}^*) - q^* \overline{C_{total}}(\mathcal{S}^*, \mathcal{P}^*) = 0. \quad (17)$$

*Proof:* The details are omitted here due to space limitation. A similar proof can be found in [44]. ■

Based on Theorem 2, there exists an alternative subtractive-form problem which is equivalent to **P1**. Thus, **P1** can be rewritten as

$$\begin{aligned} \mathbf{P2} : & \max_{(\mathcal{S}, \mathcal{P})} \overline{U_{sel}}(\mathcal{S}, \mathcal{P}) - q^* \overline{C_{total}}(\mathcal{S}, \mathcal{P}) \\ \text{s.t.} \quad & C_1 \sim C_9. \end{aligned} \quad (18)$$

However, the specific value of  $q^*$  in **P2** is still unknown. Therefore, base on [45], we use an alternative variable  $q(t_e)$  to replace  $q^*$ , which is defined as

$$q(t_e) = \frac{\sum_{\tau=1}^{t_e} \mathbb{E}\{U_{sel}(\mathcal{S}_\tau, \mathcal{P}_\tau)\}}{\sum_{\tau=1}^{t_e} \mathbb{E}\{C_{total}(\mathcal{S}_\tau, \mathcal{P}_\tau)\}}. \quad (19)$$

Then **P2** can be rewritten as

$$\begin{aligned} \mathbf{P3} : & \max_{(\mathcal{S}, \mathcal{P})} \overline{U_{sel}}(\mathcal{S}, \mathcal{P}) - q(t_e) \overline{C_{total}}(\mathcal{S}, \mathcal{P}) \\ \text{s.t.} \quad & C_1 \sim C_9. \end{aligned} \quad (20)$$

*Remark 3:* **P3** is a mixed integer nonlinear programming (MINLP) problem, where both integer and continuous variables have to be jointly optimized. Furthermore, it also involves long-term optimization objective function and constraints. Therefore, **P3** is NP-hard and  $q(t_e)$  cannot be directly obtained by the conventional Dinkelbach approach [46].

### B. The Formulation of Lyapunov Optimization

Based on the concept of virtual queue [44], the long-term time-average constraint  $C_7$  of **P3** is converted to a queue stability constraint. Specifically, the virtual queue  $Z(t_e)$  associated with  $C_7$  is given by

$$Z(t_e + 1) = \max[Z(t_e) - P_{Tx,mean}, 0] + P_{Tx}(t_e). \quad (21)$$

We set the initial queue backlog as  $Z(1) = 0$ .

**Theorem 3.** *If  $Z(t_e)$  is mean rate stable,  $C_7$  holds automatically.*

*Proof:* The detailed proof is provided in Section VI. ■

Based on Theorem 3, **P3** can be rewritten as

$$\begin{aligned} \mathbf{P4} : & \max_{(\mathcal{S}, \mathcal{P})} \overline{U_{sel}}(\mathcal{S}, \mathcal{P}) - q(t_e) \overline{C_{total}}(\mathcal{S}, \mathcal{P}) \\ \text{s.t.} \quad & C_1 \sim C_6, C_8, C_9, \\ & C_{10} : \text{Queue } Z \text{ is mean rate stable.} \end{aligned} \quad (22)$$

Then, the Lyapunov function  $L(Z(t_e))$  is given by

$$L(Z(t_e)) = \frac{1}{2} Z^2(t_e). \quad (23)$$

We introduce a Lyapunov drift to push the Lyapunov function to a lower congestion state and keep the virtual queue stable. The Lyapunov drift is the expected change in the Lyapunov function over one slot, given that the current state at the  $t_e$ -th slot is  $Z(t_e)$ . Thus, the one-slot conditional Lyapunov drift is defined as

$$\Delta(Z(t_e)) \triangleq \mathbb{E}\{L(Z(t_e + 1)) - L(Z(t_e)) | Z(t_e)\}. \quad (24)$$

To maximize  $\overline{U_{sel}}(\mathcal{S}, \mathcal{P}) - q(t_e) \overline{C_{total}}(\mathcal{S}, \mathcal{P})$  under the constraint that queue  $Z$  is stable, we define the drift-minus-reward term as

$$DM(Z(t_e)) = \Delta(Z(t_e)) - V \mathbb{E}\{U_{sel}(\mathcal{S}_{t_e}, \mathcal{P}_{t_e}) - q(t_e) C_{total}(\mathcal{S}_{t_e}, \mathcal{P}_{t_e}) | Z(t_e)\}, \quad (25)$$

where  $V$  is a nonnegative parameter which controls the relative importance of the drift  $\Delta(Z(t_e))$  compared with the reward  $\mathbb{E}\{U_{sel}(\mathcal{S}_{t_e}, \mathcal{P}_{t_e}) - q(t_e)C_{total}(\mathcal{S}_{t_e}, \mathcal{P}_{t_e})|Z(t_e)\}$ , i.e., the tradeoff between “queue stability” and the “reward maximization”.

**Theorem 4.** *The drift-minus-reward term, i.e.,  $\Delta(Z(t_e)) - V\mathbb{E}\{U_{sel}(\mathcal{S}_{t_e}, \mathcal{P}_{t_e}) - q(t_e)C_{total}(\mathcal{S}_{t_e}, \mathcal{P}_{t_e})|Z(t_e)\}$ , is upper bounded by*

$$\begin{aligned} & \Delta(Z(t_e)) - V\mathbb{E}\{U_{sel}(\mathcal{S}_{t_e}, \mathcal{P}_{t_e}) - q(t_e)C_{total}(\mathcal{S}_{t_e}, \mathcal{P}_{t_e})|Z(t_e)\} \\ & \leq C + \mathbb{E}\{Z(t_e)[P_{Tx}(t_e) - P_{Tx,mean}]|Z(t_e)\} - V\mathbb{E}\{U_{sel}(\mathcal{S}_{t_e}, \mathcal{P}_{t_e}) - q(t_e)C_{total}(\mathcal{S}_{t_e}, \mathcal{P}_{t_e})|Z(t_e)\}, \end{aligned} \quad (26)$$

where  $C$  is a finite positive constant that satisfies

$$C \geq \mathbb{E}\left\{\frac{P_{Tx}^2(t_e) + P_{Tx,mean}^2}{2} \middle| Z(t_e)\right\}. \quad (27)$$

*Proof:* The detailed proof is omitted here due to space limitation. A similar proof can be found in [35]. ■

According to the principle of Lyapunov optimization, the upper bound of the drift-minus-reward term defined in (26) is minimized at each slot subject to constraints  $C_1 \sim C_6$ ,  $C_8$ , and  $C_9$ . Thus, **P4** can be rewritten as

$$\begin{aligned} \mathbf{P5} : & \min_{(\mathcal{S}_{t_e}, \mathcal{P}_{t_e})} Z(t_e)[P_{Tx}(t_e) - P_{Tx,mean}] - V[U_{sel}(\mathcal{S}_{t_e}, \mathcal{P}_{t_e}) - q(t_e)C_{total}(\mathcal{S}_{t_e}, \mathcal{P}_{t_e})] \\ \text{s.t.} & \quad C_1 \sim C_6, C_8, C_9. \end{aligned} \quad (28)$$

### C. Joint Antenna Selection and Power Control

In this subsection, we propose an iterative online algorithm to solve **P5**, which consists of the antenna selection algorithm summarized in Algorithm 1, and the power control algorithm summarized in Algorithm 2.

1) *Antenna Selection:* Algorithm 1 is based on the bisection method [47], which is an effective low-complexity searching algorithm with logarithmic complexity. It has been widely employed in various application scenarios including antenna selection [11] and power allocation [48]. It is noted that the bisection-based antenna selection algorithm developed in [11] cannot be directly applied because the coupling between antenna selection and energy domain optimization is not considered. Let  $\lfloor x \rfloor$  denote the largest integer that is less than or equal to  $x$ , and  $\lceil x \rceil$

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**Algorithm 1** Antenna Selection Algorithm
 

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1:  $M_{low}(t_e) \leftarrow 1, M_{high}(t_e) \leftarrow N,$ 
2: while  $M_{high}(t_e) - M_{low}(t_e) > 1$  do
3:   calculate  $M_{mid}(t_e) = \lfloor M_{high}(t_e) + M_{low}(t_e) \rfloor / 2,$ 
4:   given  $M_{mid}(t_e)$  and  $M_{mid}(t_e) - 1$ , obtain  $(\hat{\mathcal{P}}'_{t_e}, \hat{q}'(t_e))$ , and  $(\hat{\mathcal{P}}''_{t_e}, \hat{q}''(t_e))$  by Algorithm 2,
5:   if  $F_1(M_{mid}(t_e), \hat{\mathcal{P}}'_{t_e}, \hat{q}'(t_e)) \leq F_1(M_{mid}(t_e) - 1, \hat{\mathcal{P}}''_{t_e}, \hat{q}''(t_e))$ , then
6:      $M_{low}(t_e) = M_{mid}(t_e);$ 
7:   else if  $F_1(M_{mid}(t_e), \hat{\mathcal{P}}'_{t_e}, \hat{q}'(t_e)) > F_1(M_{mid}(t_e) - 1, \hat{\mathcal{P}}''_{t_e}, \hat{q}''(t_e))$ , then
8:      $M_{high}(t_e) = M_{mid}(t_e);$ 
9:   else
10:    break;
11:  end if
12: end while
13: if  $M_{high}(t_e) - M_{low}(t_e) = 1$ , then
14:    $M^*(t_e) = \arg \max_{(M_{high}(t_e), M_{low}(t_e))} \left[ F_1(M_{high}(t_e), \hat{\mathcal{P}}'_{t_e}, \hat{q}'(t_e)), F_1(M_{low}(t_e), \hat{\mathcal{P}}''_{t_e}, \hat{q}''(t_e)) \right];$ 
15: else
16:    $M^*(t_e) = M_{mid}(t_e);$ 
17: end if
18: Output:  $M^*(t_e).$ 

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denote the smallest integer that is not less than  $x$ . At the  $t_e$ -th slot, we start with an interval  $[M_{low}(t_e), M_{high}(t_e)]$ , which is known to contain the optimum antenna number  $M^*(t_e)$ . In each iteration, we calculate  $M_{mid}(t_e)$  and  $M_{mid}(t_e) - 1$ , and obtain the corresponding optimum power control policy  $\hat{\mathcal{P}}'_{t_e}$  and  $\hat{\mathcal{P}}''_{t_e}$  respectively by using Algorithm 2. It is noted that only the last two terms of P5 involve the variables of antenna selection. Thus, we define  $F_1(M(t_e), \mathcal{P}_{t_e}, (t_e))$  as

$$F_1(M(t_e), \mathcal{P}_{t_e}, q(t_e)) = U_{sel}(M(t_e), \mathcal{P}_{t_e}) - q(t_e)C_{total}(M(t_e), \mathcal{P}_{t_e}). \quad (29)$$

Then, we compare  $F_1(M_{mid}(t_e), \hat{\mathcal{P}}'_{t_e}, \hat{q}'(t_e))$  with  $F_1(M_{mid}(t_e) - 1, \hat{\mathcal{P}}''_{t_e}, \hat{q}''(t_e))$  to determine whether  $M^*(t_e)$  lies in the interval  $[M_{low}(t_e), M_{mid}(t_e)]$  or the interval  $[M_{mid}(t_e), M_{high}(t_e)]$ ,

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**Algorithm 2** Iterative Power Control Algorithm
 

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- 1: **Input:**  $P_C(t_e)$ ,  $P_{RF}(t_e)$ ,  $P_{Tx,max}$ ,  $P_{max}^G$ ,  $R_{min}$ ,  $q(t_e, 1)$ ,  $Z(t_e)$ ,  $L_{max}$ ,  $\Delta$ .
  - 2: Obtain  $M(t_e)$  by Algorithm 1.
  - 3: **Initialize:**  $n = 1$ .
  - 4: **while**  $n \leq L_{max}$  **do**
  - 5:   for a given  $q(t_e, n)$  and  $M(t_e)$ , solve (33) to obtain  $\hat{\mathcal{P}}_{t_e}(n)$ ,
  - 6:   **if**  $|U_{sel}(M(t_e), \hat{\mathcal{P}}_{t_e}(n)) - q(t_e, n)C_{total}(M(t_e), \hat{\mathcal{P}}_{t_e}(n))| > \Delta$ , **then**
  - 7:      $q(t_e, n+1) = \left( \sum_{\tau=1}^{t_e-1} \mathbb{E}\{U_{sel}(\mathcal{S}_\tau, \mathcal{P}_\tau)\} + \mathbb{E}\{U_{sel}(M(t_e), \hat{\mathcal{P}}_{t_e}(n))\} \right) /$   
        $\left( \sum_{\tau=1}^{t_e-1} \mathbb{E}\{C_{total}(\mathcal{S}_\tau, \mathcal{P}_\tau)\} + \mathbb{E}\{C_{total}(M(t_e), \hat{\mathcal{P}}_{t_e}(n))\} \right);$
  - 8:   **else**
  - 9:      $\mathcal{P}_{t_e}^* = \hat{\mathcal{P}}_{t_e}(n)$ , and  $q(t_e) = q(t_e, n)$ ;
  - 10:   **break;**
  - 11:   **end if**
  - 12:   **Update:**  $n \rightarrow n + 1$ .
  - 13: **end while**
  - 14: **Output:**  $q(t_e)$ ,  $\mathcal{P}_{t_e}^*$ .
  - 15: Calculate the virtual queue  $Z(t_e+1)$  of next slot based on (21), and update  $q(t_e+1, 1) = q(t_e)$ .
- 

which is given by

$$\begin{cases} M_{low}(t_e) = M_{mid}(t_e), & \text{if } F_1(M_{mid}(t_e), \hat{\mathcal{P}}'_{t_e}, \hat{q}'(t_e)) \leq F_1(M_{mid}(t_e) - 1, \hat{\mathcal{P}}''_{t_e}, \hat{q}''(t_e)), \\ M_{high}(t_e) = M_{mid}(t_e), & \text{otherwise.} \end{cases} \quad (30)$$

If  $F_1(M_{mid}(t_e), \hat{\mathcal{P}}'_{t_e}, \hat{q}'(t_e)) \leq F_1(M_{mid}(t_e) - 1, \hat{\mathcal{P}}''_{t_e}, \hat{q}''(t_e))$ ,  $M^*(t_e)$  lies in the interval  $[M_{mid}(t_e), M_{high}(t_e)]$  and  $M_{low}(t_e) = M_{mid}(t_e)$ . Otherwise,  $M^*(t_e)$  lies in the interval  $[M_{low}(t_e), M_{mid}(t_e)]$  and  $M_{high}(t_e) = M_{mid}(t_e)$ . The details are provided in line 5 ~ 11 of Algorithm 1.

2) *Power Control:* The power control algorithm is provided as Algorithm 2.  $L_{max}$  denotes the total iteration number,  $n$  denotes the iteration index, and  $\Delta$  denotes the tolerance threshold. We use  $q(t_e, n)$  to represent  $q(t_e)$  obtained from the  $(n - 1)$ -th iteration at the  $t_e$ -th slot, the initial value of which is  $q(1, 1) = 0$ . Then, at the  $n$ -th iteration, by using  $q(t_e, n)$ , we can obtain



$\hat{\mathcal{P}}_{t_e}(n)$  associated with  $M(t_e)$  by solving the following power control problem.

$$\begin{aligned} \mathbf{P6} : \min_{(\mathcal{P}_{t_e})} & Z(t_e)[P_{Tx}(t_e) - P_{Tx,mean}] - V[U_{sel}(M(t_e), \mathcal{P}_{t_e}(n)) - q(t_e, n)C_{total}(M(t_e), \mathcal{P}_{t_e}(n))] \\ \text{s.t.} & C_1 \sim C_6, C_9. \end{aligned} \quad (31)$$

It is noted that (31) is concave with differentiable objective function and constraints. The corresponding augmented Lagrangian is give by (32).

$$\begin{aligned} \mathcal{L}_{M(t_e)}^{E^3}(\mathcal{P}_{t_e}, \alpha_{t_e}, \beta_{t_e}, \gamma_{t_e}, \delta_{t_e}, \zeta_{t_e}, \theta_{t_e}) &= Z(t_e)[P_{Tx}(t_e) - P_{Tx,mean}] \\ &- V[U_{sel}(M(t_e), \mathcal{P}_{t_e}) - q(t_e, n)C_{total}(M(t_e), \mathcal{P}_{t_e}(n))] + \alpha_{t_e}(n) [P_{total}^E(t_e)T_0 - B(t_e)] \\ &+ \beta_{t_e}(n) [P_C^E(t_e) + P_C^G(t_e) - P_C(t_e)] + \gamma_{t_e}(n) [P_{RF}^E(t_e) + P_{RF}^G(t_e) - P_{RF}(t_e)] \\ &+ \delta_{t_e}(n) [P_{Tx}^E(t_e) + P_{Tx}^G(t_e) - P_{Tx,mean}] + \zeta_{t_e}(n) [P_{total}^G(t_e) - P_{max}^G] \\ &- \theta_{t_e}(n) [U_{sel}(M(t_e), \mathcal{P}_{t_e}) - K R_{min}]. \end{aligned} \quad (32)$$

The Lagrange multipliers associated with constraints  $C_1 \sim C_6$  are defined as  $\alpha_{t_e}, \beta_{t_e}, \gamma_{t_e}, \delta_{t_e}, \zeta_{t_e}$ , and  $\theta_{t_e}$ , respectively. The equivalent Lagrange dual problem is given by

$$\max_{(\alpha_{t_e}, \beta_{t_e}, \gamma_{t_e}, \delta_{t_e}, \zeta_{t_e}, \theta_{t_e} \geq 0)} \min_{(\mathcal{P}_{t_e})} \mathcal{L}_{M(t_e)}^{E^3}(\mathcal{P}_{t_e}, \alpha_{t_e}, \beta_{t_e}, \gamma_{t_e}, \delta_{t_e}, \zeta_{t_e}, \theta_{t_e}). \quad (33)$$

Denote the optimal power control policy associated with  $q(t_e, n)$  as  $\hat{\mathcal{P}}_{t_e}(n) = \{\hat{\mathcal{P}}_C^E(t_e, n), \hat{\mathcal{P}}_C^G(t_e, n), \hat{\mathcal{P}}_{Tx}^E(t_e, n), \hat{\mathcal{P}}_{Tx}^G(t_e, n), \hat{\mathcal{P}}_{RF}^E(t_e, n), \hat{\mathcal{P}}_{RF}^G(t_e, n)\}$ .  $\hat{\mathcal{P}}_{t_e}(n)$  can be obtained by using Karush-Kuhn-Tucker (KKT) conditions. Then, the Lagrange multipliers are updated based on the sub-gradient method [49], [50]. Next,  $q(t_e, n+1)$  for the next iteration is calculated based on  $M(t_e)$  and  $\hat{\mathcal{P}}_{t_e}(n)$ . The details are provided in line 4 ~ 12 of Algorithm 2.

## VI. PERFORMANCE ANALYSIS

In this section, the theoretical properties in terms of queue stability, performance bound, and complexity are analyzed.

### A. Stability of Virtual Queue

If the virtual queue  $Z(t_e)$  is mean rate stable, then the constraint  $C_7$  holds automatically. The proof is provided as follows.

**Theorem 5.** *The virtual queue  $Z(t_e)$  is mean rate stable.*

TABLE I  
SIMULATION PARAMETERS.

Parameter	Value
Maximum transmission power constraint $P_{Tx,max}$	46 dBm
Average transmission power constraint $P_{Tx,mean}$	45 dBm
Constant operation power $P_C$	160.8 W
RF chain power $P_{RF}$	0, 160, 450 mW
Antenna number $N$	100
Maximum grid power $P_{max}^G$	300 W
QoS $R_{min}$	7 bits/Hz
The number of smart terminals $K$	4
The variance $\sigma_0^2$	1

*Proof:* We assume that both  $U_{sel}(\mathcal{S}_{t_e}, \mathcal{P}_{t_e})$  and  $C_{total}(\mathcal{S}_{t_e}, \mathcal{P}_{t_e})$  are bounded by

$$\begin{aligned} U_{sel,min} &\leq U_{sel}(\mathcal{S}_{t_e}, \mathcal{P}_{t_e}) \leq U_{sel,max}, \\ C_{total,min} &\leq C_{total}(\mathcal{S}_{t_e}, \mathcal{P}_r) \leq C_{total,max}, \end{aligned} \quad (34)$$

where  $U_{sel,min}$ ,  $U_{sel,max}$ ,  $C_{total,min}$ , and  $C_{total,max}$  are finite positive constants. Based on (26) and (34), there exists a positive constant  $C$  that satisfies

$$\Delta(Z(t_e)) \leq C. \quad (35)$$

Then, according to (24), we have

$$\mathbb{E}\{L(Z(t_e + 1)) - L(Z(t_e)) | Z(t_e)\} \leq C. \quad (36)$$

We can take expectations of both sides of (36) and use the law of iterated expectations to yield

$$\mathbb{E}\{L(Z(t_e + 1))\} - \mathbb{E}\{L(Z(t_e))\} \leq C. \quad (37)$$

Summing over  $t_e \in \{1, 2, \dots, T_e T_\omega\}$  and using the law of telescoping sums yields

$$\mathbb{E}\{L(Z(T_e T_\omega))\} - \mathbb{E}\{L(Z(1))\} \leq C T_e T_\omega. \quad (38)$$

Using (23), (38) can be rewritten as

$$\mathbb{E}\{Z(T_e T_\omega)^2\} \leq 2C T_e T_\omega + 2\mathbb{E}\{L(Z(1))\}. \quad (39)$$

Since the variance of  $|Z(T_e T_\omega)|$  is positive, we have  $\mathbb{E}\{Z(T_e T_\omega)^2\} \geq \mathbb{E}\{Z(T_e T_\omega)\}^2$ . Thus, we can get

$$\mathbb{E}\{Z(T_e T_\omega)\} \leq \sqrt{2CT_e T_\omega + 2\mathbb{E}\{L(Z(1))\}}. \quad (40)$$

Next, dividing (40) by  $T_e T_\omega$  and taking the limit  $T_\omega \rightarrow \infty$  proves that

$$\lim_{T_\omega \rightarrow \infty} \frac{\mathbb{E}\{Z(T_e T_\omega)\}}{T_e T_\omega} = 0. \quad (41)$$

Thus, the virtual queue  $Z(t_e)$  is mean rate stable.  $\blacksquare$

We can rewrite (21) as

$$Z(t_e + 1) - Z(t_e) = P_{Tx}(t_e) - \hat{P}(t_e), \quad (42)$$

where  $\hat{P}(t_e)$  is given by

$$\hat{P}(t_e) = \min [Z(t_e), P_{Tx,mean}]. \quad (43)$$

Summing (42) over  $t_e = [1, 2, \dots, T_e T_\omega]$  and using the law of telescoping sums yields:

$$Z(T_e T_\omega) - Z(1) = \sum_{t_e=1}^{T_e T_\omega} P_{Tx}(t_e) - \sum_{t_e=1}^{T_e T_\omega} \hat{P}(t_e). \quad (44)$$

Combining (43) and (44), we have

$$Z(T_e T_\omega) - Z(1) \geq \sum_{t_e=1}^{T_e T_\omega} P_{Tx}(t_e) - \sum_{t_e=1}^{T_e T_\omega} P_{Tx,mean}. \quad (45)$$

Finally, dividing (45) by  $T_e T_\omega$  and taking the limit  $T_\omega \rightarrow \infty$ , we have

$$\lim_{T_\omega \rightarrow +\infty} \frac{1}{T_e T_\omega} \sum_{t_e=1}^{T_e T_\omega} \mathbb{E}\{P_{Tx}(t_e)\} \leq P_{Tx,mean}. \quad (46)$$

This proves that constraint  $C_7$  holds.

### B. Tradeoff between Queue Stability and Reward Maximization

The energy economic efficiency performance and the average queue backlog performance obtained by the proposed algorithm is given in Theorem 6.

**Theorem 6.** *The energy economic efficiency  $U_{E^3}$  and the average backlog of the virtual queue  $Z$  are bounded by*

$$U_{E^3} \geq q^* - \frac{C}{VC_{total,min}}, \quad (47)$$

$$Z \leq \frac{C + V(U_{sel,max} - q^* C_{total,min})}{\epsilon}. \quad (48)$$

*Proof:* Please see Appendix B. ■

*Remark 4:* Theorem 6 shows that economic energy efficiency achieved by the algorithm is bounded as

$$q^* - \frac{C}{VC_{total,min}} \leq U_{E^3} \leq q^*. \quad (49)$$

When  $V$  is large enough, the value of  $\frac{C}{VC_{total,min}}$  can be arbitrarily small, so that  $U_{E^3}$  can arbitrarily approach the optimum objective value  $q^*$ . As a result, there exists an  $[O(1/V), O(V)]$  tradeoff between “queue stability” and “reward maximization”.

### C. Complexity Analysis

For each slot, Algorithm 1 requires at most  $\lceil \log_2[M_{high}(t_e) - M_{low}(t_e)] \rceil + 1$  comparisons to find the optimum  $M^*(t_e)$ . In comparison, the computational complexity of the exhaustive search method grows exponentially as  $N$  increases. For example, with a total of  $N = 100$  antennas, Algorithm 1 needs approximately 8 comparisons to find the optimal number of selected antennas while the exhaustive search method requires 99 comparisons, i.e., the computational complexity is reduced by nearly 98.9%. Hence, Algorithm 1 has a much lower complexity than the exhaustive method. Algorithm 2 has a complexity  $\mathcal{O}(L_{max}^{Loop} \times L_{max}^{dual})$ , where  $L_{max}^{Loop}$  and  $L_{max}^{dual}$  are iteration numbers needed by the nonlinear fractional programming and Lagrange dual decomposition in each slot, respectively.

## VII. SIMULATION RESULTS

In this section, we verify the proposed algorithm through simulations. Simulation parameters are summarized in Table I [33], [43], [51]. Two heuristic algorithms are used as baselines for comparison purpose. The baseline 1 algorithm relies on the statistical information of energy arrival and electricity price for decision making and always uses all the available antennas, i.e., antenna selection is not considered. The baseline 2 algorithm is developed based on the snapshot-based optimal algorithm [52], which maximizes  $U_{E^3}$  at each energy slot without considering the long-term optimization objective and constraints.

Fig. 20 shows the relations between the energy economic efficiency  $U_{E^3}$  and the selected antenna number  $M$  in one energy slot. The electricity prices of renewable energy and grid power are set as  $\omega^E = 0.3$  cents/kWh and  $\omega^G = 3$  cents/kWh, respectively. For the purpose of illustration, the battery capacity is set as  $B_{max} = 1000$  J, and the energy arrival is set as

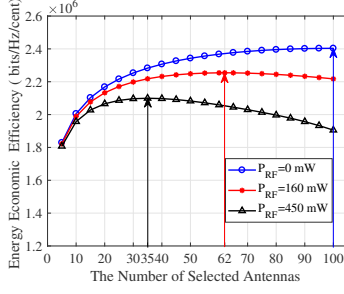


Fig. 2. Energy economic efficiency  $U_{E3}$  versus the number of selected antennas  $M$ .

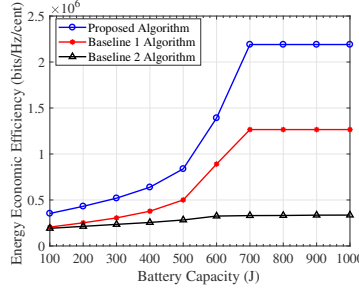


Fig. 3. Energy economic efficiency  $U_{E3}$  versus the battery capacity  $B_{max}$ .

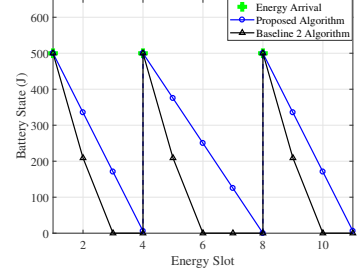


Fig. 4. A snapshot of the battery state.

$E_{in}(t_e) = 700$  J. Simulation results demonstrate that  $U_{E3}$  is a monotonically increasing function of  $M$  in the ideal case that the single RF chain is energy free, i.e.,  $P_{RF} = 0$  mW. However, in the nonideal case, i.e.,  $P_{RF} = 160$  mW or  $P_{RF} = 450$  mW,  $U_{E3}$  increases first and then decreases monotonically with  $M$ . The optimum antenna numbers for  $P_{RF} = 160$  mW or  $P_{RF} = 450$  mW are  $M^* = 62$  and  $M^* = 35$ , respectively. We found that the optimum antenna number decreases monotonically as  $P_{RF}$  increases.

Fig. 12 shows the relations between the energy economic efficiency  $U_{E3}$  and the battery capacity  $B_{max}$ . We set  $T_\omega = 20$  and  $T_e = 5$ , i.e., a total of 100 energy slots. The energy slot duration is set as  $T_0 = 3$  s [35, 52, 53]. It is noted that the proposed algorithm is also applicable to other timescales, which provides great scalability and compatibility. The parameter  $V$  is set as 10, and  $E_{in}(t_e)$  follows a uniform distribution within the interval  $[0, 500]$  J. The entire region can be divided into two regimes, i.e., the battery-capacity limited regime ( $0 \text{ J} \leq B_{max} \leq 600 \text{ J}$ ), and the renewable-energy limited regime ( $600 \text{ J} \leq B_{max} \leq 1000 \text{ J}$ ). In the battery-capacity limited regime, the performance gap between the proposed algorithm and baseline algorithms is small because the performance is degraded significantly due to the frequent energy overflow caused by the limited battery capacity. On the other hand, in the renewable-energy limited regime, the proposed algorithm outperforms the baseline 1 algorithm and baseline 2 algorithm by 73% and 552% ( $B_{max} = 1000 \text{ J}$ ), respectively. The reason is further elaborated in Fig. 21 and Fig. 22. The baseline 2 algorithm without the awareness of long-term optimization objective and constraints performs the worst among the three.

The snapshots of battery states and energy economic efficiency are shown in Fig. 21 and Fig. 22, respectively. We consider  $T_\omega = 2$ , and  $T_e = 5$ , i.e., a total of  $T_e T_\omega = 10$  energy slots. The

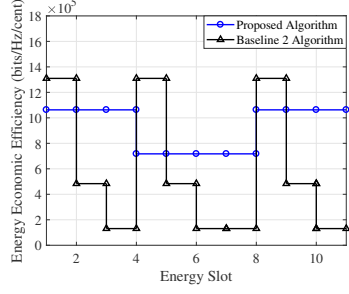


Fig. 5. A snapshot of the energy economic efficiency  $U_E^3$ .

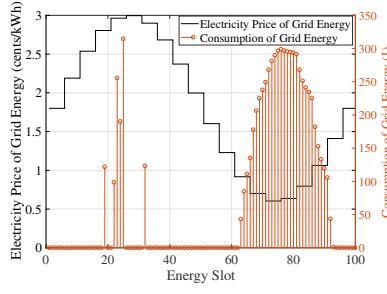


Fig. 6. Adaptiveness for the electricity price of grid energy.

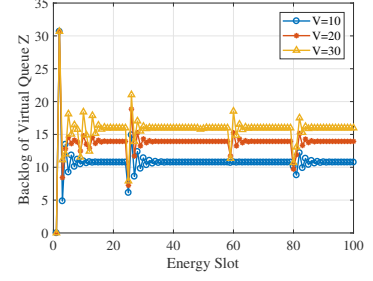


Fig. 7. A snapshot of the backlog of virtual queue  $Z$ .

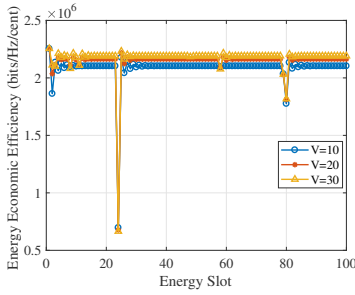


Fig. 8. A snapshot of energy economic efficiency.

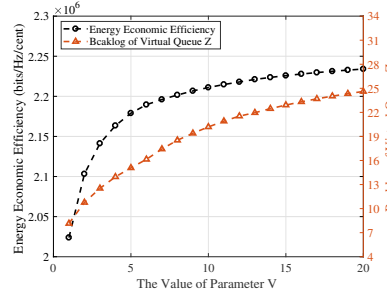


Fig. 9. Energy economic efficiency performance and backlog of queue  $Z$  versus the parameter  $V$ .

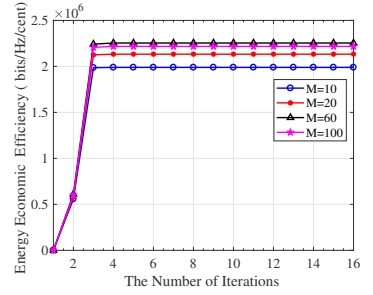


Fig. 10. The convergence performances with different value of  $M$ .

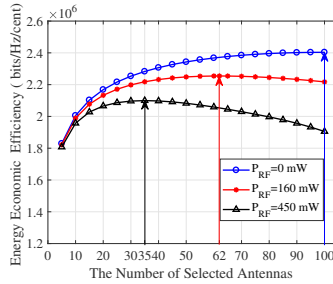


Fig. 11. Economic energy efficiency  $U_E^3$  versus the number of selected antennas  $M$ .

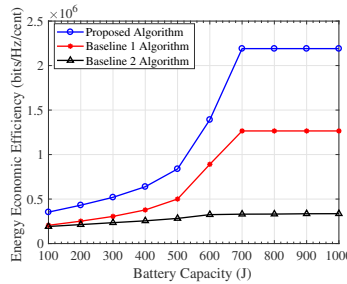


Fig. 12. Economic energy Efficiency  $U_E^3$  versus the battery capacity  $B_{max}$ .

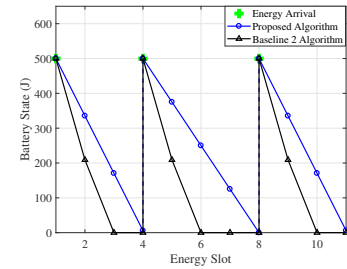


Fig. 13. A snapshot of the battery state.

slot duration is set as  $T_0 = 1$  s. The battery capacity is set as  $B_{max} = 700$  J, and the initial battery state is 500 J. The parameter  $V$  is set as 10. The energy arrival is set as  $E_{in}(t_e) = 500$  J when  $t_e = 4, 8$ , and  $E_{in}(t_e) = 0$  J otherwise. In the baseline 2 algorithm, the renewable energy is

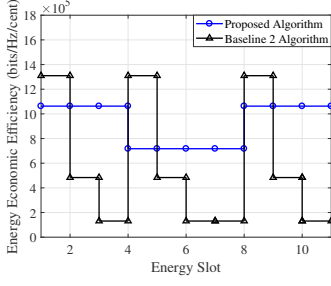
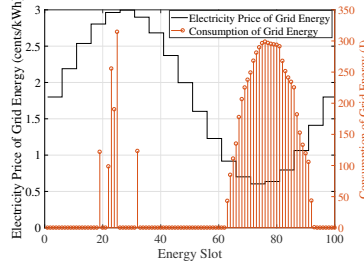


Fig. 14. A snapshot of the energy economic efficiency  $U_{E^3}$ .



versus electricity price.

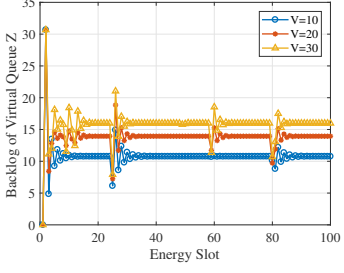


Fig. 16. Virtual queue backlog versus control parameter  $V$ .

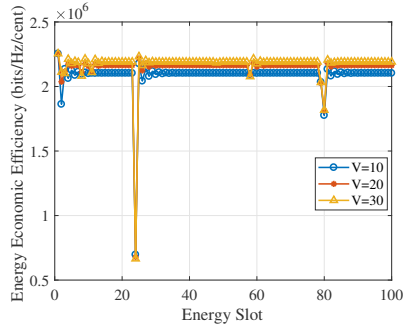


Fig. 17. Energy economic efficiency versus control parameter  $V$ .

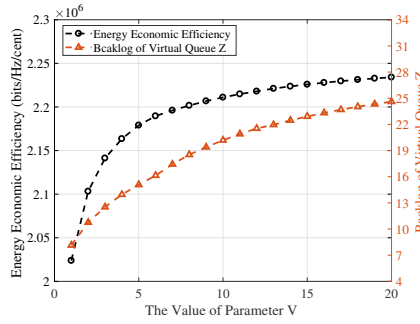


Fig. 18. The tradeoff between energy economic efficiency and virtual queue backlog.

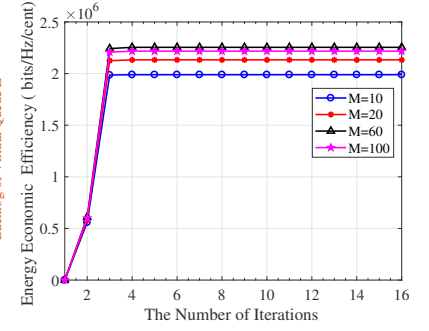


Fig. 19. Energy economic efficiency versus number of iterations  $n$ .

used more aggressively than the proposed algorithm because only the performance of the current slot is optimized. For example, the baseline 2 algorithm uses out all the stored energy at the 6-th slot while the next energy arrival is at the 8-th slot. Then, the expensive grid power has to be used, which results in severe performance degradation as shown in Fig. 22.

Fig. 23 shows relations between electricity price and energy consumption. We set  $T_w = 20$  and  $T_e = 5$ , i.e., a total of  $T_e T_w = 100$  energy slots. The parameter  $V$  is set as 10.  $E_{in}(t_e)$  follows a uniform distribution within the interval  $[0, 700]$  J when  $t_e = [1, 50]$  slots, and follows a uniform distribution within the interval  $[0, 400]$  J when  $t_e = [51, 100]$  slots. The price of renewable energy is set as 1 cent/kWh. Simulation results show that the proposed algorithm can dynamically adapt grid power consumption with time-varying electricity price. It is able to reduce the consumption amount of the expensive grid power during the peak-price period.

Fig. 24 and Fig. 25 show the impact of control parameter  $V$  on queue backlog and energy

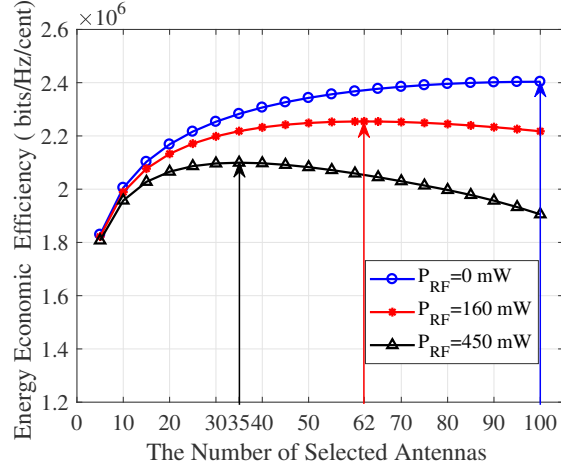


Fig. 20. Economic energy efficiency  $U_{E^3}$  versus the number of selected antennas  $M$ .

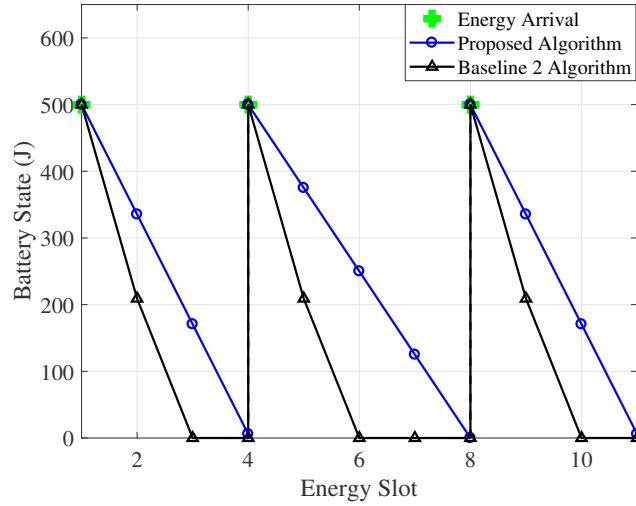


Fig. 21. A snapshot of the battery state.

economic efficiency, respectively. We compare the performances under three scenarios that  $V = 10, 20, 30$ .  $E_{in}(t_e)$  follows a uniform distribution within the interval  $[0, 700]$  J. Fig. 24 shows that the queue backlog is able to converge to a stable state within a short period of time under all the scenarios. The change of  $V$  mainly affects the final stable state rather than the convergence speed. Fig. 25 shows that the energy economic efficiency of the proposed algorithm is dynamically optimized in accordance with the energy arrival and electricity prices. The  $[O(1/V), O(V)]$



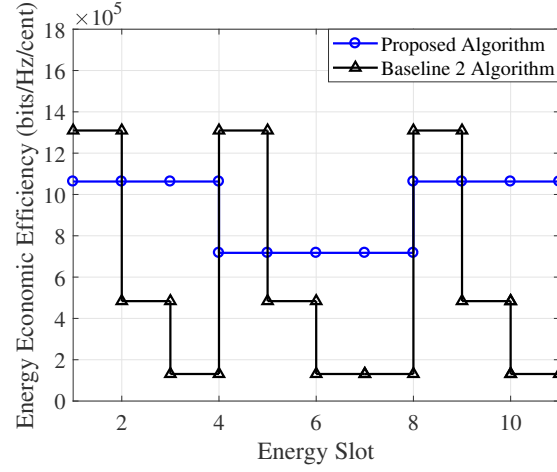


Fig. 22. A snapshot of the energy economic efficiency.

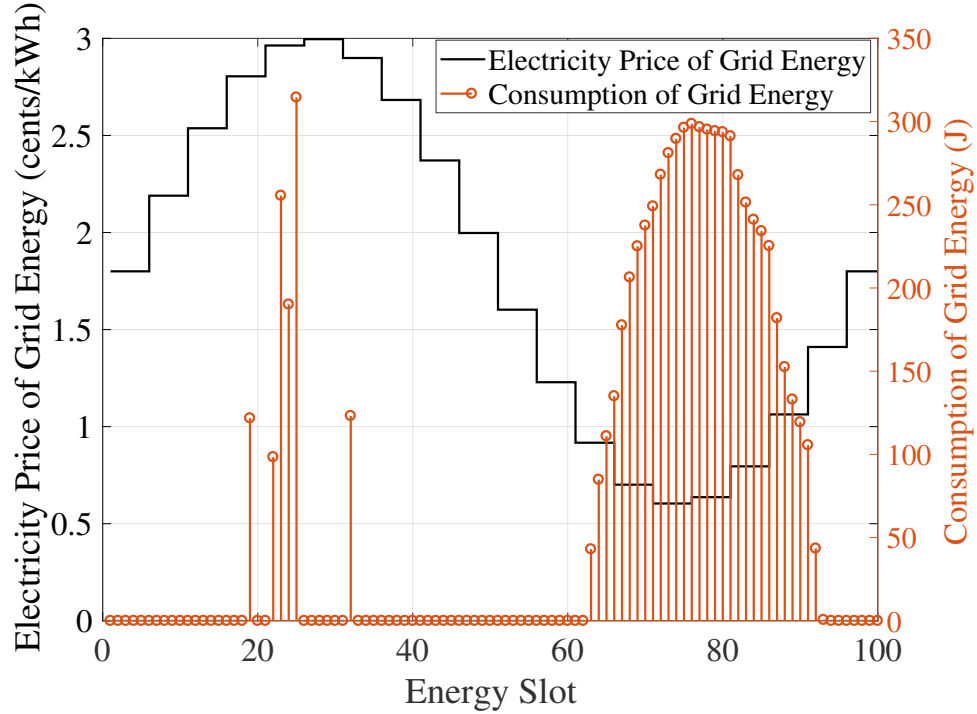


Fig. 23. Adaptiveness for the electricity price of smart grid.

tradeoff between queue backlog and energy economic efficiency is also validated in Fig. 26, i.e., the energy economic efficiency decreases monotonically with  $V$  while the queue backlog increases monotonically with  $V$ .

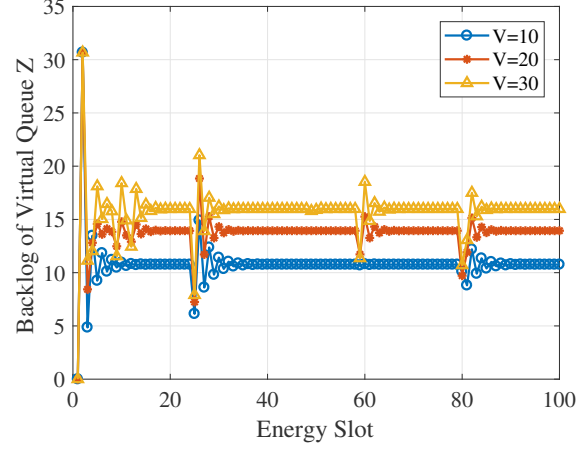


Fig. 24. A snapshot of the backlog of virtual queue Z

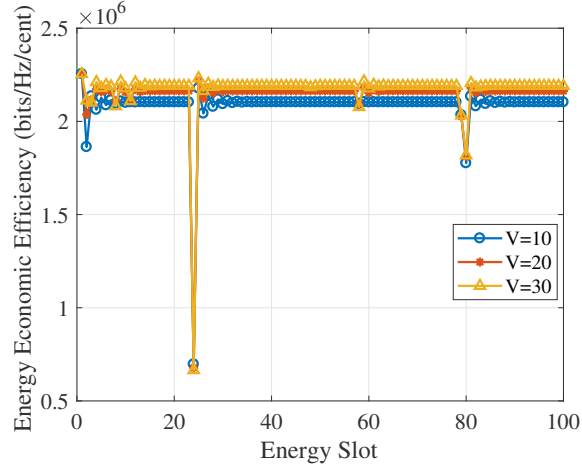


Fig. 25. A snapshot of energy economic efficiency.

Fig. 27 shows the convergence performance of Algorithm 2 under different simulation scenarios that  $M = 10, 20, 60, 100$ . Simulation results demonstrate the proposed algorithm only requires  $3 \sim 4$  iterations for convergence, which is feasible for practical implementation.

## VIII. CONCLUSION

In this paper, we studied the implementation of large-scale multi-antenna systems for smart grid. First, we developed a new performance benchmark named energy economic efficiency for measuring the time-average throughput per unit energy cost. Then, we developed an online

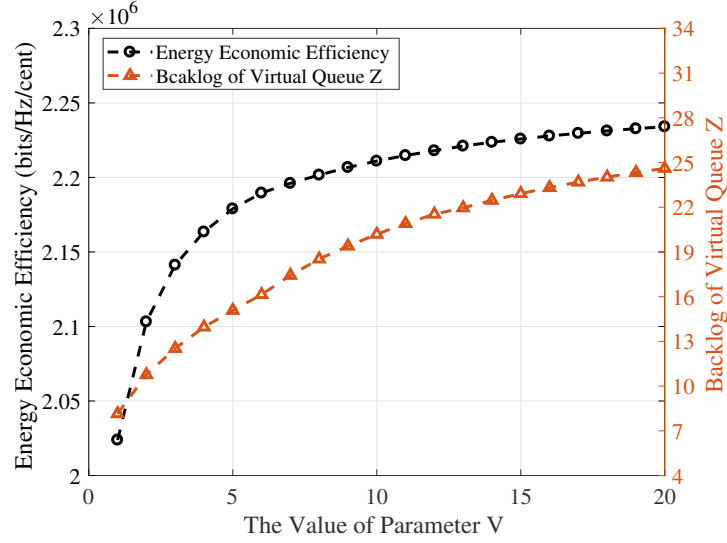


Fig. 26. Economic energy efficiency performance and backlog of queue  $Z$  versus the parameter  $V$ .

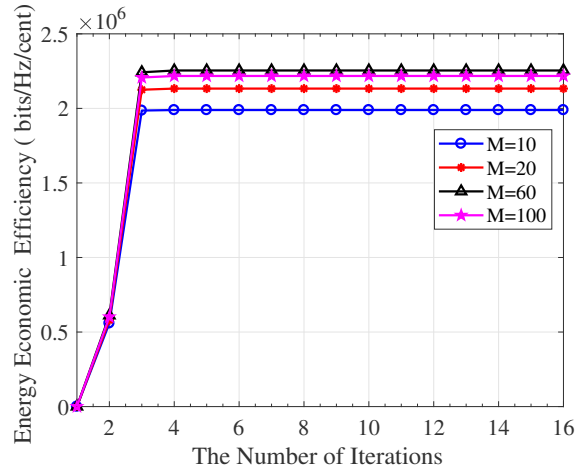


Fig. 27. The number of iterations  $n$  of fractional optimization

joint antenna selection and power control algorithm to maximize the long-term energy economic efficiency performance by combining nonlinear fractional programming, Lyapunov optimization, and bisection method. We proved that the proposed algorithm can achieve bounded performance deviation from the optimum performance without requiring the prior knowledge of future energy arrival and electricity price. Simulation results show that the proposed algorithm outperforms the baseline 1 algorithm and baseline 2 algorithm by 73% and 552%, respectively, when the battery

capacity is sufficient. It is also observed that there exists a  $[O(1/V), O(V)]$  tradeoff between queue backlog and energy economic efficiency, and the proposed algorithm can dynamically adapt grid power consumption with time-varying electricity price. In the future work, we plan to study how to integrate learning capabilities with existing framework to further improve the performance.

## APPENDIX A

### PROOF OF THEOREM 1

According to (4), we have

$$\begin{aligned}
 I_{sel} &= K \log_2 \left| 1 + \frac{P_{Tx}}{\sigma^2 K^2} \sum_{j=1}^M \sum_{k=1}^K |h_{k,j}|^2 \right| \\
 &= K \log_2 \left| \left[ 1 + \frac{P_{Tx}}{\sigma^2 K} \left( 1 + \ln \frac{N}{M} \right) \right] r \right| \\
 &= K \left[ \log_2 \left| 1 + \frac{P_{Tx}}{\sigma^2 K} \left( 1 + \ln \frac{N}{M} \right) \right| + \log_2 |r| \right] \\
 &= K \left[ \log_2 \left| 1 + \frac{P_{Tx}}{\sigma^2 K} \left( 1 + \ln \frac{N}{M} \right) \right| + \log_2 (1 + |r| - 1) \right] \\
 &= K \left[ \log_2 \left| 1 + \frac{P_{Tx}}{\sigma^2 K} \left( 1 + \ln \frac{N}{M} \right) \right| + (|r| - 1) \log_2 e \right], \tag{50}
 \end{aligned}$$

where  $|\cdot|$  denotes the absolute value, and  $r$  is given by

$$r = 1 + \frac{\frac{P_{Tx}}{\sigma^2 K^2} \sum_{j=1}^M \sum_{k=1}^K |h_{k,j}|^2 - \frac{P_{Tx} M}{\sigma^2 K} \left( 1 + \ln \frac{N}{M} \right)}{1 + \left( 1 + \ln \frac{N}{M} \right) \frac{P_{Tx} M}{\sigma^2 K}}. \tag{51}$$

According to [11], we have

$$\sum_{j=1}^M \sum_{k=1}^K |h_{k,j}|^2 \sim \mathcal{N} \left( KM \left( 1 + \ln \frac{N}{M} \right), KM \left( 2 - \frac{M}{N} \right) \right). \tag{52}$$

Then, combining (52) with (51), we can obtain

$$r \sim \mathcal{N} \left( 1, \frac{P_{Tx}^2 M \left( 2 - \frac{M}{N} \right)}{K^3 \sigma^4 \left[ 1 + \left( 1 + \ln \frac{N}{M} \right) \frac{P_{Tx} M}{K \sigma^2} \right]^2} \right). \tag{53}$$

Given a random variable  $r$  with normal distribution, its absolute value  $|r|$  follows a folded normal distribution [11]. Thus, the distribution of  $I_{sel}$  is given by

$$I_{sel} \sim \mathcal{FN} \left( K \log_2 \left[ 1 + \left( 1 + \ln \frac{N}{M} \right) \frac{P_{Tx} M}{K \sigma^2} \right], \frac{(\log_2 e P_{Tx})^2 M \left( 2 - \frac{M}{N} \right)}{K \sigma^4 \left[ 1 + \left( 1 + \ln \frac{N}{M} \right) \frac{P_{Tx} M}{K \sigma^2} \right]^2} \right). \tag{54}$$

## APPENDIX B

## PROOF OF THE THEOREM 6

**Lemma 1.** *For arbitrary energy arrival rates, there exists a randomized control policy which achieves the following steady state values*

$$\begin{aligned}\mathbb{E}\{P_{TX}(t_e)\} &\leq P_{TX,mean} - \epsilon, \\ \mathbb{E}\{C_{total}(\mathcal{S}_{t_e}^*, \mathcal{P}_{t_e}^*) - C_{total}(\mathcal{S}_{t_e}, \mathcal{P}_{t_e})\} &\leq \delta, \\ \mathbb{E}\{U_{sel}(\mathcal{S}_{t_e}, \mathcal{P}_{t_e})\} &\geq \mathbb{E}\{C_{total}(\mathcal{S}_{t_e}, \mathcal{P}_{t_e})\}(q^* - \delta).\end{aligned}\tag{55}$$

*Proof:* A similar proof can be found in [45], [53]. ■

*Remark 5:* It is noted that Lemma 1 still holds as long as the system state can take at most a finite (but arbitrarily large) number of values. Since the system state in our work depends on battery state, energy arrival, renewable energy price, and grid power. With discretization and quantification, we can guarantee that these values as well as the corresponding system state space are also finite.

Substituting (55) into (24) and taking the limit as  $\delta \rightarrow 0$ , we can get

$$\begin{aligned}\Delta(Z(t_e)) - V\mathbb{E}\{U_{sel}(\mathcal{S}_{t_e}, \mathcal{P}_{t_e}) - q(t_e)C_{total}(\mathcal{S}_{t_e}, \mathcal{P}_{t_e})\} \\ \leq C - Vq^*\mathbb{E}\{C_{total}(\mathcal{S}_{t_e}, \mathcal{P}_{t_e})\} + Vq(t_e)\mathbb{E}\{C_{total}(\mathcal{S}_{t_e}, \mathcal{P}_{t_e})\} - \epsilon(Z(t_e)).\end{aligned}\tag{56}$$

When  $Z(t_e) \geq 0$ , (56) can be further simplified as

$$\begin{aligned}\Delta(Z(t_e)) - V\mathbb{E}\{U_{sel}(\mathcal{S}_{t_e}, \mathcal{P}_{t_e}) - q(t_e)C_{total}(\mathcal{S}_{t_e}, \mathcal{P}_{t_e})\} \\ \leq C - Vq^*\mathbb{E}\{C_{total}(\mathcal{S}_{t_e}, \mathcal{P}_{t_e})\} + Vq(t_e)\mathbb{E}\{C_{total}(\mathcal{S}_{t_e}, \mathcal{P}_{t_e})\}.\end{aligned}\tag{57}$$

Applying the law of telescoping sums over  $t_e = \{1, 2, \dots, T_e T_\omega\}$  and the law of iterated expectations, we have

$$\begin{aligned}\mathbb{E}\{L(Z(T_e T_\omega))\} - \mathbb{E}\{L(Z(1))\} - V \sum_{t_e=1}^{T_e T_\omega} \mathbb{E}\{U_{sel}(\mathcal{S}_{t_e}, \mathcal{P}_{t_e}) - q(t_e)C_{total}(\mathcal{S}_{t_e}, \mathcal{P}_{t_e})\} \\ \leq T_e T_\omega [C - Vq^*\mathbb{E}\{C_{total}(\mathcal{S}_{t_e}, \mathcal{P}_{t_e})\}] + V\mathbb{E}\{C_{total}(\mathcal{S}_{t_e}, \mathcal{P}_{t_e})\} \sum_{t_e=1}^{T_e T_\omega} \mathbb{E}\{q(t_e)\}.\end{aligned}\tag{58}$$

Dividing both sides of (58) by  $VT_eT_\omega$ , we can obtain

$$\begin{aligned} & \frac{1}{T_eT_\omega} \sum_{t_e=1}^{T_eT_\omega} \mathbb{E}\{q(t_e)C_{total}(\mathcal{S}_{t_e}, \mathcal{P}_{t_e}) - U_{sel}(\mathcal{S}_{t_e}, \mathcal{P}_{t_e})\} \\ & \leq \frac{C}{V} - q^* \mathbb{E}\{C_{total}(\mathcal{S}_{t_e}, \mathcal{P}_{t_e})\} + \mathbb{E}\{C_{total}(\mathcal{S}_{t_e}, \mathcal{P}_{t_e})\} \frac{1}{T_eT_\omega} \sum_{t_e=1}^{T_eT_\omega} \mathbb{E}\{q(t_e)\} + \frac{\mathbb{E}\{L(Z(1))\}}{VT_eT_\omega}. \end{aligned} \quad (59)$$

Taking the limit  $T_\omega \rightarrow \infty$ , we can derive

$$\begin{aligned} & \lim_{T_\omega \rightarrow \infty} \frac{1}{T_eT_\omega} \sum_{t_e=1}^{T_eT_\omega} \mathbb{E}\{q(t_e)C_{total}(\mathcal{S}_{t_e}, \mathcal{P}_{t_e}) - U_{sel}(\mathcal{S}_{t_e}, \mathcal{P}_{t_e})\} \\ & = \lim_{T_\omega \rightarrow \infty} \left[ \frac{1}{T_eT_\omega} \sum_{t_e=1}^{T_eT_\omega} \mathbb{E}\{q(t_e)C_{total}(\mathcal{S}_{t_e}, \mathcal{P}_{t_e})\} - \frac{1}{T_eT_\omega} \sum_{t_e=1}^{T_eT_\omega} \mathbb{E}\{U_{sel}(\mathcal{S}_{t_e}, \mathcal{P}_{t_e})\} \right] \\ & = \overline{U_{sel}}(\mathcal{S}_{te}, \mathcal{P}_{te}) - \overline{U_{sel}}(\mathcal{S}_{te}, \mathcal{P}_{te}) = 0. \end{aligned} \quad (60)$$

Adding (60) into (59), we can obtain

$$\frac{C}{V} - q^* \mathbb{E}\{C_{total}(\mathcal{S}_{t_e}, \mathcal{P}_{t_e})\} + U_{E^3} \mathbb{E}\{C_{total}(\mathcal{S}_{t_e}, \mathcal{P}_{t_e})\} \geq 0. \quad (61)$$

Rearranging (61), we have

$$U_{E^3} \geq q^* - \frac{C}{V \mathbb{E}\{C_{total}(\mathcal{S}_{t_e}, \mathcal{P}_{t_e})\}} \geq q^* - \frac{C}{VC_{total,min}}, \quad (62)$$

where  $C_{total,min}$  is the minimum value of  $C_{total}(\mathcal{S}_{t_e}, \mathcal{P}_{t_e})$  over the entire period.

Similarly, applying the law of iterated expectations and the law of telescoping sums over  $t_e \in \{1, 2, \dots, T_eT_\omega\}$  for (56), we can get

$$\begin{aligned} & \mathbb{E}\{L(Z(T_eT_\omega))\} - \mathbb{E}\{L(Z(1))\} - V \sum_{t_e=1}^{T_eT_\omega} \mathbb{E}\{U_{sel}(\mathcal{S}_{t_e}, \mathcal{P}_{t_e}) - q(t_e)C_{total}(\mathcal{S}_{t_e}, \mathcal{P}_{t_e})\} \\ & \leq T_eT_\omega [C - Vq^* \mathbb{E}\{C_{total}(\mathcal{S}_{t_e}, \mathcal{P}_{t_e})\}] + V \mathbb{E}\{C_{total}(\mathcal{S}_{t_e}, \mathcal{P}_{t_e})\} \sum_{t_e=1}^{T_eT_\omega} \mathbb{E}\{q(t_e)\} - \epsilon \sum_{t_e=1}^{T_eT_\omega} Z(t_e). \end{aligned} \quad (63)$$

Dividing the both sides of (63) by  $\epsilon T_eT_\omega$  and taking the limit as  $T_\omega \rightarrow \infty$ , we can obtain

$$\begin{aligned} \bar{Z} & = \lim_{T_\omega \rightarrow \infty} \frac{1}{T_eT_\omega} \sum_{t_e=1}^{T_eT_\omega} Z(t_e) \\ & \leq \frac{C - Vq^* \mathbb{E}\{C_{total}(\mathcal{S}_{t_e}, \mathcal{P}_{t_e})\}}{\epsilon} + \frac{V}{\epsilon} \lim_{T_\omega \rightarrow \infty} \frac{1}{T_eT_\omega} \sum_{t_e=1}^{T_eT_\omega} \mathbb{E}\{q(t_e)C_{total}(\mathcal{S}_{t_e}, \mathcal{P}_{t_e})\} \\ & \leq \frac{C + V(U_{sel,max} - q^*C_{total,min})}{\epsilon}. \end{aligned} \quad (64)$$

This completes the proof.

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Zhou, Zhenyu

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